# GRADE 7

# Mathematics



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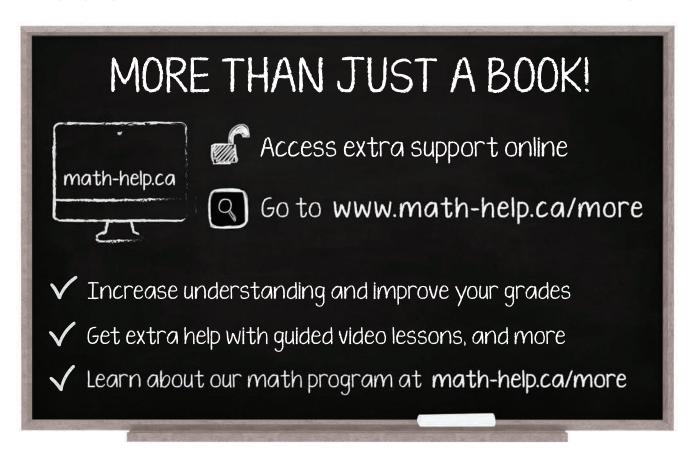
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Dear Teachers,

Dynamic Math is a company founded by teachers, and so we understand just how difficult your job can be.

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| 110011811       |   |     |

There are several skills that are important when working in mathematics. If you use these skills when you work on math questions, it will help you to think about how to get to the answers.

#### These skills are:

#### 1. Communicating

Communicating is the process of expressing mathematical ideas and your understanding of them orally, visually, and in writing. To communicate, you use numbers, symbols, pictures, graphs, diagrams, and words to show that you know what is being said or asked. You are expected to be able to express, describe, explain, and apply mathematical ideas in several different ways.

#### 2. Representing

Representing involves different ways of showing mathematical ideas. To represent, you use drawings, physical models, equations, charts, and graphs to help make things clearer so that you can answer the question.

#### 3. Connecting

Connecting involves relating mathematical concepts to each other. You should also be able to connect mathematical ideas to the real world.

#### 4. Reasoning

Reasoning involves understanding the relationships that apply to numbers, shapes, or operations. Reasoning could be considered to be organized thinking.

Unit 9 gives more details about each of these skills and gives you examples and questions to help you build your skills in these areas.

# UNIT 1 OPERATIONS WITH DECIMALS AND PERCENT

- 1.1 Prime and Composite Numbers
- 1.2 Divisibility of Numbers
- 1.3 Addition and Subtraction of Decimals
- 1.4 Multiplication of Decimals
- 1.5 Division of Decimals
- 1.6 Percent

If you need additional help, there are more resources available at math-help.ca/more.

#### 1.1 Prime and Composite Numbers

A **prime number** is an integer greater than 1 that has no other positive integer factors other than 1 and itself.

Examples: 2, 3, 5, and 7 are prime numbers since their only factors are 1 and themselves (For

example, the only factors of 3 are 1 and 3). However, 6 is <u>not</u> prime since it has two

different sets of integer factors: 1 and 6 or 2 and 3.

A **factor** of a number is a <u>divisor</u> of that number (it divides evenly into it)

Examples:

(i) List all factors of 10

- 1, 2, 5, and 10 are all factors of 10 since they all divide evenly into 10.
- Of these factors, only 2 and 5 are prime factors.
- (ii) Show the following numbers as <u>products</u> of <u>prime</u> factors
- $\blacksquare 12 = 2 \times 2 \times 3$

A **multiple** of a number is the product of that number times another whole number greater than 0.

Example: Multiples of 5 are  $(5 \times 1) = 5$ ;  $(5 \times 2) = 10$ ;  $(5 \times 3) = 15$ ;  $(5 \times 4) = 20$ ; etc.

A **composite number** is not a prime number and can be factored in more than one way. All numbers that are not prime are composite (with the exception of 1).

Example: 15 is a composite number since it can be factored as  $15 \times 1$  or  $5 \times 3$ .

#### **Examples with Solutions**

1. Which of the following numbers are <u>not</u> prime?

1, 3, 4, 5, 7, 9, 11, 15

1 is not prime since it is not greater than 1.

4, 9, and 15 are not prime. They are composite, since they have more than one pair of factors.

For example, 9 can be factored as  $9 \times 1$  or  $3 \times 3$ .

2. List all factors of 20.

Factor 20 as follows  $2 \times 2 \times 5$ 

The set of all factors consists of all numbers that

divide evenly into 20.

The numbers are 1 plus all combinations of 2, 2,

and 5 shown in step 1.

Answer: 1, 2, 4, 5, 10, 20

3. List all multiples of 7 less than 40.

Multiples of 7 consist of numbers that are the

product of 7 times 1, 2, 3, 4, ..., etc.

We want multiples of 7 less than 40.

 $7 \times 1, 7 \times 2, 7 \times 3, 7 \times 4, 7 \times 5.$  (7 × 6 is 42,

which is larger than 40.)

Answer: 7, 14, 21, 28, 35

4. Show 90 as a product of <u>prime</u> factors.

Factor 90 until all factors are broken down into

prime factors.

 $90 = 9 \times 10 = 3 \times 3 \times 2 \times 5$ 

#### **Exercises 1.1**

1. Identify whether or not each number is prime. Then give a reason for it.

| <u>Number</u> | Yes/No | Reason |
|---------------|--------|--------|
| a. 22         |        |        |
| b. 31         |        |        |
| c. 77         |        |        |
| d. 57         |        |        |
| e. 43         |        |        |
| f. 51         |        |        |
|               |        |        |

2. List all factors of each number. Then list the prime factors only.

| <u>Number</u> | All Factors | Prime Factors Only |
|---------------|-------------|--------------------|
| a. 30         |             |                    |
| b. 100        |             |                    |
| c. 75         |             |                    |
| d. 90         |             |                    |
| e. 135        |             |                    |
| f. 38         |             |                    |
|               |             |                    |

3. List all multiples of the following numbers that meet each condition.

| <u>Number</u>   | Multiples of the Number |
|---|-------------------------|
| a. all multiples of 11 that are greater than 40 and less than 100 |                         |
| b. all multiples of 5 between 11 and 41                           |                         |
| c. all multiples of 9 less than 100                               |                         |
| d. all multiples of 20 less than 200                              |                         |
| e. all multiples of 13 less than 100 that are odd numbers.        |                         |

4. Write each number as a product of prime factors.

| Number | Product of Primes | Number  | Product of Primes |
|--------|-------------------|---------|-------------------|
| a. 30  |                   | f. 1000 |                   |
| b. 12  |                   | g. 90   |                   |
| c. 26  |                   | h. 216  |                   |
| d. 36  |                   | i. 196  |                   |
| e. 250 |                   | j. 242  |                   |

#### Extra for Experts

- 5. List all factors which are <u>common</u> to both 9 and 30.
- 6. List all factors which are <u>common</u> to 10, 14, and 70.
- 7. List all numbers less than 100 that are multiples of <u>both</u> 15 and 10.
- 8. List all numbers less than 50 that are multiples of both 3 and 5.
- 9. I am a multiple of both 9 and 15. I am less than 200 and more than 150. Who am I?

- 10. I am a multiple of 3, 5, and 10. I am less than 100. Who am I?
- 11. I am a multiple of 3, 5, and 7 and am between 300 and 400. Who am I?
- 12. I am a number less than 50. If I am a multiple of both 2 and 14, who am I?

# ABORIGINAL APPLICATIONS THE EAGLE







Eagle and Salmon
BT Collection

The Eagle is a powerful symbol of courage and strength. Since it soars so high, Aboriginal people felt it was closest to the creator. It sees and hears all and its feathers are powerful tools for healing used in various ceremonies. To receive a gift of an eagle feather is considered a great honour. It represents stability, strength, and commitment.

A gift of an Eagle Feather is a great honor. It is a mark of distinction, one that could indicate that a rite of passage has been earned. The Eagle Feather represents the norms, responsibilities and behaviors that are all a part of the conditioning, learning and commitment to a spirit. In this way life is honored and becomes whole.

#### **Math Applications**

- 1. On its annual journey, from the north to the southern areas of British Columbia in pursuit of spawning salmon, an eagle travelled the following distances each day: 230.4, 125.6, 100.1, and 95.7 kilometres. How many kilometres in total did it travel?
- 2. Another eagle travelled a distance of 422.4 km on its annual journey. It took three days to complete the journey. If it travelled 111.2 km on the first day and 144.6 km on the second day, how far did it travel on the third day?

#### **Answers**

- 1. 230.4 + 125.6 + 100.1 + 95.7 = 551.8The eagle travelled 551.8 km on the 4-day trip.
- 2. 422.4 (111.2 + 144.6) = 166.6The eagle travelled 166.6 km on the third day.

# **ANSWERS TO**

# **EXERCISES AND**

# **UNIT TESTS**

#### **UNIT 1 ANSWERS**

#### Exercises 1.1 (page 3)

**1. a)** No; Factors are 1, 2, 11, and 22. **b)** Yes; Only factors are 1 and 31. c) No; Factors are 1, 77, 7, and 11. **d)** No; Factors are 1, 57, 3 and 19. e) Yes; Only factors are 1 and 43. f) No; Factors are 1, 51, 3 and 17.

| 2. | All factors               | Prime factors |
|----|---------------------------|---------------|
| a) | 1, 2, 3, 5, 6, 10, 15, 30 | 2, 3, 5       |
| b) | 1, 2, 4, 5, 10, 20, 25,   | 2, 5          |
|    | 50, 100                   |               |
| c) | 1, 3, 5, 15, 25, 75       | 3, 5          |
| d) | 1, 2, 3, 5, 6, 9, 10, 15, | 2, 3, 5       |
|    | 30, 18, 45, 90            |               |
| e) | 1,3,5,9,15,27,45,135      | 3,5           |
| f) | 1,2,19,38                 | 2,19          |

**3.** a) 44, 55, 66, 77, 88, 99 b) 15, 20, 25, 30, 35, 40 **c)** 9, 18, 27, 36, 45, 54, 63, 72, 81, 90, 99 **d)** 20, 40, 60, 80, 100, 120, 140, 160, 180 e) 13, 39, 65, 91 **4.** a)  $2 \times 3 \times 5$  b)  $2 \times 2 \times 3$ c)  $2 \times 13$  d)  $2 \times 2 \times 3 \times 3$  e)  $2 \times 5 \times 5 \times 5$ f)  $2 \times 2 \times 2 \times 5 \times 5 \times 5$  g)  $3 \times 3 \times 2 \times 5$ h)  $2 \times 2 \times 2 \times 3 \times 3 \times 3$  i)  $2 \times 2 \times 7 \times 7$ **j)**  $2 \times 11 \times 11$  **5.** 1, 3 **6.** 1, 2 **7.** 30, 60, 90 **8.** 15, 30, 45 **9.** 180 **10.** 30, 60, 90 **11.** 315 **12.** 14, 28, 42

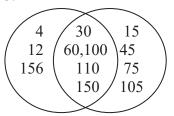
#### Exercises 1.2 (page 12)

**1.** 44, 112, 1012, 3700 **2**. 15, 35, 60, 205, 1080 **3.** 44, 320, 244 **4.** 33, 72, 135, 513 **5.** 50, 750, 2130 **6.** True **7.** False **8.** True **9.** True **10.** False **11.** 231, 234, 237, 240 **12.** 115, 120, 125, 130, 135, 140, 145, 150 **13.** 102, 108, 114

14.

| 17.          |               |               |
|--------------|---------------|---------------|
|              | Yes           | No            |
| Divisible by | 129, 612,     | 712, 908,     |
| 3            | 642, 705, 828 | 1016          |
| Divisible by | 612, 712,     | 129, 642, 705 |
| 4            | 828, 908,     |               |
|              | 1016          |               |
| Divisible by | 612, 828      |               |
| both 3 and 4 |               |               |

15.



**16.** 12, 24, 36, 48 **17.** 30, 60, 90, 120 **18.** 5 or 0 **19.** 4 **20.** 2, 5, 8 **21.** 6 **22.** 0, 5

#### Exercises 1.3 (page 19)

**1. a)** 162 **b)** 376 **c)** 227 **d)** 4053 **2. a)** 23, greater than **b)** 87, less than c) 2984, greater than d) 27, less than **3.** a) 31.3 b) 233.3 c) 3102.82 d) 2829.05 e) 124.7 f) 259.33 g) 14.8 h) 269.33 i) 41.03 j) 9042.15 k) 453.01 l) 71.871 **4.** a) 19.1 b) 129.01 c) 2084.92 d) 3225.013 e) 1144.1 f) 1097.944 g) 41.15 h) 427.43 i) 34.36 j) 2.91 k) 95.24 l) 2784.92 **5.** \$66.50 **6.** 4.8 m **7.** \$40.25 **8.** \$70.95 **9.** 401.9 km **10.** 222.31 kg **11.** \$113.82 **12.** 6.73 m **13.** 4.1 m **14.** \$18.36 **15.** a) 7 **b)** 3 **16.** 80.4 and 65.2

#### Exercises 1.4 (page 24)

**1.** a) 945 b) 200 c) 1000 d) 2210 **2.** a) 187.5 b) 100.8 c) 3662.64 d) 24 828 **3.** a) 84.9 b) 173.02 c) 116.61 d) 100.232 e) 130.231 f) 1126.5 g) 42.813 h) 16 412.3 i) 21.606 j) 100.835 k) 260.48 l) 16.443 **4.** 301 km **5.** 21.4 m **6.** \$6.45 **7.** \$43.75 **8.** 18.24 kg **9.** 12.1 kg **10.** 102.6 kg **11.** 2.5 **12.** \$8.50 **13.** 650 g **14.** \$2.70 **15.** \$16.70

#### Exercises 1.5 (page 28)

**1.** a) 7 b) 11 c) 13 d) 3 **2.** a) 21.5 b) 52 c) 3.6 d) 5.6 e) 2.5 f) 4.2 g) 5.6 h) 74 i) 70.4 j) 24.5 k) 55.5 l) 80.2 **3.** 2.225 **4.** 334.156 25 **5.** 140.3 g **6.** 40 **7.** 27.3 cm **8.** \$10.50 **9.** 0.625 kg **10.** 8 L **11.** 38.79 kg **12.** \$53.15 **13.** \$29.75 **14.** 6 and 7 **15.** 19 **16.** 5.6 **17.** 2.3

Exercises 1.6a (page 33) 1. a)  $\frac{16}{100}$  b)  $\frac{37}{100}$  c)  $\frac{4}{100}$  d)  $\frac{98}{100}$  e)  $\frac{3}{100}$ 



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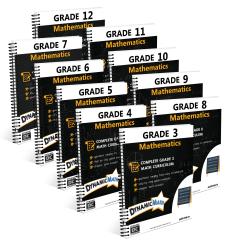
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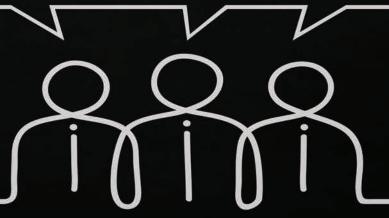


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