

## Another FREE SAMPLE LAB from TOPS LEARNING SYSTEMS!

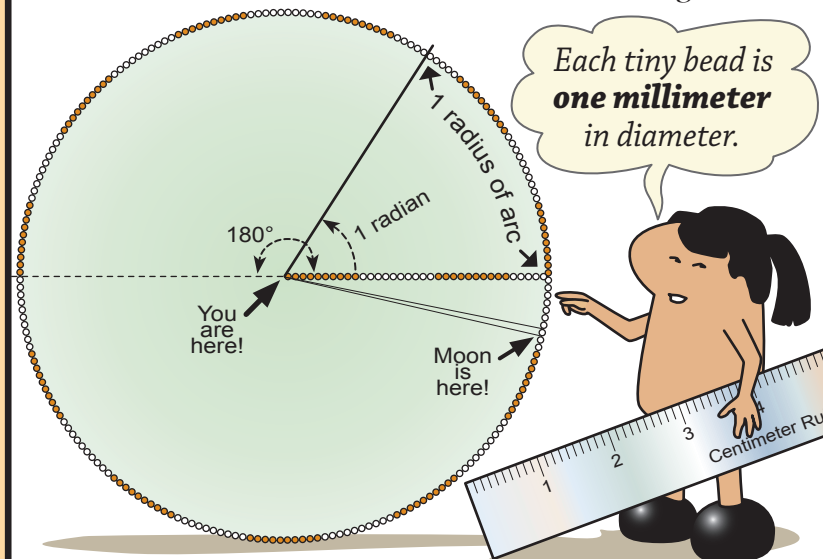
This TOPS Idea is taken from an original series of black-and-white line masters, adapted to stand alone as an independent mini-lesson. Please purchase our original book to get the whole in-depth program.

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### millimeter beads

...adapted from **PI IN THE SKY#45**  
by TOPS Learning Systems

- Count the *mm beads* to find the radius (R), diameter (D), and circumference (C) of this circle. How many D's fit around C? How many R's?
- Argue that  $180^\circ = \pi$  radians.
- If the moon were 35 moon-diameters from Earth, what would be its apparent angular size in radians? In degrees?



- Our moon is *actually* 110 moon-diameters away. What tiny angle does it subtend in your field of view?

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#### OBJECTIVE

To understand the geometry of circles, and how astronomers calculate *apparent angular size*.

#### MODEL ANSWERS

- $R = 35$  mm;  $D = 70$  mm.  $C = 220$  mm.  
D fits into C  $\pi$  times! ( $\pi = 3\frac{1}{7} = \frac{22}{7} = 3.14$ ).  
R fits into C  $2\pi$  times.
- Students might draw 3 one-radian angles, observing that they fall 5 beads short of  $180^\circ$ :  
 $3\frac{5}{35}$  rad =  $3\frac{1}{7}$  rad =  $\pi$  rad =  $180^\circ$
- angular size =  $\frac{1}{35}$  radius of arc  
( $\frac{1}{35}$  rad) ( $180^\circ / \pi$  rad) =  $1.64^\circ$
- angular size =  $\frac{1}{110}$  radian  
( $\frac{1}{110}$  rad) ( $180^\circ / \pi$  rad) =  $0.52^\circ$

#### EVALUATION

- If you divided a pizza into radian slices, how many would you have?  $2\pi$  slices =  $6\frac{2}{7}$  slices
- How big does a paper plate appear when viewed at a distance of 110 paper-plate diameters from your eye?  $\frac{1}{110}$  radian, about  $\frac{1}{2}^\circ$

#### MATERIALS

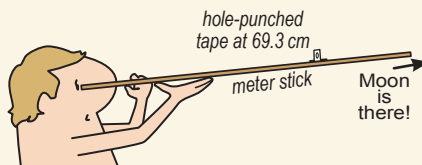
- A metric ruler or straight edge.
- A calculator.

#### EXTENSION

Model the *apparent angular size* of our real moon by holding a paper-punch hole precisely 110 hole-diameters from your eye! Let students engineer creative ways to do this on their own:

moon diameter = 3,480 km  
average orbiting distance = 384,000 km  
10 paper punch diameters = 6.3 cm  
110 paper punch diameters = 69.3 cm

Use string, straws and tape; or adding machine tape; or paper-punched masking tape stuck to a window; or a meter stick.... The moon can't possibly look this small! Can it?



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- 06 METRIC MEASURE (gr 8-12)
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- 20 MAGNETISM (gr 8-12)
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- 22 MACHINES (gr 7-12)
- 23 ROCKS & MINERALS (gr 6-12)
- 31 PERFECT BALANCE (gr K-12)
- 32 ELECTRICITY (gr 3-8)
- 33 MAGNETISM (gr 3-8)
- 34 PENDULUMS (gr 4-9)
- 35 METRIC MEASURING (gr 5-9)
- 36 MORE METRICS (gr 6-10)
- 37 ANIMAL SURVIVAL (gr 3-8)
- 38 Green Thumbs: RADISHES (gr 3-8)
- 39 Green Thumbs: CORN & BEANS (gr 4-12)
- 40 EARTH, MOON & SUN (gr 7-12)
- 41 PLANETS & STARS (gr 7-12)
- 42 FOCUS POCUS (gr 5-10)
- 43 FAR OUT MATH (gr 9-12)
- 44 SCALE THE UNIVERSE (gr 5-12)
- 45 PI IN THE SKY (gr 5-12)
- 61 A SUMMER START (gr 1-8)
- 62 Intermediate ABC SOUP (gr 4-8)
- 63 PEACEFUL PROCEDURES (gr 1-8)
- 64 Primary ABC SOUP (gr 1-3)
- 71 Primary LENTIL SCIENCE (gr K-3)
- 72 Intermediate LENTIL SCIENCE (gr 3-6)
- 73 GET A GRIP Workstation (gr K-6)
- 91 GLOBAL TOPS (gr 3-10)
- 100 TRIPLE MAGNIFIER (gr 3-12)
- 200 CARTESIAN DIVER (adapts K-12)

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