MATHEMATICS AND STATISTICS 1.4

Internally assessed 3 credits

Achievement Standard 91029
Apply linear algebra in solving problems

Fred's fishy forecast

Fred's Fish Company needs to use a local courier van company to deliver fresh fish to restaurants and shops in the Auckland region. Fred sells fish to locations in Central Auckland, the North Shore and West Auckland:

- 50% of customers are in Central Auckland, which involves distances of up to 5 km
- 30% of customers are on the North Shore which involves distances from 5–15 km
- 20% of customers are in West Auckland which involves distances from 15–30 km.

Fred is considering three reputable local companies which have refrigerated vans available for food deliveries: FastCool, QuickChill and GoCold.



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Each company has a different price structure according to its pick-up charge and the distances that the goods need to be transported.

- FastCool charges \$20 to pick up the goods plus \$1.80 per kilometre.
- QuickChill charges according to the formula C = 1.25d + 30, where d is the distance in kilometres and C is the cost in dollars.
- GoCold charges as shown on the graph below. A distance of 30 km costs \$97.

Van charges 100 90 80 GoCold 70 60 Charge (\$) 50 40 30 20 10 20 6 10 12 14 16 18 22 24 26 Distance (km)

Your task is to analyse and compare the costs of the three companies so that Fred can make the best decision about which company to choose to make deliveries for his business.

Achievement Standard 91029 (Mathematics and Statistics 1.4) Unline practice assessment task

Fred's fishy forecast solution

Answers will vary, examples are shown.

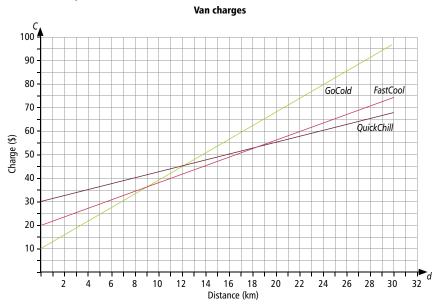
FastCool: has a line with gradient 1.8 (or $\frac{9}{5}$) and vertical intercept 20, so its equation is:

$$C = 1.8d + 20 \text{ or } C = \frac{9}{5}d + 20$$

QuickChill: the formula C = 1.25d + 30 shows that the charge per kilometre is \$1.25 and the pick-up charge is \$30.

GoCold: the line has a vertical intercept of 10 which means that the pick-up charge is \$10. The line has a gradient of $\frac{87}{30}$ or 2.9 which means that the charge per kilometre is \$2.90. So the equation of the GoCold line is C = 2.9d + 10

The graph shows the charge lines for the three companies.



Solving simultaneously, the three points of intersection on the graph have coordinates:

(9.09.36.36) - this means that GoCold and FastCool both charge \$36.36 for 9.09 km

(12.12,45.15) - this means that GoCold and QuickChill both charge \$45.15 for 12.12 km

(18.2,52.7) – this means that QuickChill and FastCool both charge \$52.70 for 18.2 km

- GoCold is cheapest for distances up to 9.1 km
- No van company is cheaper than FastCool for distances of 9.1–18.2 km.
- QuickChill is cheapest for distances over 18.2 km.

Only 20% of deliveries are over 15 km, so QuickChill is not a good choice as it is only cheapest for longer distances.

50% of deliveries are for distances under 5 km when GoCold is cheapest. Also GoCold is cheapest for deliveries of up to around 9 km, which could involve up to half of the North Shore deliveries (mean distance of delivery to North Shore is 10 km). So GoCold could be cheapest for 70-75% of Fred's deliveries.

For North Shore deliveries of 9 to 15 km the extra cost of using GoCold instead of FastCool is up to \$6.50 per delivery (a 15 km delivery by GoCold cost \$53.50 compared with \$47 from FastCool).

For every 100 deliveries, 50 go to Central Auckland, 30 go to the North Shore and 20 go to West Auckland. The table below shows the mean charges for the average distance to each area (e.g. distances to the North Shore are from 5 to 15 km which is an average distance of 10 km), plus the weighted average cost for each company, calculated using $(50 \times CA + 30 \times NS + 20 \times WA) \div 100$, where CA is the mean cost of a delivery to Central Auckland, etc.

Average charge				
	Central Auckland 2.5 km	North Shore 10 km	West Auckland 22.5 km	Weighted average cost
GoCold	\$17.25	\$39	\$75.25	\$35.38
FastCool	\$24.50	\$38	\$60.50	\$35.75
QuickChill	\$33.13	\$42.50	\$58.13	\$40.94

This also puts GoCold as the cheapest on average.

If GoCold could be persuaded to have no pick-up fee for longer trips to West Auckland, and/or to reduce its charge per kilometre, then GoCold would be a clearer winner for Fred.