



Introduction To Algebra

Basic Practice

1. Simplify the following.

(a) $(2w)^2$

(c) $3q^2 \times 5q$

(e) $12x^2 \div 4$

(g) $21w^2 \div 7w^2$

(b) $3p \times 4p$

(d) $2r \times (4r)^2$

(f) $24y^3 \div 2y$

(h) $18z^2 \div (3z)^2$

2. Simplify the following.

(a) $2x \times 3y$

(c) $6x \div 2y \times 3w$

(e) $p \times 5q - 2 \times 3r$

(g) $(3p)^2 + 5q \times 2r$

(b) $18y \div 3x$

(d) $8y \times 3y \div 2x$

(f) $3x + 8y \div 2z$

(h) $(5b)^2 - 3c \times 2d$

3. When $x = 3$ and $y = 5$, evaluate the following expressions.

(a) $4x - 5y$

(c) $3y^2 + (2x)^2$

(e) $\frac{x}{y}$

(g) $\frac{x+y}{x-y}$

(b) $8y + 2x$

(d) $2y^3 - (2x)^3$

(f) $\frac{4x}{y^2}$

(h) $\frac{x^2 + y^2}{(x-y)^3}$

4. When $x = -2$, $y = -5$, and $z = 3$, evaluate the following expressions.

(a) $2.5x - 3y + 4z$

(c) $3xy - yz$

(e) $x^2 + y^2 + z^2$

(g) $x^3 + y^3 + z^3$

(b) $3x + \frac{2z}{y}$

(d) $2y \times (z^2 - xy)$

(f) $\frac{2x^3}{(z+y)^2}$

(h) $-3x^3 - y^3 + \frac{1}{9}z^3$

5. Find the value of

(a) $\sqrt[3]{\frac{2p}{q}}$ when $p = 16$ and $q = \frac{1}{2}$,

(b) $p(R^2 - r^2)$ when $p = \frac{22}{7}$, $R = 25$, and $r = 24$,

(c) kx^t when $k = 5$, $x = 7$, and $t = 2$,

(d) $(kx + 2y)^z$ when $k = 3.5$, $x = 4$, $y = -5$, and $z = 3$,

(e) $\frac{k}{(\sqrt{x})^3}$ when $k = 3$ and $x = \frac{1}{4}$,

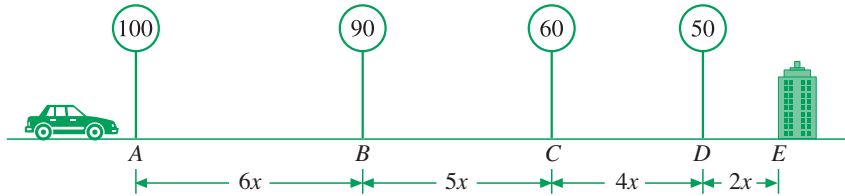
(f) $\sqrt{\frac{1}{a} + \frac{1}{b} + \frac{1}{c}}$ when $a = \frac{1}{21}$, $b = -\frac{1}{5}$, and $c = \frac{1}{9}$.

Further Practice

- 11. (a)** Find the sum of
- (i) $8x + 15y$ and $6x - 10y$,
 (ii) $7a - 3b$, $-4a + 9b$, and $-9a - 10b$,
 (iii) $2(4p - 5q)$ and $3(-4q + 3p)$,
 (iv) $\frac{1}{4}$ of $(8x - 12y)$ and $\frac{3}{2}$ of $(4x + 10y)$.
- (b)** Subtract
- (i) $4s + 9t$ from $3s - t$,
 (ii) $8r - 5w$ from $7w + 12r$,
 (iii) $-\frac{2}{3}(3x + 9y)$ from $\frac{1}{2}(8x + 14y)$.
- (c)** Subtract $7m - 8n$ from the sum of $7n - 8m$ and $20m - 9n$.
- 12.** Simplify each of the following.
- (a) $(3m - 7) + 2(4m - 5n) - 3(1 - 2n)$
 (b) $(3a + 5b - 7) + (4a - 6b + 5)$
 (c) $(4p - 7q - 9) - (p + 5 + 3q)$
 (d) $\left(-\frac{1}{2}x + \frac{2}{3}y - \frac{3}{4}\right) - \left(\frac{3}{2}x - \frac{7}{3}y + \frac{1}{4}\right)$
 (e) $5(x + 4y - 1) + 4(-4x + 6y - 2)$
 (f) $-5(3p - 2q - 8) - 4(-10 + 3p - q)$
 (g) $3\left(\frac{1}{6}a + \frac{1}{4}b - 2\right) + 4\left(\frac{5}{8}a + \frac{9}{16}b - 1\right)$
 (h) $\frac{8}{5}\left(\frac{5}{2}s - \frac{3}{4}t - \frac{5}{8}\right) - \frac{2}{3}\left(12s + \frac{6}{5}t - 3\right)$
- 13.** Simplify each of the following.
- (a) $4[-2a + 4 - 2(a + 3)]$
 (b) $6w - 5 + 3[(4 - 3w) - 2(w - 8)]$
 (c) $4 - 7c - 2[(c + 4) + 2(2c - 5)]$
 (d) $2s + 9 - 3(s - 5) - 2[3(3 - s) + 2(4 - 3s)]$
 (e) $3[5 - 3w - 5(2w + 1)]$
 (f) $-y + 3x + 2[3x - y + 2(y - 2x)]$
 (g) $4(3p + 7q) - 5[4p - (q + 4p) + 5q]$
 (h) $-21m + 8n - 3[2(m - 2n) - 3(3m - 2n)]$
- 14. (a)** (i) Simplify the expression $3a + 9 - 5a - 6$.
 (ii) Hence, find the value of the expression when $a = 2.5$.
- (b)** (i) Simplify the expression $2(4b - 7c) - 3(2c - 3b)$.
 (ii) Hence, find the value of the expression when $b = -6$ and $c = \frac{1}{2}$.
- (c)** (i) Simplify the expression $\frac{x}{3}(6y - 9) - \frac{x}{2}(8y - 6)$.
 (ii) Hence, find the value of the expression when $x = 5$ and $y = -3$.
- (d)** (i) Simplify the expression $\frac{3}{5}p - \frac{1}{4}q + \frac{3}{10}(2p - q)$.
 (ii) Hence, find the value of the expression when $p = 15$ and $q = -10$.
- (e)** (i) Simplify the expression $40 - z - 3[2(4 + 3z) - 3(3z - 1)]$.
 (ii) Hence, find the value of the expression when $z = 4$.
- 15.** Express each of the following in its simplest form.
- (a) $\frac{2x + 1}{3} + \frac{x - 3}{4}$
 (b) $\frac{4y - 3}{3} - \frac{y - 5}{2}$
 (c) $\frac{4z + 2}{4} + \frac{1 - 5z}{5}$
 (d) $\frac{3(2 - 3w)}{2} + \frac{6(4w - 3)}{5}$
 (e) $\frac{3(4p + 5)}{5} - \frac{2(3p + 1)}{3}$
 (f) $\frac{q + 5}{2} + \frac{2q + 7}{5} - 1$
 (g) $\frac{2(2p - q)}{3} - \frac{3(q + 4p)}{2} + \frac{1}{4}$
 (h) $12\left(\frac{m + 2m}{3} - \frac{m - 3n}{6} - \frac{m + n}{2}\right)$

Enrichment

26.



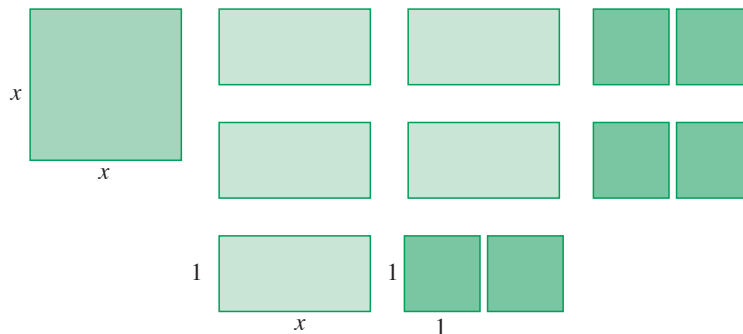
In the figure, $ABCDE$ is a portion of a road from the exit A of an expressway to a building E . $AB = 6x$ km, $BC = 5x$ km, $CD = 4x$ km, and $DE = 2x$ km. A car drives at the speed limits, i.e., 100 km/hr, 90 km/hr, 60 km/hr, and 50 km/hr in each section from A to E respectively. Let T minutes be the time taken by the car to reach E from A .

- (a) Express T in terms of x .
- (b) When $x = 0.45$, find the value of T .

27. The sides of $\triangle ABC$ are $AB = (3x + 4)$ cm, $BC = (4x - 5)$ cm, and $CA = (x + 13)$ cm.

- (a) Express the perimeter of $\triangle ABC$ in terms of x . Give the answer in factored form.
- (b) A square $PQRS$ has the same perimeter as $\triangle ABC$. Express the length of PQ in terms of x .
- (c) When $x = 7$, find
 - (i) the perimeter of $\triangle ABC$,
 - (ii) the area of $PQRS$.

28.



- (a) The figure shows 1 square tile of x by x units, 5 rectangular tiles of x by 1 unit, and 6 square tiles of 1 by 1 unit. Arrange the tiles to form a rectangle and state its dimensions.
- (b) Hence, or otherwise, express $x^2 + 5x + 6$ in the form $(x + a)(x + b)$, where a and b are integers.
- (c) Express $x^2 + 8x + 15$ in the form $(x + p)(x + q)$, where p and q are integers.

29. The volumes of two glasses of water are $(7ax - 3bx + 6ay - 4by)$ cm^3 and $(11bx + 5ax - 6by - 21ay)$ cm^3 respectively. Let V cm^3 be the total volume of water in the two glasses.

- (a) Express V in terms of a , b , x , and y in factored form.
- (b) If both x and y are doubled, determine whether V will be doubled.

Challenging Practice

24. The following table shows Kenneth's results in 4 tests.

Test Number	Score	Maximum Possible Score
1	6.5	10
2	12	20
3	19	25
4	28	40

- (a) In which test was Kenneth's performance the best? Explain your answer.
- (b) For each test, grade 'A' is given if the score is more than or equal to 70% of the maximum possible score. Find, as a percentage, the number of times Kenneth was given grade 'A'.
- (c) Suppose that 67.5% of the students in Kenneth's class were given grade 'A' at least once in the 4 tests. Find the number of students who were not given grade 'A' in any of the tests if there are 40 students in the class.
25. (a) A fruit crate contains a mix of 80 apples and oranges. If 21.25% of the fruits are rotten, find the number of rotten fruits.
- (b) Suppose that 30% of the apples and $\frac{1}{5}$ of the oranges are rotten. Find the number of
- rotten apples,
 - rotten oranges.
- (c) Hence, express the number of apples as a percentage of
- the number of fruits,
 - the number of oranges.
26. Eligible clients of a bank are offered 2 repayment schemes for a one-year loan.
- Scheme A: Pay \$50 and 105% of the loan at the end of the one-year period
- Scheme B: Pay 103% of the sum of \$200 and the loan at the end of the one-year period
- (a) (i) Which is a better scheme for Mr. Martin to use if he is eligible for the loan and wants to borrow \$10,000?
- (ii) How much will he save if he selects the better scheme?
- (b) Mr. Carter, another eligible client, also borrowed from the bank. Find his loan amount if his payment by either of the schemes is the same.
27. (a) If X is 25% less than Y , by how many percent is Y more than X ?
- (b) If X is 25% more than Y , by how many percent is Y less than X ?
- (c) If X is decreased by 10% and then increased by 10%, find the percentage change in X .
- (d) If Y is increased by 10% and then decreased by 10%, find the percentage change in Y .