TRANSFORMATIONS — TRANSLATIONS AND REFLECTIONS Model

Foundational Concepts

Some students may still need to acquire some of the following Foundational Concepts. Remember to seize teachable moments during the lesson by embedding these concepts and terms as opportunities arise. This allows students to practice their emerging numeracy skills while also having access to high school–level materials and standards.

- A coordinate plane is a plane containing an x-axis and a y-axis.
- Numbers can be positive or negative on the coordinate plane.
- Points can be plotted on a coordinate plane.
- Coordinates are pairs of numbers that tell an exact location on a coordinate plane.
- Horizontal, vertical, diagonal, clockwise, and counterclockwise are direction words.

Essential Understandings / Big Ideas

- A transformation is a movement of a shape on a plane.
- A translation slides and a reflection flips.

Learning Objectives

- Identify two types of transformations: translations and reflections
- Demonstrate a translation by sliding a figure
- Demonstrate a reflection by flipping a figure

Challenge Objective

• Given origin points and directions for movement, complete a translation and a reflection and determine the ending points



Materials

Supplied

- Access Geometry Student Workbook (pgs. 7–10)
- Vocabulary cards: *reflection, rotation, transformation, translation*
- Coordinate Plane poster
- Student Workbook pages for Lesson 2 (project from the digital files)
- Shapes: triangles, rectangles, and squares
- Dry-erase marker
- Problem statement for Lesson 2 (Appendix C or print from the digital file)
 Vocabulary cards: *slide, flip, vertical, horizontal, diagonal* Number stamps

To Bring From Home

• A toy Transformer or an item to demonstrate a transformation

🔁 Wikki Stix

🔁 Small removable circle stickers to plot points

🔁 Glue stick

Lesson Preparation

- 1. Project Lesson 2 from the Student Workbook onto a whiteboard.
- 2. If needed for students who have difficulty writing, print the problem statement for Lesson 2 from the digital file (or photocopy Appendix C.) Copy and cut out enough problem statements to have on hand for these students to use as they work.
- 3. Program AAC devices with response options: Vocabulary words; yes and no; Lesson 2 problem statement and big ideas; flip, slide; birds, mountain; things seen sliding.
- 4. Review sign language for *flip* and *slide* by searching the terms: *sign language for flip* and *sign language for slide*.

- 5. Build a coordinate plane with an origin point and *x* and *y*-axes using masking tape on the floor of the classroom.
- 6. Search online for examples of transformations. At the time of publication, the following resources were active: www.mathsisfun.com/geometry/translation.html www.mathsisfun.com/geometry/reflection.html www.geogebra.org/geometry?lang=en www.nctm.org/Classroom-Resources/Illuminations/ Interactives/Shape-Cutter/

M Prompts for Modeling

Model each step of the Task Analysis in the Student Workbook. Have students follow your model. If needed, prompt using the least intrusive prompt (LIP) as follows:

- I If a student does not respond, give a verbal prompt (e.g., Write the problem in your Student Workbook).
- 2 If the student still does not respond or responds incorrectly, model the step again and repeat your verbal prompt to give the student another opportunity to respond.
- **3** If still no response, physically guide the student to complete the step.

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ENGAGE THE STUDENTS

Engage the students and introduce the lesson.

	Student Response
Set up the day's lesson: Today we are going to learn about <i>transformations</i> ! Let's clap that long word out. Clap the syllables in <i>trans-for-ma-tion</i> .	Responds by clapping out the syllables
	Responds by clapping, tapp moving to the syllables
Excellent! Now say that word with me: transformation. Call on various students to practice saying	Responds in chorus
the word.	Responds in chorus using a AAC device
A transformation is a change. Show a toy Transformer. Say, This toy shows a transformation. How	Responds <i>a change</i>
many of you have seen a Transformer like this? If you have seen the toy change, you have seen a transformation. Encourage students to share what they know about Transformers.	Responds in chorus using a AAC device
Ask, What is a transformation? Wait for students to respond.	
Very good. In geometry, a <i>transformation</i> is a change of a shape. The change can be as simple as moving the figure without changing its size or shape, like this. Demonstrate moving an object in your room. Describe how the figure's size and shape did not change. Say, I just transformed this [chair]. The transformation was the movement. Say, We call this a rigid transformation, meaning that we didn't change its size and shape, just its position. Other transformations can change the size of the figure or the shape of the figure.	
In this unit, we will only study transformations that move a shape — a rigid transformation. We are going to learn about three rigid transformations: 1. translations, 2. reflections, and 3. rotations.	
These transformations all have to do with movement of a shape. One of our big ideas in this lesson is that: <i>A transformation is a movement of a shape on a plane.</i>	
Today you will learn more about transformations. Hold up the Vocabulary card for <i>transformation</i> . We'll be talking about two of the movements you see on this Vocabulary card for <i>transformation</i> . And I'll show you have to follow the store of a Task Analysis to solve a math store problem related to transformations.	



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	Teacher Instructions		Student Response
	slide: to move a shape without turning it or	vertical: going up and down	
	flipping it <i>symmetry:</i> another name for reflection; when	<i>x-axis:</i> a line on a graph that runs horizontally (left to right)	
	one half is a reflection of the other half <i>turn:</i> to rotate around a point	y-axis: a line on a graph that runs vertically (up and down)	
3	Outline the lesson and link it to	o the students' prior knowledge.	1
100	Teacher Instructions		Student Response
	Begin the lesson: Remember, I told you a rigid tra it. The size or shape of the figure doesn't change	ansformation is a change made to a figure by moving e. Rigid transformations happen all around us.	
	Have you ever seen a plane take off and fly into ground to the sky, but it is still the same size. It slide into the sky. A transformation where the r) the sky? The plane changes positions from the is still the same shape. The movement is like a novement is a slide is a called a <i>translation</i> .	Responds <i>yes</i> or <i>no</i>
	Hold up the Vocabulary card for <i>translation</i> and See the arrows? Have you ever slid anything or	l say, The square in this picture shows it was slid. r seen sliding? Demonstrate the sign for slide. Have	Responds <i>yes</i> or <i>no</i> and then names things slid or seen sliding
	students name some examples of sliding, like sl in baseball.	iding on ice, sliding on a slide, or sliding into a base	₽ Responds <i>yes</i> or <i>no</i> ; signs the word <i>slide</i>
-	Explain the next transformation — <i>reflection</i> . H you look at your reflection in the mirror, you still flipped and reflected in the mirror. This type of the Vocabulary card for <i>reflection</i> and point out how Demonstrate the sign for reflection or flip	ave you ever seen your reflection in a mirror? When Il see you, not a changed you. Your face is simply transformation is called a <i>reflection</i> . Hold up the w the triangle is just flipped to make a reflection.	Responds <i>yes</i> or <i>no</i>

Teacher Instructions	Student Response
Place the Coordinate Plane poster on a table. These are the two types of transformations we will talk about in this lesson: translations and reflections.	Responds <i>slide</i> Given 2 Vocabulary cards,
Does translation mean to "flip," "slide," or "turn"? Use the sign for these actions.	chooses the card for <i>slide</i>
Very good. A translation is a slide, like this. Demonstrate sliding a shape on the Coordinate Plane poster.	Translates the shape in any direction on the coordinate plane in the Student Workbook
Give each student a triangle shape. Say, Open your Student Workbook to Lesson 2. You will see a coordinate plane on page 9 in Lesson 2. Use the triangle to show a translation on the coordinate plane in your Student Workbook.	E Slides the shape in any direction on the coordinate plane in the Student Workbook
NOTE : The Coordinate Plane poster can also be used by students to demonstrate the translations and the reflections.	
Say, Translations are slides that can be done vertically, horizontally, or diagonally. Show me with your finger which way is vertical.	Uses finger to show an up and down motion
	Given 2 Vocabulary cards, chooses <i>vertical</i> and then moves hand up and down
Great. Now show me with your finger which way is horizontal.	Uses finger to show a horizontal direction
	➡ Given 2 Vocabulary cards, chooses <i>horizontal</i> and then moves hand left to right
Perfect. Now show me with your finger which way is diagonal.	Uses finger to show a corner-to- corner direction
	Given 2 Vocabulary cards, chooses <i>diagonal</i> and then

Teacher Instructions	Student Response
Let's use your triangle to demonstrate sliding horizontally. Put your triangle on the coordinates (0, 2), (6, 8), and (10, 0). This is in Quadrant I. Now we are going to translate it to Quadrant II	Starts the shape at the coor and then translates it horizo
horizontally.	₩ With guidance, slides the horizontally from Quadran Quadrant II
Next, let's translate it to Quadrant III vertically.	Translates the triangle vert
	With guidance, slides the vertically from Quadrant to Quadrant III
Last, let's translate it to Quadrant I diagonally.	Translates the triangle diag
NOTE : When repeating the lesson, choose different origin points to start, move across different quadrants, and practice with squares or other shapes.	d With guidance, slides the diagonally from Quadrant Quadrant I
The second type of transformation in this lesson is a reflection. Does <i>reflection</i> mean to flip, slide,	Responds <i>flip</i>
or turn? Use the sign for these actions.	🔁 Responds using the sign f
Very good. A reflection is a flip. Demonstrate flipping a triangle on the Coordinate Plane poster. Now, let's use your triangle to demonstrate a reflection — a flip — on the coordinate plane in your Student Workbook.	Reflects the shape in any di on the coordinate plane in t Student Workbook
	Flips the shape in any dire on the coordinate plane ir Student Workbook to show reflection



TEACH THE TASK ANALYSIS

Listen to or read the math story.

Teacher Instructions

Say, **OK**, **let's begin**. Point to the Task Analysis in the Student Workbook. Say, **This is a list of steps** that will help us solve today's math story. We call it a *Task Analysis*. We will follow the steps on this Task Analysis and check them off (\checkmark) one at a time as we complete them.

Let's turn the page. Read the math story with me. Read the math story and encourage the students to follow along.

Student Response

Listens to the story being read; follows along in the Student Workbook

Watches as the words are read and pointed to



Read the math story.

Painting with Transformations

Maria is an artist. She is painting a landscape picture. She has already painted some mountains, but she wants to reflect the mountain in the lake below it. The reflection must match the mountain exactly. She also painted a bird on the ground. She wants to paint another bird just like it to look like the bird has taken flight.

Figure 1: Maria plotted the points of the first figure using these coordinates: (1, 2), (3, 2), and (5, 2). She connected the points with curved lines. To transform the figure, she plotted these coordinates (5, 6), (7, 6), and (9, 6). She connected these points with curved lines.

Figure 2: Maria plotted these coordinates for the second figure: (-10, 0), (-7, 6), (-5, 2), (-3, 6), and (0, 0). She connected these points with straight lines. To transform this figure, she plotted these coordinates (-10, 0), (-7, -6), (-5, -2), (-3, -6), and (0, 0). She connected these points with straight lines.

What types of transformations did Maria use?

X		
	Teacher Instructions	Student Response
\triangleleft	Point to the Task Analysis in the Student Workbook. We just read the math story, so let's go back a page to the Task Analysis and check off (Checks off Step 1 Finds Step 1 on the Task Analysis and checks it off with your help
2 C	Identify the problem.	
	Teacher Instructions	Student Response
	Review the math story, In this math story, Maria (the artist) will make two types of transformations She will make two types of changes to her painting. She will use what she knows about geometry to make these changes .	s. /
	Say, Let's talk about the transformations. In this math story, one transformation has to do with the mountains and one transformation has to do with the bird. One of our big ideas in this lesson is that: A transformation is a movement of a shape on a plane.	
	Point to the math story in the Student Workbook. (As an alternative, project the Student Workbook pages onto a whiteboard.) Have students identify the problem to be solved. Let's find the problem we will be solving. Point to the problem statement in the story. I see this question: What types of transformations did Maria use? I will underline this question because this is the problem I have to solve. Your turn. Underline this question in your Student Workbook.	Finds and underlines the question Given 2 choices, chooses the correct problem statement
	what ty	pes of transformations did Maria use

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Plot the transformed figure(s) on the coordinate plane.

Teacher Instructions

Let's plot the transformed Figure 1 on the coordinate plane.

Using the Coordinate Plane poster, plot the points using the coordinates of transformed Figure 1. Explain while you plot the points using the coordinates, **The transformed Figure 1 is placed at** (5, 6), (7, 6), and (9, 6). I know the first number in a coordinate pair goes on the *x*-axis and the second number goes on the *y*-axis. I'll connect the points with curved lines, like this. Your turn. Plot these points and connect them using curved lines.

Let's plot the second figure on the coordinate plane. Using the Coordinate Plane poster, plot the points of transformed Figure 2. Explain while you plot the points using the coordinates, The second figure is placed at (-10, 0), (-7, -6), (-5, -2), (-3, -6), and (0, 0). I know the first number in a coordinate pair goes on the *x*-axis and the second number goes on the *y*-axis. I'll connect the points in this order with straight lines. Your turn.

We plotted the points of the transformed figures on the coordinate plane, so we can check off (\checkmark) Step 4 of the Task Analysis in your Student Workbook.



Student Response

Plots the points using coordinates for transformed Figure 2 and then connects the points with curved lines

Plots the points with support (using removable circle stickers if needed) and then connects the points (using Wikki Stix if needed)

Plots the points of transformed Figure 2 and then connects the points with straight lines

Plots the points with support (using removable circle stickers if needed) and then connects the points (using Wikki Stix if needed)

Checks off Step 4

Finds Step 4 on the Task Analysis and checks it off with your help

Teacher Instructions	Student Response
One of the big ideas in this lesson is that: <i>A transformation is a movement of a shape on a plane</i> Say, The artist performed two transformations in her painting. We must decide which types of transformations she used for each figure.	
Using the Coordinate Plane poster, say, Let's look at this coordinate plane. You can look at the coordinate plane in your Student Workbook too.	
Figure 1 was placed at (1, 2), (3, 2), and (5, 2). The points are connected with curved lines. The transformed figure's coordinates are (5, 6), (7, 6), and (9, 6). What does it look like Maria did?	Responds <i>slid the shape</i>
Help students determine the type of transformation by demonstrating the transformation. Say, What type of transformation is this?	Responds <i>translation</i>
That's correct. This is a translation. The transformed shape and size are the same as the original shap The figure just moved diagonally. The x-coordinate moved +4 units to the right and the y-coordinate moved +4 units up. Every point of the shape moved the same distance in the same direction.	e. Responds <i>bird</i>
ls this the bird or the mountains?	
That's correct. Let's write translation next to the transformed bird.	Writes <i>translation</i> next to the transformed bird
	Given 2 Vocabulary cards, chooses the card for <i>translation</i> and places it next to the bird on the coordinate plane

Teacher Instructions	Student Response
Let's look at Figure 2. Figure 2 was placed at (-10, 0), (-7, 6), (-5, 2), (-3, 6), and (0, 0). The points are	Responds she flipped the fig
connected with straight lines. The transformed figure's coordinates are (-10, 0), (-7, -6), (-5, -2), (-3, -6), and (0, 0). What does it look like Maria did?	Given 2 Vocabulary cards chooses the card for <i>flip</i>
Help students determine the type of transformation by demonstrating the transformation. Say, What type	Responds reflection
of transformation is this?	Given 2 Vocabulary cards chooses the card for <i>refle</i>
That's correct. This transformation is a reflection. The transformed shape and size are the same as the original shape. The figure just flipped to be a reflection. Notice how all the coordinates in the transformed figure had a negative, or inverse, <i>y</i> -axis coordinate. This is how we know it is a reflection. Looking at our coordinate plane, you can see that it is a reflection across the <i>x</i> -axis.	Responds <i>mountains</i>
Is this the bird or the mountains?	
That's correct. Let's write <i>reflection</i> next to the mountains.	Writes <i>reflection</i> next to the mountains
	Given 2 Vocabulary cards chooses <i>reflection</i> and pl it next to the mountains o coordinate plane
We have identified the types of transformations and labeled them on the coordinate plane. This is	Checks off Step 5
one of our big ideas: A translation slides and a reflection flips. Let's check off (\checkmark) Step 5.	Finds Step 5 on the Task Analysis and checks it of

6	State the solution to the math story problem.	
	Teacher Instructions	Student Response
	Let's look back at the problem to be solved. The question to solve was "What types of transformations did Maria use?" A big idea in this lesson is that: <i>a transformation is a movement of a shape on a plane.</i>	
	Model stating the solution using the Student Workbook pages projected onto a whiteboard. Say, We just decided that Maria used a translation for the bird and a reflection for the mountains. I will circle <i>translation</i> for the bird and <i>reflection</i> for the mountains in the Student Workbook. Your turn.	Circles translation for the bird and reflection for the mountains in the Student Workbook Circles or marks translation for the bird and reflection for the mountains in the Student Workbook
	This is one of our big ideas: A translation slides and a reflection flips.	Checks off Step 6
	I will now be able to check off (\checkmark) Step 6. You can do the same.	Finds Step 6 on the Task Analysis and checks it off with your help
P	Fill in the big ideas.	1
	Teacher InstructionsSay, Now, let's review the big ideas we learned. Let's think about this together.We learned that: A transformation is a movement of a shape on a plane. We also learned about two types of transformations that involve movement of the shape: translation and reflection. A translation slides and a reflection flips.	Student Response
	Let's fill in both big ideas in your Student Workbook.	Fills in the big ideas Circles the correct responses to complete the big ideas



CHALLENGE PROBLEM

To add challenge to the lesson, print this Challenge Problem and a blank Coordinate Plane Graphic Organizer (Appendix B) from the digital file. Distribute to students who are ready for a challenge.

Remind students that there are two rules for performing translations and reflections.

- For translations, each point of the shape is moved the same distance (or number of units) in the same direction.
- For triangles that are *reflections* and that cross a vertical line of symmetry, two points on the vertical line of symmetry will stay the same, but the third point changes. The same applies for reflections across a horizontal line of symmetry. The lengths of the sides of the triangle do not change, so the point will be the same distance on the reflected side of the figure after the reflection.

Read the story aloud to students before they begin to solve the problem.

Nick is an artist who is drawing a new lake picture with two sailboats in the lake. He wants them to be a distance apart and of equal size. He uses what he knows about geometry to make the drawing work. He uses triangles on a coordinate plane as the sailboats. He places the first sailboat — triangle ABC — at the coordinates (-6, 2), (-2, 2), and (-4, 6). Nick performs a translation of +8 units right, -6 units down to paint the second sailboat — triangle DEF. Nick also wants each sailboat to have a reflection in the water across a line of symmetry. The line of symmetry is the base of the triangle.

What are the coordinates for the second sailboat's position in the water? Also find the coordinates for the reflections of both boats.

Answer:

Sailboat DEF translated coordinates are (2, -4), (6, -4), and (4, 0). Sailboat ABC's reflection is (-6, 2), (-2, 2), and (-4, -2). Sailboat DEF's reflection is (2, -4), (6, -4), and (4, -8). The coordinate points on the line of symmetry (the base of the triangle) remain constant, but the coordinate point that is reflected across the line of symmetry changes to +8 units, which allows the length of the sides to remain the same.

CHALLENGE PROBLEM ANSWERKEY



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