

# TRANSFORMATIONS TRANSLATIONS AND REFLECTIONS <br> <br> Model 

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## Foundational Concepts

Some students may still need to acquire some of the following Foundational Concepts. Remember to seize teachable moments during the lesson by embedding these concepts and terms as opportunities arise. This allows students to practice their emerging numeracy skills while also having access to high school-level materials and standards.

- A coordinate plane is a plane containing an $\boldsymbol{x}$-axis and a $\boldsymbol{y}$-axis.
- Numbers can be positive or negative on the coordinate plane.
- Points can be plotted on a coordinate plane.
- Coordinates are pairs of numbers that tell an exact location on a coordinate plane.
- Horizontal, vertical, diagonal, clockwise, and counterclockwise are direction words.


## Essential Understandings / Big Ideas

- A transformation is a movement of a shape on a plane.
- A translation slides and a reflection flips.



## La Learning Objectives

- Identify two types of transformations: translations and reflections
- Demonstrate a translation by sliding a figure
- Demonstrate a reflection by flipping a figure


## $\sum$ Challenge Objective

- Given origin points and directions for movement, complete a translation and a reflection and determine the ending points


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## Materials

## Supplied

- Access Geometry Student Workbook (pgs. 7-10)
- Vocabulary cards: reflection, rotation, transformation, translation
- Coordinate Plane poster
- Student Workbook pages for Lesson 2 (project from the digital files)
- Shapes: triangles, rectangles, and squares
- Dry-erase markerProblem statement for Lesson 2
(Appendix C or print from the digital file)
I+ Vocabulary cards: slide, flip, vertical, horizontal, diagonal
$\ddagger$ Number stamps


## To Bring From Home

- A toy Transformer or an item to demonstrate a transformation

ㅍ] Wikki Stix
$\ddagger$ Small removable circle stickers to plot points
++| Glue stick

## Lesson Preparation

1. Project Lesson 2 from the Student Workbook onto a whiteboard.
2. If needed for students who have difficulty writing, print the problem statement for Lesson 2 from the digital file (or photocopy Appendix C.) Copy and cut out enough problem statements to have on hand for these students to use as they work.
3. Program AAC devices with response options: Vocabulary words; yes and no; Lesson 2 problem statement and big ideas; flip, slide; birds, mountain; things seen sliding.
4. Review sign language for flip and slide by searching the terms: sign language for flip and sign language for slide.
5. Build a coordinate plane with an origin point and $\boldsymbol{x}$ - and $\boldsymbol{y}$-axes using masking tape on the floor of the classroom.
6. Search online for examples of transformations. At the time of publication, the following resources were active:
www.mathsisfun.com/geometry/translation.html www.mathsisfun.com/geometry/reflection.html www.geogebra.org/geometry?lang=en www.nctm.org/Classroom-Resources/IIluminations/ Interactives/Shape-Cutter/

## (M) Prompts for Modeling

Model each step of the Task Analysis in the Student Workbook. Have students follow your model. If needed, prompt using the least intrusive prompt (LIP) as follows:1 If a student does not respond, give a verbal prompt
(e.g., Write the problem in your Student Workbook).

2 If the student still does not respond or responds incorrectly, model the step again and repeat your verbal prompt to give the student another opportunity to respond.

3 If still no response, physically guide the student to complete the step.


## ENGAGE THE STUDENTS

## 1 Engage the students and introduce the lesson.

## Teacher Instructions

Set up the day's lesson: Today we are going to learn about transformations! Let's clap that long word out. Clap the syllables in trans-for-ma-tion.

Excellent! Now say that word with me: transformation. Call on various students to practice saying the word.

A transformation is a change. Show a toy Transformer. Say, This toy shows a transformation. How many of you have seen a Transformer like this? If you have seen the toy change, you have seen a transformation. Encourage students to share what they know about Transformers

Ask, What is a transformation? Wait for students to respond.
Very good. In geometry, a transformation is a change of a shape. The change can be as simple as moving the figure without changing its size or shape, like this. Demonstrate moving an object in your room. Describe how the figure's size and shape did not change. Say, I just transformed this [chair]. The transformation was the movement. Say, We call this a rigid transformation, meaning that we didn't change its size and shape, just its position. Other transformations can change the size of the figure or the shape of the figure.

In this unit, we will only study transformations that move a shape - a rigid transformation. We are going to learn about three rigid transformations: 1. translations, 2. reflections, and 3. rotations.

These transformations all have to do with movement of a shape. One of our big ideas in this lesson is that: A transformation is a movement of a shape on a plane.

Today you will learn more about transformations. Hold up the Vocabulary card for transformation. We'll be talking about two of the movements you see on this Vocabulary card for transformation. And I'll show you how to follow the steps of a Task Analysis to solve a math story problem related to transformations.

Student Response
Responds by clapping out the syllablesResponds by clapping, tapping, moving to the syllables

Responds in chorusResponds in chorus using an AAC device

Responds a change
 AAC device

[^0]
## 2 Review the vocabulary terms.

## Teacher Instructions

## Say, Before we get to our lesson, let's review this unit's vocabulary words.

Use the Vocabulary cards to review each term and definition using the constant time-delay procedure described on page 51.

## Definitions

reflection: moving a figure by flipping it across a line without changing its size or shape
rotation: moving an object around a fixed point in a circle
transformation: changing a shape using a turn, flip, or slide
translation: moving a figure by sliding it without changing its size or shape

NOTE: You may also need to review the following foundational vocabulary as they come up in the lesson.
clockwise: moving in the direction of the hands on a clock
coordinate plane: a plane containing an $x$-axis and a $\boldsymbol{y}$-axis
coordinates $(x, y)$ : pairs of numbers that tell an exact position
counterclockwise: moving in the opposite direction of the hands on a clock
diagonal: a line segment that goes from one corner to another, but is not an edge
flip: to turn something over
horizontal: going side to side, like the horizon negative number: a number less than zero origin point: the point where the $x$-axis and the $y$-axis meet ( 0,0 )
positive number: a number greater than zero

## Student Response

## Responds by selecting the correct

 Vocabulary card given 4 cards to choose from[+] Responds by selecting or eyegazing to the correct Vocabulary card given 2 or 3 cards to choose from


Teacher Instructions
slide: to move a shape without turning it or flipping it
symmetry: another name for reflection; when one half is a reflection of the other half turn: to rotate around a point
vertical: going up and down
$\boldsymbol{x}$-axis: a line on a graph that runs horizontally (left to right)
$\boldsymbol{y}$-axis: a line on a graph that runs vertically (up and down)

Student Response
...........................


3 Outline the lesson and link it to the students' prior knowledge.

## Teacher Instructions

Begin the lesson: Remember, I told you a rigid transformation is a change made to a figure by moving it. The size or shape of the figure doesn't change. Rigid transformations happen all around us.

Have you ever seen a plane take off and fly into the sky? The plane changes positions from the ground to the sky, but it is still the same size. It is still the same shape. The movement is like a slide into the sky. A transformation where the movement is a slide is a called a translation.

Hold up the Vocabulary card for translation and say, The square in this picture shows it was slid. See the arrows? Have you ever slid anything or seen sliding? Demonstrate the sign for slide. Have students name some examples of sliding, like sliding on ice, sliding on a slide, or sliding into a base in baseball.

Explain the next transformation - reflection. Have you ever seen your reflection in a mirror? When you look at your reflection in the mirror, you still see you, not a changed you. Your face is simply flipped and reflected in the mirror. This type of transformation is called a reflection. Hold up the Vocabulary card for reflection and point out how the triangle is just flipped to make a reflection. Demonstrate the sign for reflection or flip.

Student Response

Responds yes or no

Responds yes or no and then names things slid or seen sliding
$\ddagger$ Responds yes or no; signs the word slide

Responds yes or no

## Teacher Instructions

Place the Coordinate Plane poster on a table. These are the two types of transformations we will talk about in this lesson: translations and reflections.

Does translation mean to "flip," "slide," or "turn"? Use the sign for these actions.
Very good. A translation is a slide, like this. Demonstrate sliding a shape on the
Coordinate Plane poster.
Give each student a triangle shape. Say, Open your Student Workbook to Lesson 2. You will see a coordinate plane on page 9 in Lesson 2. Use the triangle to show a translation on the coordinate plane in your Student Workbook.

NOTE: The Coordinate Plane poster can also be used by students to demonstrate the translations and the reflections.

Say, Translations are slides that can be done vertically, horizontally, or diagonally. Show me with your finger which way is vertical.

## Great. Now show me with your finger which way is horizontal.

## Perfect. Now show me with your finger which way is diagonal.

## Student Response

Responds slide
 chooses the card for slide

Translates the shape in any direction on the coordinate plane in the Student Workbook

田
$\ddagger$ Slides the shape in any direction on the coordinate plane in the Student Workbook

## Uses finger to show an up and

 down motionGiven 2 Vocabulary cards, chooses vertical and then moves hand up and down
## Uses finger to show a horizonta

 directionGiven 2 Vocabulary cards, chooses horizontal and then moves hand left to rightUses finger to show a corner-tocorner direction$\ddagger$ Given 2 Vocabulary cards, chooses diagonal and then moves hand in a corner-tocorner manner

## Teacher Instructions

Let's use your triangle to demonstrate sliding horizontally. Put your triangle on the coordinates $(0,2),(6,8)$, and $(10,0)$. This is in Quadrant I. Now we are going to translate it to Quadrant II horizontally.

## Next, let's translate it to Quadrant III vertically.

## Last, let's translate it to Quadrant I diagonally.

NOTE: When repeating the lesson, choose different origin points to start, move across different quadrants, and practice with squares or other shapes.

The second type of transformation in this lesson is a reflection. Does reflection mean to flip, slide, or turn? Use the sign for these actions.

Very good. A reflection is a flip. Demonstrate flipping a triangle on the Coordinate Plane poster. Now, let's use your triangle to demonstrate a reflection - a flip - on the coordinate plane in your Student Workbook.

## Teacher Instructions

Reflections are flips that can be done across a mirror line - we call that the line of symmetry. In other words, the shape on both sides of the line will match exactly. Let's practice using the $x$-axis as the line of symmetry.

Show me again with your hand which way the $x$-axis goes.
Great. Now, show me with your hand which way the $y$-axis goes.

A reflection is a flip, so first I will practice flipping across the $\boldsymbol{x}$-axis. Put your triangle on the coordinates ( 0,2 ), $(6,8)$, and ( 10,0 ).

## Now let's flip the triangle across the $\boldsymbol{x}$-axis like this.

Model flipping the shape, keeping the base side on (0, 2) and (10, 0). Your turn.


Great job! You reflected the triangle across the $x$-axis. The $x$-axis is the line of symmetry the mirror line. The triangle looks the same on both sides of the $x$-axis.

When repeating this lesson, perform the same task across the $\boldsymbol{y}$-axis using new coordinates. For additional lessons, use different shapes with four points, such as rectangles or squares.

Say, Very good. We have demonstrated both reflections and translations. Another of our big ideas in this lesson is that: $\boldsymbol{A}$ translation slides and a reflection flips.

Nice work.

## Student Response

Uses hand motion to show horizontal direction
$+\ddagger$ Points to the $\boldsymbol{x}$-axis

## Shows vertical direction

 with hand$\ddagger$ Points to the $y$-axis
Starts the shape at the coordinates given
[ + Places the triangle on the Coordinate Plane poster that has been pre-marked with dots for coordinate points, then reflects the shape

Flips the shape across the $x$-axis

## TEACH THE TASK ANALYSIS

## Listen to or read the math story.

## Teacher Instructions

Say, OK, let's begin. Point to the Task Analysis in the Student Workbook. Say, This is a list of steps that will help us solve today's math story. We call it a Task Analysis. We will follow the steps on this Task Analysis and check them off $(\checkmark)$ one at a time as we complete them.

Let's turn the page. Read the math story with me. Read the math story and encourage the students to follow along.

## Student Response

Listens to the story being read; follows along in the Student Workbook
$\mp+$ Watches as the words are read and pointed to

Teacher Instructions
Point to the Task Analysis in the Student Workbook. We just read the math story, so let's go back a page to the Task Analysis and check off ( $\checkmark$ ) Step 1.

## Student Response

Checks off Step 1$\ddagger$ Finds Step 1 on the Task Analysis and checks it off with your help

## Identify the problem.

## Teacher Instructions

Review the math story, In this math story, Maria (the artist) will make two types of transformations. She will make two types of changes to her painting. She will use what she knows about geometry to make these changes.

Say, Let's talk about the transformations. In this math story, one transformation has to do with the mountains and one transformation has to do with the bird. One of our big ideas in this lesson is that: A transformation is a movement of a shape on a plane.

Point to the math story in the Student Workbook. (As an alternative, project the Student Workbook pages onto a whiteboard.) Have students identify the problem to be solved. Let's find the problem we will be solving. Point to the problem statement in the story. I see this question: What types of transformations did Maria use? I will underline this question because this is the problem I have to solve. Your turn. Underline this question in your Student Workbook.

## Student Response

## Finds and underlines the question

Given 2 choices, chooses the correct problem statement

Teacher Instructions
Now, I will write this problem statement in the Student Workbook. Your turn. Write the problem to be identified in the space for Step 2.

We have identified the problem, so we can check off $(\checkmark)$ Step 2 on the Task Analysis in your Student Workbook. You will have to flip back one page to the Task Analysis.

## Student Response

Writes the problem statement in the Student Workbook

ㅍ] Glues the problem statement in the space provided in the Student Workbook

## Checks off Step 2

Finds Step 2 on the Task Analysis and checks it off with your help
## 3 IIEP (x,y) Plot the original figure(s) on the coordinate plane.

## Teacher Instructions

Let's plot the first figure on the coordinate plane.
Using the Coordinate Plane poster, plot the points using the coordinates of Figure 1. Explain while you plot the points, The first figure is placed at $(1,2),(3,2)$, and $(5,2)$. I know the first number in a coordinate pair goes on the $x$-axis and the second number goes on the $y$-axis. I will mark these points with my marker, $x$-axis first and then up for the $y$-axis.

Maria connected the points with curved lines so I will do that. Your turn. Use your pencil. Plot the points using the coordinates $-x$-axis first, then up for the $y$-axis. Connect them using curved lines.


## Student Response

Plots the points using coordinates for Figure 1
$\ddagger \downarrow$ Plots the points with support (using removable circle stickers if needed)

Connects the points with curved lines
[ + Connects the points (using Wikki Stix if needed)

Teacher Instructions
To help me remember this is Figure 1, I will mark this shape Figure 1. You do the same.

Let's plot the points of the second figure on the coordinate plane. Using the Coordinate Plane poster, plot the points using the coordinates of Figure 2. Explain while you plot the points, The second figure is placed at $(-10,0),(-7,6),(-5,2),(-3,6)$, and $(0,0)$. I know the first number in a coordinate pair goes on the $x$-axis and the coordinate is negative so I will mark on the left side of 0 . The second number goes on the $y$-axis. It's positive so I will go up. You try it. Plot the points using the coordinates in your Student Workbook.

I'll connect the points in this order with straight lines. Your turn.

## To help me remember this is Figure 2, I will mark this shape Figure 2.

We plotted the figures on the coordinate plane, so we can check off $(\checkmark)$ Step 3 on the Task Analysis in your Student Workbook.


## Student Response

Labels the shape as Figure 1
$\ddagger$ Stamps 1 near the shape
Plots the points using coordinates for Figure 2

+     + Plots the points with support (using removable circle stickers if needed)

Connects the points with straight lines
$\ddagger$ Connects the points (using Wikki Stix if needed)

Labels the shape as Figure 2Stamps 2 near the shape

Checks off Step 3
[ $\ddagger$ Finds Step 3 on the Task Analysis and checks it off with your help

## 4

## Plot the transformed figure(s) on the coordinate plane.

## Teacher Instructions

## Let's plot the transformed Figure 1 on the coordinate plane.

Using the Coordinate Plane poster, plot the points using the coordinates of transformed Figure 1. Explain while you plot the points using the coordinates, The transformed Figure $\mathbf{1}$ is placed at $(5,6),(7,6)$, and $(9,6)$. I know the first number in a coordinate pair goes on the $x$-axis and the second number goes on the $y$-axis. I'll connect the points with curved lines, like this. Your turn. Plot these points and connect them using curved lines.

Let's plot the second figure on the coordinate plane. Using the Coordinate Plane poster, plot the points of transformed Figure 2. Explain while you plot the points using the coordinates, The second figure is placed at $(-10,0),(-7,-6),(-5,-2),(-3,-6)$, and $(0,0)$. I know the first number in a coordinate pair goes on the $x$-axis and the second number goes on the $y$-axis. I'll connect the points in this order with straight lines. Your turn.

## We plotted the points of the transformed

 figures on the coordinate plane, so we can check off $(\checkmark)$ Step 4 of the Task Analysis in your Student Workbook.

## Student Response

Plots the points using coordinates for transformed Figure 2 and then connects the points with curved lines
$\ddagger$ Plots the points with support (using removable circle stickers if needed) and then connects the points (using Wikki Stix if needed)

Plots the points of transformed Figure 2 and then connects the points with straight lines

+     + Plots the points with support (using removable circle stickers if needed) and then connects the points (using Wikki Stix if needed)


## Checks off Step 4

$\ddagger+$ Finds Step 4 on the Task Analysis and checks it off with your help

STEP Identify the transformations on the coordinate plane.
Teacher Instructions
One of the big ideas in this lesson is that: A transformation is a movement of a shape on a plane. Say, The artist performed two transformations in her painting. We must decide which types of transformations she used for each figure.

Using the Coordinate Plane poster, say, Let's look at this coordinate plane. You can look at the coordinate plane in your Student Workbook too.

Figure 1 was placed at $(1,2),(3,2)$, and $(5,2)$. The points are connected with curved lines. The transformed figure's coordinates are ( 5,6 ), ( 7,6 ) and $(9,6)$. What does it look like Maria did?

Help students determine the type of transformation by demonstrating the transformation.
Say, What type of transformation is this?

That's correct. This is a translation. The transformed shape and size are the same as the original shape. The figure just moved diagonally. The $x$-coordinate moved +4 units to the right and the $y$-coordinate moved +4 units up. Every point of the shape moved the same distance in the same direction.

Is this the bird or the mountains?
That's correct. Let's write translation next to the transformed bird.

Student Response

## Responds slid the shape

$\dagger+$ Given 2 Vocabulary cards, chooses slide or signs slide

## Responds translation

Given 2 Vocabulary cards, chooses translationResponds bird

位es translation next to the transformed bird$\ddagger$ Given 2 Vocabulary cards, chooses the card for translation and places it next to the bird on the coordinate plane

Teacher Instructions
Let's look at Figure 2. Figure 2 was placed at ( $-10,0$ ), ( $-7,6$ ), ( $-5,2$ ), ( $-3,6$ ), and ( 0,0 ). The points are connected with straight lines. The transformed figure's coordinates are ( $-10,0),(-7,-6),(-5,-2),(-3,-6)$, and ( 0,0 ). What does it look like Maria did?

Help students determine the type of transformation by demonstrating the transformation. Say, What type of transformation is this?

That's correct. This transformation is a reflection. The transformed shape and size are the same as the original shape. The figure just flipped to be a reflection. Notice how all the coordinates in the transformed figure had a negative, or inverse, $y$-axis coordinate. This is how we know it is a reflection. Looking at our coordinate plane, you can see that it is a reflection across the $\boldsymbol{x}$-axis.

Is this the bird or the mountains?

That's correct. Let's write reflection next to the mountains.

We have identified the types of transformations and labeled them on the coordinate plane. This is one of our big ideas: A translation slides and a reflection flips. Let's check off ( $\checkmark$ ) Step 5.

## Student Response

Responds she flipped the figure
$\ddagger$ Given 2 Vocabulary cards, chooses the card for flip

## Responds reflection

ㅍ Given 2 Vocabulary cards, chooses the card for reflection

Responds mountains

Writes reflection next to the mountains
$\ddagger+$ Given 2 Vocabulary cards, chooses reflection and places it next to the mountains on the coordinate plane

Checks off Step 5
號 5 on the Task Analysis and checks it off with your help

## State the solution to the math story problem.

Teacher Instructions
Let's look back at the problem to be solved. The question to solve was "What types of transformations did Maria use?" A big idea in this lesson is that: a transformation is a movement of a shape on a plane.

Model stating the solution using the Student Workbook pages projected onto a whiteboard. Say, We just decided that Maria used a translation for the bird and a reflection for the mountains. I will circle translation for the bird and reflection for the mountains in the Student Workbook. Your turn.

This is one of our big ideas: A translation slides and a reflection flips.
I will now be able to check off ( $\checkmark$ ) Step 6. You can do the same.

## ${ }_{7}^{\operatorname{TIEP}}$ (1) Fill in the big ideas.

Say, Now, let's review the big ideas we learned. Let's think about this together.
We learned that: $\boldsymbol{A}$ transformation is a movement of a shape on a plane. We also learned about two types of transformations that involve movement of the shape: translation and reflection.
A translation slides and a reflection flips.
Let's fill in both big ideas in your Student Workbook.

## Teacher Instructions

Student Response

Circles translation for the bird and reflection for the mountains in the Student Workbook
$\mp+$ Circles or marks translation for the bird and reflection for the mountains in the Student Workbook

## Checks off Step 6

$\ddagger$ Finds Step 6 on the Task Analysis and checks it off with your help
-


## Teacher Instructions

Let's read them together.

## Student Response

Reads the big ideas with you
$\stackrel{+}{\square}$ Points to the words as you read
Checks off Step 7
$\ddagger$ Finds Step 7 on the Task Analysis and checks it off with your help

## REPEAT THE LESSON

Repeat this lesson as needed (many times, repeating for a week is helpful to students) until students are fairly consistent in following your model to complete the steps of the Task Analysis. Remember that you can print additional pages of the Student Workbook from the digital file. Change elements of the story problem as appropriate to give students additional practice.

## LESSON 2

## CHALLENGE PROBLEM

To add challenge to the lesson, print this Challenge Problem and a blank Coordinate Plane Graphic Organizer (Appendix B) from the digital file. Distribute to students who are ready for a challenge.

Remind students that there are two rules for performing translations and reflections.

- For translations, each point of the shape is moved the same distance (or number of units) in the same direction.
- For triangles that are reflections and that cross a vertical line of symmetry, two points on the vertical line of symmetry will stay the same, but the third point changes. The same applies for reflections across a horizontal line of symmetry. The lengths of the sides of the triangle do not change, so the point will be the same distance on the reflected side of the figure after the reflection.

Read the story aloud to students before they begin to solve the problem.
Nick is an artist who is drawing a new lake picture with two sailboats in the lake. He wants them to be a distance apart and of equal size. He uses what he knows about geometry to make the drawing work. He uses triangles on a coordinate plane as the sailboats. He places the first sailboat - triangle ABC - at the coordinates ( $-6,2$ ), ( $-2,2$ ), and ( $-4,6$ ). Nick performs a translation of +8 units right, -6 units down to paint the second sailboat - triangle DEF. Nick also wants each sailboat to have a reflection in the water across a line of symmetry. The line of symmetry is the base of the triangle.

What are the coordinates for the second sailboat's position in the water? Also find the coordinates for the reflections of both boats.

## Answer:

> Sailboat DEF translated coordinates are (2, -4), (6, -4), and (4, 0). Sailboat ABC's reflection is $(-6,2),(-2,2)$, and ( $-4,-2$ ).
> Sailboat DEF's reflection is $(2,-4),(6,-4)$, and ( $4,-8$ ).

The coordinate points on the line of symmetry (the base of the triangle) remain constant, but the coordinate point that is reflected across the line of symmetry changes to +8 units, which allows the length of the sides to remain the same.


LESSON 2

LESSON ANSWERKEY



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