CHAPTER-1 **REAL NUMBERS**

Fundamental Theorem of Arithmetic

Topic-1

<u>Concepts Covered</u> • Fundamental Theorem of Arithmetic: For any two positive integers a and b, We have HCF (a, b) \times LCM (a, b) = a \times b or or LCM(a, b) =

HCF (a, b) = $\frac{u \times b}{LCM(a,b)}$

Revision Notes

The Fundamental Theorem of Arithmetic Every composite number can be expressed as a product of primes and this factorisation is unique, apart from the order in which the prime factors occur. Fundamental theorem of arithmetic is also called **Unique Factorization Theorem.**

Composite number = Product of prime numbers

Or

Any integer greater than 1 can either be a prime **number** or can be written as a unique product of prime numbers. e.g.,

- (i) $2 \times 11 = 22$ is the same as $11 \times 2 = 22$.
- (ii) 6 can be written as 2×3 or 3×2 , where 2 and 3 are prime numbers.
- (iii) 15 can be written as 3×5 or 5×3 , where 3 and 5 are prime numbers.

The prime factorization of a natural number is unique, except to the order of its factors.

e.g., 12 obtained by multiplying the prime numbers 2, 2 and 3 together,

$$12 = 2 \times 2 \times 3$$

it as

 $12 = 2^2 \times 3$

By using Fundamental Theorem of Arithmetic, we should find the HCF and LCM of given numbers (two or more). This method is also called Prime Factorization

Method.

- Prime Factorization Method to find HCF and LCM:
- Find all the prime factors of given numbers. (i)
- (ii) HCF of two or more numbers = Product of the smallest power of each common prime factor, involved in the numbers.
- (iii) LCM of two or more numbers = Product of the greatest power of each prime factor, involved in the numbers.

Fundamental Facts

- (1) The concept of LCM is important to solve problem related to race tracks, traffic light etc.
- (2) In Mathematics problem, we pair two objects against each other, the LCM value is useful in optimizing the quantities of the given objects.

Irrational Numbers 2-DigoT

Concept Covered • Rational & Irrational Numbers.

Revision Notes

We can write

Rational Numbers: A number in the form $\frac{p}{q}$, where *p*

For example: $2, -3, \frac{3}{7}, -\frac{2}{5}$, etc. are rational numbers. Irrational Numbers: A number is called irrational if it cannot be written in the form $\frac{p}{q}$, where *p* and *q* are

and *q* are **co-prime numbers** and $q \neq 0$, is known as rational number.

integers and $q \neq 0$. For example, $\sqrt{2}$, $\sqrt{3}$, $\sqrt{5}$, π .

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- Let p be a prime number. If p divides a², then p divides a, where a is a positive integer.
- The sum or difference of a rational and an irrational number is irrational.
- The product and quotient of a non-zero rational and an irrational number is irrational.

🔁 Fundamental Facts

- The discovery of irrational numbers is usually attributed to Pythagoras, more specifically to the Pythagorean Hippasus of metapontum who produced a proof of the irrationality of √2.
- (2) Irrational numbers are numbers that cannot be expressed as the ratio of two whole numbers.

CHAPTER-2 POLYNOMIALS



Revision Notes

- Polynomial: An algebraic expression in the form of $a_n x^n + a_{n-1} x^{n-1} + \dots + a_2 x^2 + a_1 x + a_0$, (where *n* is a whole number and a_0 , a_1 , a_2 , ..., a_n are real numbers) is called a polynomial in one variable *x* of degree *n*.
- Value of a Polynomial at a given point: If p(x) is a polynomial in x and ' α ' is any real number, then the value obtained by putting $x = \alpha$ in p(x), is called the value of p(x) at $x = \alpha$.
- Zero of a Polynomial: A real number k is said to be a zero of a polynomial p(x), if p(k) = 0.

Geometrically, the zeroes of a polynomial p(x) are precisely the **X**-co-ordinates of the points, where the graph of y = p(x) intersects the X-axis.

- (i) A linear polynomial has one and only one zero.
- (ii) A quadratic polynomial has at most two zeroes.
- (iii) A cubic polynomial has at most three zeroes.
- (iv) In general, a polynomial of degree *n* has at most *n* zeroes.
- Graphs of Different types of Polynomials:
 - **Linear Polynomial:** The **graph** of a linear polynomial p(x) = ax + b is a straight line that intersects X-axis at one point only.
 - **Quadratic Polynomial: (i) Graph** of a quadratic polynomial $p(x) = ax^2 + bx + c$ is a parabola which opens upwards, if a > 0 and intersects X-axis at a maximum of two distinct points.

(ii) Graph of a quadratic polynomial $p(x) = ax^2 + bx + c$ is a parabola which opens downwards, if

a < 0 and intersects X-axis at a maximum of two **distinct** points.

Cubic polynomial: Graph of cubic polynomial $p(x) = ax^3 + bx^2 + cx + d$ intersects X-axis at a maximum of three **distinct** points.

Relationship between the Zeroes and the Coefficients of a Polynomial:

(i) Zero of a linear **polynomial**

$$= \frac{(-1)^1 \text{Constant term}}{\text{Coefficient of } x}$$

If ax + b is a given linear polynomial, then zero of **linear polynomial is** $\frac{-b}{a}$.

(ii) In a quadratic polynomial, Sum of zeroes of a quadratic polynomial

 $= \frac{(-1)^1 \operatorname{Coefficient} \operatorname{of} x}{\operatorname{Coefficient} \operatorname{of} x^2}$

Product of zeroes of a quadratic polynomial

 $= \frac{(-1)^2 \text{ Constant term}}{\text{Coefficient of } x^2}$

If α and β are the zeroes of a quadratic polynomial $ax^2 + bx + c$, then

$$\alpha + \beta = -\frac{b}{a}$$
 and $\alpha\beta = \frac{c}{a}$

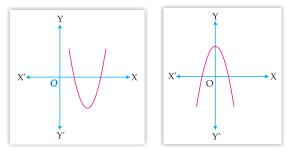
(iii) If α , β and γ are the zeroes of a cubic polynomial $ax^3 + bx^2 + cx + d$, then

$$\alpha + \beta + \gamma = (-1)^1 \frac{b}{a} = -\frac{b}{a}, \ \alpha\beta + \beta\gamma + \gamma\alpha$$

$$= (-1)^2 \frac{c}{a} = \frac{c}{a} \text{ and } \alpha \beta \gamma$$
$$= (-1)^3 \frac{d}{a} = -\frac{d}{a}$$

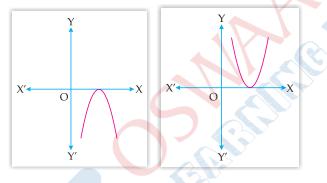
Discriminant of a Quadratic Polynomial: For $f(x) = ax^2 + bx + c$, where $a \neq 0$, $b^2 - 4ac$ is called its discriminant D. The discriminant D determines the nature of roots/zeroes of a quadratic polynomial.

Case I: If **D** > 0, graph of $f(x) = ax^2 + bx + c$ will intersect the **X**-axis at two distinct points, *x*-coordinates of points of intersection with **X**-axis are known as 'zeroes' of f(x).



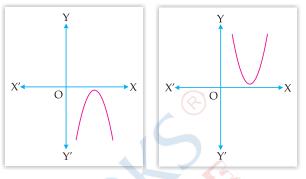
 \therefore *f*(*x*) will have two zeroes and we can say that roots/ zeroes of the two given polynomials are real and unequal.

Case II: If $\mathbf{D} = 0$, graph of $f(x) = ax^2 + bx + c$ will touch the **X**-axis at one point only.



 \therefore *f*(*x*) will have only one 'zero' and we can say that roots/zeroes of the given polynomial are real and equal.

Case III: If D < 0, graph of $f(x) = ax^2 + bx + c$ will neither touch nor intersect the **X**-axis.



 \therefore f(x) will not have any real zero.

Fundamental Facts

(1) Polynomials are also an essential tool in describing and predicting traffic patterns so appropriate traffic control measures, such as traffic lights, can be implemented.

Mnemonics

Concept: $\alpha.\beta = \frac{c}{c}$

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Mnemonics: Amitabh Bachchan went Canada by aeroplane. **Interpretation:** Amitabh's $A \Rightarrow$ Alpha (α) Bachchan's $B \Rightarrow$ Beta (β) Canada's $C \Rightarrow$ Constant (c)

Canada's
$$C \Rightarrow Cons$$

By for Divide by

Aeroplane's $a \Rightarrow$ Variable (*a*).

CHAPTER-3

PAIR OF LINEAR EQUATIONS IN TWO VARIABLES

Graphical Solution of Linear Equations in two variables

Concepts Covered • To Solve the equations by graphical method. • Possibilities of solutions and consistency/inconsistency. • Conditions of unique solution/infinite number of solutions/ no Solution.

Revision Notes

Topic-1

Linear equation in two variables: An equation in the form of ax + by + c = 0, where *a*, *b* and *c* are real

numbers and a and b are not zero, is called a linear equation in two **variables** x and y.

General form of a pair of linear equations in two **variables** is:

 $a_1x + b_1y + c_1 = 0$

and
$$a_2x + b_2y + c_2 = 0$$

where a_1 , a_2 , b_1 , b_2 , c_1 and c_2 are real numbers, such that

$$a_1, b_1 \neq 0 \text{ and } a_2, b_2 \neq 0.$$

3x - y + 7 = 0,

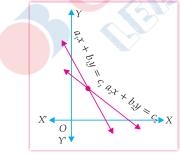
7x + y = 3

e.g.,

are linear equations in two **variables** *x* and *y*.

- There are two methods of solving simultaneous linear equations in two variables:
 - (i) Graphical method, and
 - (ii) Algebraic methods.
 - 1. Graphical Method:
 - (i) Express one variable (say *y*) in terms of the other variable *x*, *y* = *ax* + *b*, for the given equation.
 - (ii) Take at least two values of independent variable x and find the corresponding values of dependent variable y, take integral values only.
 - (iii) Plot these values on the graph paper in order to represent these equations.
 - (iv) **If the lines intersect** at a distinct point, then point of intersection will be the unique solution for given equations. In this case, the pair of linear equations is consistent.
 - If $\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$, then the pair of linear equations is

consistent with a unique solution.

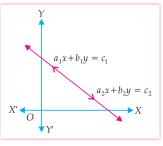


Intersecting Lines

(v) If the lines representing the linear equations coincides, then system of equations has infinitely many **solutions**. In this case, the pair of linear equations is consistent and dependent.

If $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$, then the pair of linear equations

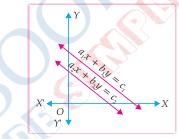
is consistent with infinitely many solutions.



Coincident Lines

- (vi) If the lines representing the pair of linear equations are parallel, then the system of equations has no solution and is called inconsistent.
 - If $\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$, then the pair of linear equations

is inconsistent with no solution.



Parallel Lines

Fundamental Facts

- (1) A linear equation in two variables is represented geometrically by a line whose points make up the collection of solutions of the equation.
- (2) In case of two variables, each solution may be interpreted as the cartesian co-ordinates of a point of the Euclidean plane.

Mnemonics

Concept: Algebraic Method

System has unique solution

$$\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$$

 $\begin{array}{l} \text{Mnemonics: For unique feature Audi A_1}\\ \text{and A_2 are not same as BMW B_1 and B_2} \end{array}$

Interpretation:

$$A_1 \Rightarrow a_1$$
$$A_2 \Rightarrow a_2$$
$$B_1 \Rightarrow b_1$$
$$B_2 \Rightarrow b_2$$

5

Topic-2

Algebraic Methods to Solve Pair of Linear Equations

<u>Concept Covered</u> • Solve the linear equations algebraically by Substitution and Elimination method.

• To Solve word problems.

Revision Notes

 Algebraic Method: We can solve the linear equations algebraically by substitution method and elimination method.

- 1. Substitution Method:
 - (i) Find the value of one variable (say *y*) in terms of the other variable *i.e.*, *x* from either of the equations.
 - (ii) Substitute this value of *y* in other equation and reduce it to an equation in one variable.
 - (iii) Solve the equation so obtained and find the value of *x*.
 - (iv) Put this value of *x* in one of the equations to get the value of variable *y*.

2. Elimination Method:

(i) Multiply given equations with suitable

constants, make either the *x*-coefficients or the *y*-coefficients of the two equations equal.

- (ii) Subtract or add one equation from the other to get an equation in one variable.
- (iii) Solve the equation so obtained to get the value of the variable.
- (iv) Put this value in any one of the equations to get the value of the second variable.

Note:

- (a) If in step (ii), we obtain a true equation involving no variable, then the original pair of equations has infinitely many solutions.
- (b) If in step (ii), we obtain a false equation involving no variable, then the original pair of equations has no solution *i.e.*, it is inconsistent.

Steps to be followed for solving word problems							
S. No.	Problem type	Steps to be followed					
1.	Age Problems	If the problem involves finding out the ages of two persons, take the present age of one person as x and of the other as y . Then, ' a ' years ago, age of 1^{st} person was ' $x - a$ ' years and that of 2^{nd} person was ' $y - a$ ' and after ' b ' years, age of 1^{st} person will be ' $x + b$ ' years and that of 2^{nd} person will be ' $y + b$ ' years. Formulate the equations and then solve them.					
2.	Problems based on Numbers and Digits	Let the digit in unit's place be x and that in ten's place be y . The two-digit number is given by $10y + x$. On interchanging the positions of the digits, the digit in unit's place becomes y and in ten's place becomes x . The two digit number becomes $10x + y$. Formulate the equations and then solve them.					
3.	Problems based on Fractions	Let the numerator of the fraction be x and denominator be y , then the fraction is $\frac{x}{y}$. Formulate the linear equations on the basis of conditions given and solve for x and y to get the value of the fraction.					
4.	Problems based on Distance, Speed and Time	Speed = $\frac{\text{Distance}}{\text{Time}}$ or Distance = Speed × Time and Time = $\frac{\text{Distance}}{\text{Speed}}$. To solve the problems related to speed of boat going downstream and upstream, let the speed of boat in still water be <i>x</i> km/h and speed of stream be <i>y</i> km/h. Then, the speed of boat in downstream = $(x + y)$ km/h and speed of boat in upstream = $(x - y)$ km/h.					

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5.	Problems based on commercial Mathematics	 For solving specific questions based on commercial mathematics, To the fare of 1 full ticket may be taken as ₹ x and the reservation charges may be taken as ₹ y, so that one full fare = x + y and one half fare = x/2 + y.
		 To solve the questions of profit and loss, take the cost price of 1st article as ₹ x and that of 2nd article as ₹ y. To solve the questions based on simple interest, take the amount invested as ₹ x at some rate of interest and ₹ y at some other rate of interest as per given in question.
6.	Problems based on Geometry and Mensuration	 Make use of angle sum property of a triangle (∠A + ∠B + ∠C = 180°, in case of a triangle. In case of a parallelogram, opposite angles are equal and in case of a cyclic quadrilateral, opposite angles are supplementary.

🛃 Fundamental Fact

Algebraic expressions are the mathematical equations consisting of variables, constants, terms and coefficients.

CHAPTER-4 QUADRATIC EQUATIONS



6

Revision Notes

Solutions of Quadratic Equations

- A quadratic equation in variable x is of the form ax² + bx + c = 0, where a, b and c are real numbers and a ≠ 0.
- The values of *x* that satisfy the equation are called the solutions or roots or zeros of the equation.
- A real number α is said to be a solution/root or zero of the quadratic equation ax² + bx + c = 0, if aα² + bα + c = 0.
- A quadratic equation can be solved by the following algebraic methods:
 - (i) By factorization (splitting the middle term),
 - (ii) Making perfect squares and
 - (iii) Using quadratic formula.
- If ax² + bx + c = 0, where a ≠ 0 can be reduced to the product of two linear factors, then the roots of the **quadratic** equation ax² + bx + c = 0 can be found by equating each factor to zero.

- Method for factorization of the equation $ax^2 + bx + c = 0$, where $a \neq 0$.
 - Find the product of *a* and *c i.e.*, "*ac*"
 - Find a pair of numbers b₁ and b₂ whose product is "ac" and whose sum is "b" (if you can't find such number, it can't be factorized).
 - Split the middle term using b_1 and b_2 , that expresses the term bx as $b_1x \pm b_2x$. Now factorize, by grouping the pairs of terms.

Solution of a Quadratic equation using Quadratic formula

The roots of the quadratic equation ax² + bx + c = 0;
 a ≠ 0 can be find using the following formula:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

The above result is known as quadratic formula or Sridharacharya Formula.

Here, $b^2 - 4ac \ge 0$, for real roots.

- The Greek mathematician Euclid developed a geometrical approach for finding out roots, which are solutions of quadratic equations.
- **Brahmagupta** (C.E. 598-665) gave an explicit formula to solve a quadratic equation of the form $ax^2 + bx + c = 0$.
- Sridharacharya (C.E. 1025) derived the quadratic formula for solving a quadratic equation by the method of completing the perfect square.
- Discriminant and Nature of Roots
 - For the quadratic equation ax² + bx + c = 0, the expression b² 4ac is known as discriminant *i.e.*, Discriminant, D = b² 4ac.
- Nature of roots of a quadratic equation:
 - If b² 4ac > 0, the quadratic equation has two distinct real roots.
 - If $b^2 4ac = 0$, the quadratic equation has two equal real roots.
 - If $b^2 4ac < 0$, the quadratic equation has no real root.

🔠 Fundamental Facts

- (1) Quadratic equations are second order polynomials. This means that the highest power of the variable is two.
- (2) An equation of the form of $ax^2 + bx + c = 0$ is called as a quadratic equation. It has two roots. Both of them may be real, equal or imaginary.

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The real roots of ax^2 + bx + c = 0, where a \neq 0 are
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$$\frac{-b+\sqrt{b^2-4ac}}{2a} \text{ and } \frac{-b-\sqrt{b^2-4ac}}{2a} \text{ , where } b^2-4ac > 0.$$

Roots of $ax^2 + bx + c = 0$, where $a \neq 0$ are $\frac{-b}{2a}$ and $\frac{-b}{2a}$

, where $b^2 - 4ac = 0$ Quadratic identities: (i) $(a + b)^2 = a^2 + 2ab + b^2$ (ii) $(a - b)^2 = a^2 - 2ab + b^2$

(iii)
$$a^2 - b^2 = (a + b)(a - b)$$

Mnemonics

Concept: To Find the roots of quadratic equation,

$$-b\pm\sqrt{b^2-4ac}$$

2a

Mnemonics: A negative **B**oy could not decided if he did or didn't want to go to a **Radical** party. The Boy was **Square** so he **missed out** on 4 **A**wesome Chicks.

This was all over by **2 a.m.**

Interpretation:

A negative Boy \Rightarrow (– <i>b</i>)
he did or didn't want to go \Rightarrow (+/-)
to a Radical party \Rightarrow ($$)
Boy was Square \Rightarrow (b^2)
missed out \Rightarrow (–)
4 Awesome \Rightarrow 4 <i>a</i>
Chicks \Rightarrow <i>c</i>
all over \Rightarrow Divided by
2 a.m. $\Rightarrow 2a$

CHAPTER-5

ARITHMETIC PROGRESSIONS

To Find *n*th Term of the Arithmetic Progression

Topic-1

Concepts Covered • First term and common difference of an A.P.
Finite and infinite A.P.
Formula for finding nth term of an A.P.



- An arithmetic progression is a sequence of numbers in which each term is obtained by adding or subtracting a fixed number to the preceding term, except the first term.
- The difference between the two successive terms of an A.P. is called the common difference and is denoted by *d*.
- Each number in the sequence of arithmetic progression is called a term of an A.P.
- The arithmetic progression having finite number of terms is called a finite arithmetic progression.
- The arithmetic progression having infinite number of terms is called an infinite arithmetic progression.
- A list of numbers a_1 , a_2 , a_3 , ..., a_n is an A.P., if the differences $a_2 a_1$, $a_3 a_2$, $a_4 a_3$, ... give the same value *i.e.*, $a_{k+1} a_k$ is same for all different values of *k*.
- The general form of an A.P. is a, a + d, a + 2d, a + 3d,
- If the A.P. a, a + d, a + 2d,..., l is reversed to l, l d, l – 2d, ..., a, the common difference changes to negative of common difference of original sequence.

©=₩ Key Formulae

- The general (nth) term of an A.P. is expressed as:
 - $a_n = a + (n 1)d$ from the starting. where, *a* is the first term and *d* is the common difference.
- The general (n^{th}) term of an A.P. l, l d, l 2d,...., a is given by:

 $a_n = l + (n - 1)(-d) = l - (n - 1)d$ from the end.

where, l is the last term, d is the common difference and n is the number of terms.

Fundamental Facts

- (1) An A.P. or arithmetic sequence is a sequence of numbers such that the difference between the consecutive terms is constant.
- (2) If a constant is added or subtracted from each term of an A.P., the resulting sequence is also an A.P.
- (3) If each term of an A.P. is multiplied or divided by a non-zero constant, the resulting sequence is also an A.P.
- (4) If the terms are selected at a regular interval, the given sequence is in A.P.
- (4) If the terms are selected at a regular interval, the given sequence is in A.P.
- (5) If the terms of sequence are connected with plus (+) or minus (-), the pattern is called a series.
- Example: 2 + 4 + 6 + 8 + is a series.
 (6) If the terms of a sequence or a series are written under specific conditions, then the sequence or series is called a progression.

Mnemonics

Concept: n^{th} Term of Arithmetic Progression n = a + (n - 1)d. **Mnemonics:** Nokia Offers Additional **Programmes in English To Attract Positive New**

One Buyer Daily Interpretation:

*

Nokia 'N' $\Rightarrow n^{th}$ term. Offer 'O' \Rightarrow of Additional 'A' \Rightarrow Arithmetic Programme 'P' \Rightarrow Progression In T' \Rightarrow is. English 'E' \Rightarrow Equal To 'T' \Rightarrow To Attract 'A' $\Rightarrow a$ Positive 'P' \Rightarrow + New 'N' $\Rightarrow n$ One Buyer \Rightarrow -1 Daily 'D' $\Rightarrow d$

Sum of *n* Terms of an Arithmetic Progression

<u>Concepts Covered</u> • Formula to find the sum of n terms of A.P. • Students will be able to recall some patterns which occur in their daily life.

Revision Notes

Sum of *n* terms of an A.P. is given by:

$$S_n = \frac{n}{2} \left[2a + (n-1)d \right]$$

where, a is the first term, d is the common difference and n is the total number of terms.

Sum of *n* terms of an A.P. when first and last term is given.

$$S_n = \frac{n}{2} \ [a+l]$$

where, *a* is the first term and *l* is the last term.

The n^{th} term of an A.P. is the difference of the sum of first *n* terms and the sum to first (n - 1) terms of it. *i.e.*, $a_n = S_n - S_{n-1}$.

🔚 Fundamental Facts

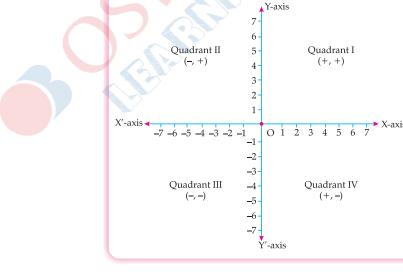
- (1) To find the sum of *n* terms of an A.P., we use a formula first founded by Johann carl friedrich Gauss in the 19th century.
- (2) A.P. can be applied in real life by analysing a certain pattern, for example, A.P. is used in straight line depreciation.

CHAPTER-6 CO-ORDINATE GEOMETRY

Revision Notes

Two perpendicular number lines intersecting at origin are called co-ordinate axes. The horizontal line is the

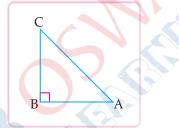
X-axis (denoted by X'OX) and the vertical line is the *Y*-axis (denoted by Y'OY).



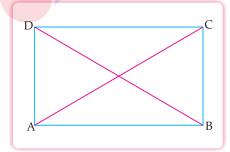
- The point of intersection of X-axis and Y-axis is called origin and denoted by O.
- Cartesian plane is a plane obtained by putting the co-ordinate axes perpendicular to each other in the plane. It is also called co-ordinate plane or XY-plane.
- The X-co-ordinate of a **point** is its perpendicular distance from Y-axis. The Y-co-ordinate of a **point** is its perpendicular distance from X-axis.
- The point where the X-axis and the Y-axis intersect has co-ordinate **point** (0, 0).

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- The abscissa of a point is the X-co-ordinate of the point.
- The ordinate of a point is the Y-co-ordinate of the point.
- If the abscissa of a point is x and the ordinate of the point is y, then (x, y) is called the co-ordinates of the point.
- The axes divide the Cartesian plane into four parts called the quadrants (one fourth part), numbered I, II, III and IV anti-clockwise from OX.
- The co-ordinates of a point on the X-axis are of the form (x, 0) and that of the point on Y-axis are (0, y).
- Sign of co-ordinates depicts the quadrant in which it lies. The co-ordinates of a point are of the form (+, +) in the first quadrant, (-, +) in the second quadrant, (-, -) in the third quadrant and (+, -) in the fourth quadrant.
- Three points A, B and C are collinear if the distances AB, BC and CA are such that the sum of two distances is equal to the third.
- Three points A, B and C are the vertices of an equilateral triangle if AB = BC = CA.
- The points A, B and C are the vertices of an isosceles triangle if AB = BC or BC = CA or CA = AB.
- Three points A, B and C are the vertices of a right triangle, if $AB^2 + BC^2 = CA^2$.

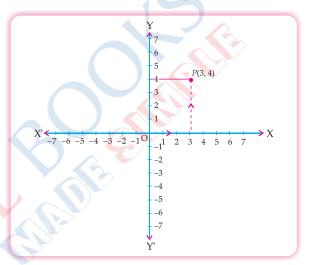


For the given four points A, B, C and D:



- If AB = BC = CD = DA; AC = BD, τηεn ABCD is a square.
- 2. If AB = BC = CD = DA; $AC \neq BD$, $\tau\eta$ en ABCD is a rhombus.
- 3. If AB = CD, BC = DA; AC = BD, $\tau\eta en ABCD$ is a rectangle.

- 4. If AB = CD, BC = DA; $AC \neq BD$, $\tau\eta en ABCD$ is a parallelogram.
- Diagonals of a square, rhombus, rectangle and parallelogram always bisect each other.
- Diagonals of rhombus and square bisect each other at right angle.
- If $x \neq y$, then $(x, y) \neq (y, x)$ and if (x, y) = (y, x), then x = y.
- To plot a point P(3, 4) in the cartesian plane.
 - (i) A distance of 3 units along X-axis.
 - (ii) A distance of 4 units along Y-axis.



©=₩ Key Formulae

The distance between two points i.e., $P(x_1, y_1)$ and $Q(x_2, y_2)$ is

$$d = \left| \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \right|$$

- The distance of a point P(*x*, *y*) from origin is $\left|\sqrt{x^2 + y^2}\right|$
- Co-ordinates of point (x, y) which divides the line segment by joining the points (x_1, y_1) and (x_2, y_2) in the ratio m : n internally are

$$x = \left(\frac{mx_2 + nx_1}{m+n}\right)$$
$$y = \left(\frac{my_2 + ny_1}{m+n}\right)$$

Co-ordinates of mid-point of the line segment by joining the points (x₁, y₁) and (x₂, y₂) are

$$x = \left(\frac{x_2 + x_1}{2}\right)$$
$$y = \left(\frac{y_2 + y_1}{2}\right)$$

and

and

Fundamental Facts

- (1) Co-ordinate geometry is the system of geometry where the position of points on the plane is described using an ordered pair of numbers.
- (2) Co-ordinate geometry acts as a bridge between the Algebra and Geometry.
- (3) Medians of a triangle are concurrent. The point of concurrency is called the centroid.
- (4) Trisection of a line segment means dividing it into 3 equal parts, so 2 points are required.

CHAPTER-7 TRIANGLES

Revision Notes

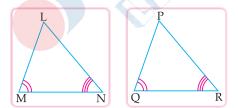
- A triangle is one of the basic shapes of geometry. It is a polygon with 3 sides and 3 vertices/corners.
- Two figures are said to be congruent if they have the same shape and the same size.
- Those figures which have the same shape but not necessarily the same size are called **similar** figures. Hence, we can say that all congruent figures are

similar but all similar figures are not congruent.

- **Similarity of Triangles:** Two triangles are similar, if:
 - (i) their **corresponding** sides are proportional.
 - (ii) their **corresponding** angles are equal.

If \triangle **ABC** and \triangle **DEF** are **similar**, then this similarity can be written as \triangle *ABC* ~ \triangle *DEF*.

Criteria for Similarity of Triangles:



In Δ LMN and Δ PQR, if

(a)
$$\angle L = \angle P, \angle M = \angle Q$$

 $\angle R$

(b)
$$\frac{LM}{PQ} = \frac{MN}{QR} = \frac{LN}{PR}$$

then $\Delta LMN \sim \Delta PQR$.

(i) **AAA-Criterion:** In two triangles, if corresponding angles are equal, then the triangles are similar

and $\angle N =$

and hence their **corresponding** sides are in the same ratio.

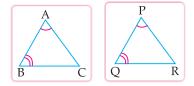


If $\triangle ABC$ and $\triangle DEF$ are similar $\angle A = \angle D, \angle B = \angle E$ and $\angle C = \angle F$. Then, $\frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF}$

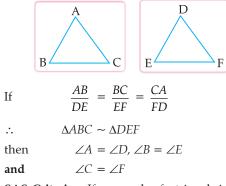
Remark: If two angles of a triangle are respectively equal to the two angles of another triangle, then by the angle sum property of a triangle their third angles will also be equal. Therefore, AAA similarity criterion can also be stated as follows:

AA-Criterion: If two angles of one triangle are respectively equal to two angles of another triangle, then the two triangles are similar.

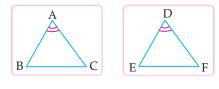
As we know that the sum of all angles in a triangle is 180°, so if two angles in \triangle ABC and \triangle PQR are same *i.e.*, $\angle A = \angle P$, $\angle B = \angle Q$.



(ii) SSS-Criterion: In two triangles if the sides of one triangle are proportional to the sides of another triangle, then the two triangles are similar and hence corresponding angles are equal.



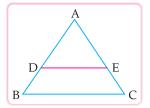
(iii) SAS-Criterion: If one angle of a triangle is equal to one angle of another triangle and the sides including these angles are in the same ratio, then the two triangles are similar.



If $\frac{AB}{DE} = \frac{AC}{DE}$ and $\angle A = \angle D$, then $\triangle ABC \sim \triangle DEE$.

Some theorems based on similarity of triangles

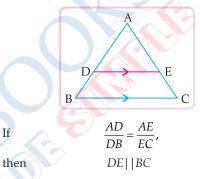
If a line is drawn **parallel** to one side of a triangle (i) to intersect the other two sides at distinct points, the other two sides are divided in the same ratio. It is known as 'Basic Proportionality Theorem' or 'Thales Theorem'.



In $\triangle ABC$, let $DE \mid \mid BC$, then

(a)
$$\frac{AD}{DB} = \frac{AE}{EC}$$
 (b) $\frac{AB}{DB} = \frac{AC}{EC}$ (c) $\frac{AD}{AB} = \frac{AE}{AC}$

(ii) If a line divides any two sides of a triangle in the same ratio, then the line is parallel to the third side. It is the 'Converse of Basic Proportionality Theorem'.



If

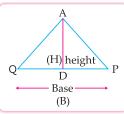
Fundamental Facts

- (1) The use of similar triangles has made possible the measurements of heights and distances.
- (2) Thales of Miletus was the great mathematician who found the similar triangles.

Mnemonics

Concept: Area of triangle = $\frac{1}{2}$ × Base × height

Mnemonics: Audi is the product of half of BMW and Honda Interpretations: $A \Rightarrow Area$ $B \Rightarrow Base$ $H \Rightarrow Height$



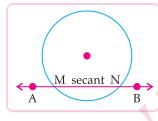
CHAPTER-8 CIRCLES

Concepts Covered

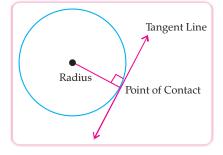
- Tangent to a circle
- Property/theorems of tangents to a circle

Revision Notes

- Circle: A circle is a round shaped figure has no corners or edges.
- Tangent: A tangent to a circle is a line that intersects the circle at one point only.
- The common point of the circle and the tangent is called the point of contact.
- Secant: A line which intersects the circle at two district points is called a secant.

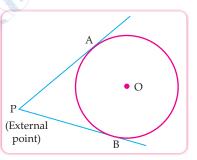


- A tangent to a circle is a special case of the secant when the two end points of the corresponding chord are coincide.
- There is no **tangent** to a circle passing through a point lying inside the circle.
- At any point on the circle there can be one and only one tangent.
- The tangent at any point of a circle is perpendicular to the radius through the point of contact.



- There are exactly two tangents to a circle through a point outside the circle.
- The length of the segment of the tangent from the external point *P* and the point of contact with the circle is called the length of the tangent.
- The lengths of the tangents drawn from an external point to a circle are equal.

In the figure, PA = PB.



Fundamental

- (1) The word 'tangent' comes from the Latin word 'tangere', which means to touch and was introduced by the Danish mathematician Thomas Fincke in 1583.
- (2) The line perpendicular to the tangent and passing through the point of contact, is known as the **normal**.
- (3) In two concentric circles, the chord of the larger circle, which touches the smaller circle, is bisected at the point of contact.

CHAPTER-9

INTRODUCTION TO TRIGONOMETRY AND IDENTITIES

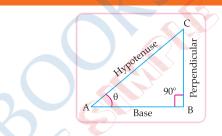
Trigonometric Ratios and Their Values

<u>Concepts Covered</u> • Six trigonometric ratios with their sides of a right angled triangle. • Values of trigonometric ratios between 0° to 90°.

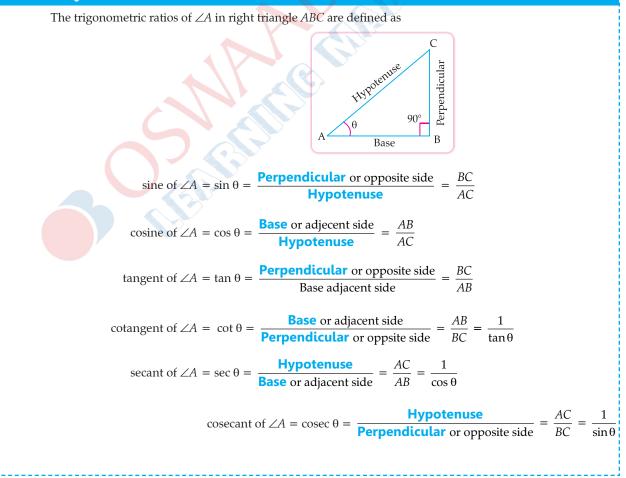
Revision Notes

Topic-1

In fig., a right triangle **ABC** right angled at **B** is given and $\angle BAC = \theta$ is an acute angle. Here side **AB** which is adjacent to $\angle A$ is base, side **BC** opposite to $\angle A$ is perpendicular and the side **AC** is hypotenuse which is opposite to the right angle **B**.



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It is clear from the above ratios that cosecant, secant and cotangent are the reciprocals of sine, cosine and tangent respectively.

Also,	$\tan \theta = \frac{\sin \theta}{\cos \theta}$
and	$\cot \theta = \frac{\cos \theta}{\sin \theta}$

- The trigonometric ratios of an acute angle in a right triangle express the relationship between the angle and length of its sides.
- The value of trigonometric ratio of an angle does not depend on the size of the triangle but depends on the angle only.

ZA	0°	30°	45°	60°	90°
sin A	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	
cos A	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0
tan A	0	$\frac{1}{\sqrt{3}}$		$\sqrt{3}$	Not defined (∞)
cot A	Not defined (∞)	$\sqrt{3}$	1	$\frac{1}{\sqrt{3}}$	0
sec A	1	$\frac{2}{\sqrt{3}}$	$\sqrt{2}$	2	Not defined (∞)
cosec A	Not defined (∞)	2	$\sqrt{2}$	$\frac{2}{\sqrt{3}}$	1

Fundamental Facts

- (1) The three basic functions in trigonometry are sine, cosine and tangent.
- (2) Trigonometry, as the name might suggest, is all about triangles.

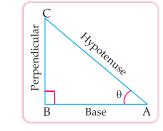
Mnemonics

1. Trigonometric Ratios Mnemonics:

*

In right angled Δ ABC, we have

$$\sin \theta = \frac{BC}{AC}, \cos \theta = \frac{BA}{AC}, \tan \theta = \frac{BC}{AB},$$
$$\cot \theta = \frac{AB}{BC}, \sec \theta = \frac{AC}{BA}, \operatorname{cosec} \theta = \frac{AC}{BC}$$
$$\frac{\operatorname{sin}}{\operatorname{Pandit}} \begin{array}{c} \cos \varphi & \operatorname{tan} \varphi \\ \end{array}$$



Interpretation:

$$\sin \theta = \frac{\mathbf{Pandit}}{\mathbf{Har}} = \frac{P}{H} = \frac{\text{Perpendicular}}{\text{Hypotenuse}} = \frac{BC}{AC}$$

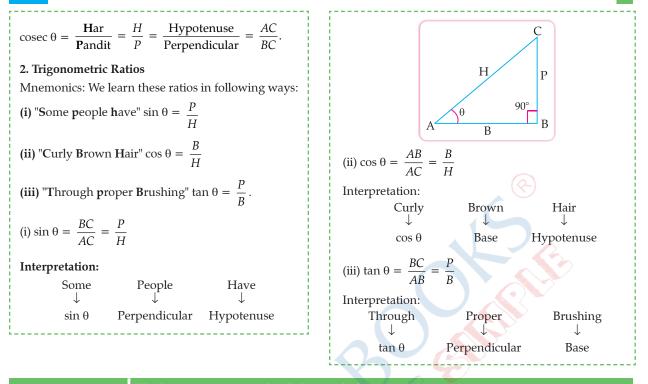
$$\cos \theta = \frac{\mathbf{Badri}}{\mathbf{Har}} = \frac{B}{H} = \frac{\text{Base}}{\text{Hypotenuse}} = \frac{BA}{AC}$$

$$\tan \theta = \frac{\mathbf{Prasad}}{\mathbf{Bhole}} = \frac{P}{B} = \frac{\text{Perpendicular}}{\text{Base}} = \frac{BC}{AB}$$

$$\cot \theta = \frac{\mathbf{Bhole}}{\mathbf{Prasad}} = \frac{B}{P} = \frac{\mathbf{Base}}{\mathbf{Perpendicular}} = \frac{AB}{BC}$$

$$\sec \theta = \frac{\mathbf{Har}}{\mathbf{Badri}} = \frac{H}{B} = \frac{\mathbf{Hypotenuse}}{\mathbf{Base}} = \frac{AC}{BA}$$

Oswaal CBSE Revision Notes Chapterwise & Topicwise, MATHEMATICS (STANDARD), Class-X



Trigonometric Identities

<u>Concepts Covered</u> • Three important identities are: (i) $\sin^2 \theta + \cos^2 \theta = 1$, (ii) $1 + \tan^2 \theta = \sec^2 \theta$, (iii) $1 + \cot^2 \theta = \csc^2 \theta$.

Revision Notes

Topic-2

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- An equation is called an identity if it is true for all values of the variable(s) involved.
- An equation involving trigonometric ratios of an angle is called a trigonometric identity if it is true for all values of the angle.

In \triangle *ABC*, right-angled at *B*, By Pythagoras Theorem,

$$AB^{2} + BC^{2} = AC^{2} \qquad \dots (i)$$

 $AB^2 + BC^2 = AC^2$. Dividing each term of (i) by AC^2 ,

$$\frac{AB^2}{AC^2} + \frac{BC^2}{AC^2} = \frac{AC^2}{AC^2}$$

or $\left(\frac{AB}{AC}\right)^2 + \left(\frac{BC}{AC}\right)^2 = \left(\frac{AC}{AC}\right)^2$

or $(\cos A)^2 + (\sin A)^2 = 1$ or $\cos^2 A + \sin^2 A = 1$...(ii)

This is true for all values of *A* such that $0^{\circ} \le A \le 90^{\circ}$. So, this is a trigonometric identity. Now divide eqn.(i) by AB^2 .

$$\frac{AB^2}{AB^2} + \frac{BC^2}{AB^2} = \frac{AC^2}{AB^2}$$

or $\left(\frac{AB}{AB}\right)^2 + \left(\frac{BC}{AB}\right)^2 = \left(\frac{AC}{AB}\right)^2$
or $1 + \tan^2 A = \sec^2 A$...(iii)

Is this equation true for $A = 0^\circ$? Yes, it is. What about $A = 90^\circ$? Well, tan A and sec A are not defined for $A = 90^\circ$. So, eqn. (iii) is true for all values of A such that $0^\circ \le A < 90^\circ$.

Again dividing eqn. (i) by BC^2 .

$$\frac{AB^2}{BC^2} + \frac{BC^2}{BC^2} = \frac{AC^2}{BC^2}$$

or $\left(\frac{AB}{BC}\right)^2 + \left(\frac{BC}{BC}\right)^2 = \left(\frac{AC}{BC}\right)^2$
or $\cot^2 A + 1 = \csc^2 A$...(iv)

Note that cosec *A* and cot *A* are not defined for all $A = 0^{\circ}$. Therefore eqn. (iv) is true for all values of *A* such that $0^{\circ} < A \le 90^{\circ}$.

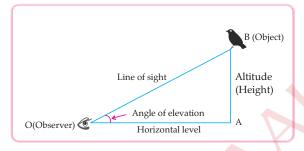
Using these identities, we can express each trigonometric ratio in terms of other trigonometric ratios, *i.e.*, if any one of the ratios is known, we can determine the values of other trigonometric ratios.

CHAPTER-10

SOME APPLICATIONS OF TRIGONOMETRY

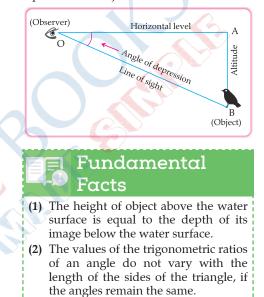
Revision Notes

- The line of sight is the line drawn from the eye of an observer to the point on the object viewed by the observer.
- The angle of elevation of a point on the object being viewed is the angle formed by the line of sight with the horizontal when it is above the horizontal level, *i.e.*, the case when we raise our head to look at a point on the object.
- Line of sight, angle of elevation and altitude (height):



- (i) $\angle AOB$ is the angle of elevation.
- (ii) By height AB, means object is at point B from the point A located at the ground.
- (iii) AO is the distance of the observer from the point A.

The angle of depression of a point on the object being viewed is the angle formed by the line of sight with the horizontal when it is below the horizontal level, *i.e.*, the case when we lower our head to look at a point on the object.

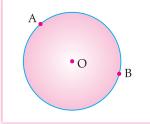


CHAPTER-11

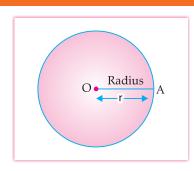
AREAS RELATED TO CIRCLES

Revision Notes

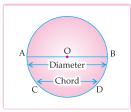
A circle is a collection of all points in a plane which are at a constant distance from a fixed point in the same plane.



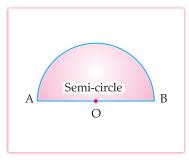
A line segment joining the centre of the circle to a point on the circumference of the circle is called its radius.



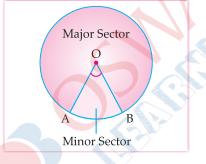
A line segment joining any two points of a circle is called a chord. A chord passing through the centre of circle is called its diameter. A diameter is the longest chord of the circle. Here AB is a diameter.



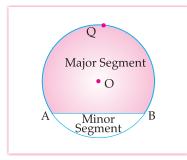
A diameter of a circle divides a circle into two equal arcs, each known as a semi-circle.



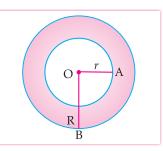
- A part of a **circumference** of circle is called an arc.
- An arc of a circle whose length is less than that of a semi-circle of the same circle is called a minor arc.
- An arc of a circle whose length is greater than that of a semi-circle of the same circle is called a major arc.
- The region bounded by an arc of a circle and two radii at its end points is called a sector.



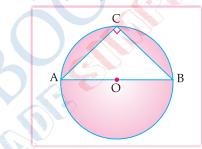
A chord divides the interior of a circle into two parts, each called a segment.



Circles having the same centre but different radii are called concentric circles.



- Two circles (or arcs) are said to be congruent if on placing one over the other cover each other completely.
- The distance around the circle or the length of a circle is called its circumference or perimeter.
- The mid-point of the hypotenuse of a right triangle is equidistant from the vertices of the triangle.
- Angle subtended at the circumference by a diameter is always a right angle.



- Angle described by minute hand in 60 minutes is 360°.
- Angle described by hour hand in 12 hours is 360°.

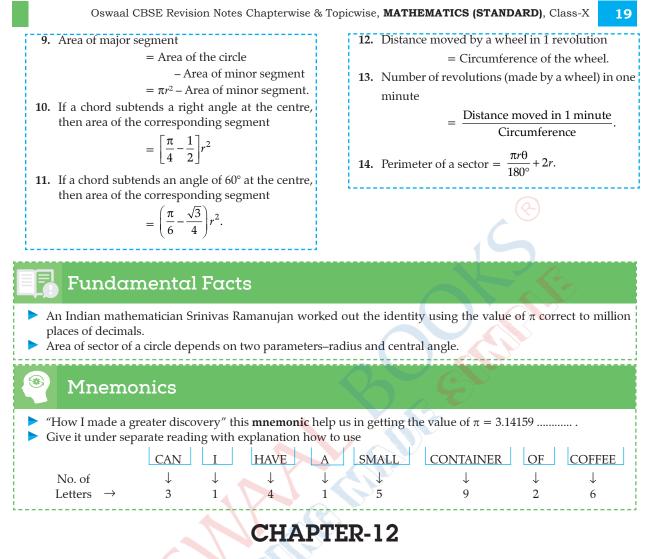
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- **1.** Circumference (perimeter) of a circle = πd or $2\pi r$, where *d* is diameter and *r* is the radius of the circle.
- **2.** Area of a circle = πr^2 .
- 3. Area of a semi-circle = $\frac{1}{2}\pi r^2$.
- **4.** Perimeter of a semi-circle = $\pi r + 2r = (\pi + 2)r$
- 5. Area of a ring or an annulus $= \pi(R + r)(R r)$. where R is the outer radius and r is the inner radius.
- 6. Length of arc, $l = \frac{2\pi r\theta}{360^{\circ}}$ or $\frac{\pi r\theta}{180^{\circ}}$, where θ is the angle subtended at centre by the arc.

7. Area of a sector =
$$\frac{\pi r^2 \theta}{360^\circ}$$
 or area of sector

 $=\frac{1}{2}(l \times r)$, where *l* is the length of arc.

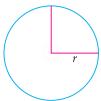
8. Area of minor segment = $\frac{\pi r^2 \theta}{360^\circ} - \frac{1}{2}r^2 \sin \theta$.



SURFACE AREAS AND VOLUMES

Revision Notes

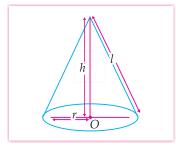
A sphere is a perfectly round geometrical object in three-dimensional space.



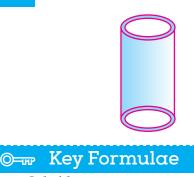
A hemisphere is half of a sphere.

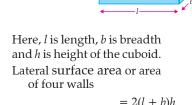


A cone is a three dimensional geometric shape tapers smoothly from a flat base to a point called the apex or vertex.



A cylinder is a solid or a hollow object that has a circular base and a circular top of the same size.





Total surface area =
$$2(lb + bh + hl)$$

Volume = $l \times b \times h$

$$Diagonal = \sqrt{l^2 + b^2 + h^2}$$

Cube:

Cuboid:

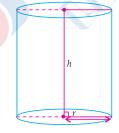
Here, *a* is edge of cube.

Lateral surface area or area of four walls = $4 \times a^2$

Total surface area = $6 \times a^2$ Volume = a^3

Diagonal of a cube = $\sqrt{3} \times a$

Right Circular Cylinder:

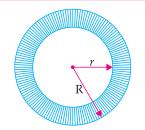


Here, *r* is the radius of base and *h* is the height of the right circular cylinder. Area of base or top face = πr^2 Area of curved surface or curved surface area = perimeter of the base × height = $2\pi rh$ Total surface area (including both ends)

 $= 2\pi rh + 2\pi r^2 = 2\pi r(h + r)$ Volume = (Area of the base × height) = π

volume = (Area of the base × height) =
$$\pi r^2 h$$

Right Circular Hollow Cylinder:



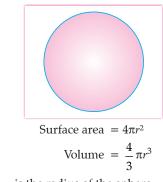
Here, R and r are the external and internal radii and *h* is the height of the right circular hollow cylinder. Total surface area = (External surface area + Internal surface area + Area of brim $= (2\pi Rh + 2\pi rh) + 2(\pi R^2 - \pi r^2)$ $= [2\pi h(R+r) + 2\pi (R^2 - r^2)]$ $= [2\pi(R + r)(h + R - r)]$ Curved surface area = $(2\pi Rh + 2\pi rh) = 2\pi h(R + r)$ Volume of the material used = (External volume) – (Internal volume) $=\pi R^{2}h - \pi r^{2}h = \pi h(R^{2} - r^{2})$ **Right** Circular Cone: Here, r, h and l are the radius, vertical height and slant height respectively of the right circular cone. $l = \sqrt{h^2 + r^2}$ Slant height, Area of curved surface $= \pi r l$ $=\pi r\sqrt{h^2+r^2}$ Total surface area = Area of curved surface

+ Area of base

$$= \pi r l + \pi r^2$$
$$= \pi r (l + r)$$

Volume =
$$\frac{1}{2}\pi r^2 h$$

Sphere:



Here, *r* is the radius of the sphere.

Spherical Shell:

Here, R and *r* are the external and internal radii of the spherical shell. Surface area (outer) = $4\pi R^2$

Volume of material =
$$\frac{4}{3}\pi R^3 - \frac{4}{3}\pi r^3$$

= $\frac{4}{3}\pi (R^3 - r^3)$

Hemisphere:

Here, *r* is the radius of the hemisphere. Area of curved surface = $2\pi r^2$ Total surface area= Area of curved surface

+ Area of base

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 $= 3\pi r^2$ Volume = $\frac{2}{3}\pi r^3$

 $=2\pi r^{2}+\pi r^{2}$

CHAPTER-13 STATISTICS

Revision Notes

- Statistics deals with the collection, presentation and analysis of numerical data.
- Three measures of central tendency are:
 (i) Mean, (ii) Median and (iii) Mode.
- Mean: In statistics mean stands for the arithmetic mean of the given items.

i.e., Mean = $\frac{\text{Sum of given items}}{\text{No. of items}}$

Median: It is defined as the middle most or the central value of the variable in a set of observations, when the observations are arranged either in ascending or descending order of their magnitudes.

It divides the arranged series in two equal parts i.e., 50% of the observations lie below the median and the remaining are above the median.

Mode: Mode is the observation which occurred maximum times. In ungrouped data, mode is the observation having maximum frequency. In a grouped frequency distribution, it is not possible to determine the mode by looking at the frequencies. To find the mode of grouped data, locate the class with the maximum frequency. This class is known as the modal class. The mode of the data is a value inside the modal class.

©=₩ Key Formulae

Mean:

(a) For Raw Data:

If *n* observations $x_1, x_2, ..., x_n$ are given, then their arithmetic mean is given by :

$$\overline{x} = \frac{x_1 + x_2 + \dots + x_n}{n} = \frac{1}{n} \sum_{i=1}^n x_i$$

(b) For Ungrouped Data:

If there are *n* distinct observations x_1 , x_2 ,..., x_n of variable *x* with frequencies f_1 , f_2 ,..., f_n respectively, then the arithmetic mean is given by:

$$\bar{x} = \frac{f_1 x_1 + f_2 x_2 + \dots + f_n x_n}{f_1 + f_2 + f_3 + \dots + f_n} = \frac{\sum_{i=1}^n f_i x_i}{\sum_{i=1}^n f_i}$$

- (c) For Grouped Data:
 - (i) To find the mean of grouped data, it is assumed that the frequency of each class-interval is centred around its mid-point.
 - (ii) Direct Method:

Mean
$$(\bar{x}) = \frac{\Sigma f_i x_i}{\Sigma f_i}$$

where the x_i (class mark) is the mid-point of the *i*th class interval and f_i is the corresponding frequency.

(iii) Assumed Mean Method or Short-cut Method:

$$Mean(\bar{x}) = A + \frac{\Sigma f_i d_i}{\Sigma f_i}$$

where, *A* is the assumed mean and $d_i = x_i - A$ are the deviations of x_i from *A* for each *i*.

(iv) Step-Deviation Method:

Mean
$$(\bar{x}) = A + h\left(\frac{\Sigma f_i u_i}{\Sigma f_i}\right)$$

where, *A* is the assumed mean, *h*

the class size and
$$u_i = \frac{x_i - A}{h}$$

Median of Grouped Data:

is

Let $N = f_1 + f_2 + f_3 + \dots + f_n$. First of all $\frac{N}{2}$ and then the class in which $\frac{N}{2}$ field This

class is known as the **median class.** Median of the given distribution lies in this class.

Median of the grouped data can be calculated using the formula:

Median (M_e) =
$$l + \left(\frac{\frac{N}{2} - c.f.}{f}\right) \times h$$

where l = lower limit of median class, f = frequency of median class, N = number of observations, *c.f.* = cumulative frequency of the class preceding the median class, h = class-size or width of the class-interval.

Mode of Grouped Data:

Mode of the grouped data can be calculated by using the formula:

Mode (M) =
$$l + \left(\frac{f_1 - f_0}{2f_1 - f_0 - f_2}\right) \times h$$

where, l = lower limit of the modal class, h = width or size of the class-interval, $f_1 =$ frequency of the modal class, $f_0 =$ frequency of the class preceding the modal class, $f_2 =$ frequency of the class succeeding the modal class.

- Empirical relation between mean, median and mode:
- (i) Mode = 3 median 2 mean
- (ii) Median = $\frac{1}{3}$ mode + $\frac{2}{3}$ mean

(iii) Mean =
$$\frac{3}{2}$$
 median – $\frac{1}{2}$ mode

Fundamental Facts

- The mean is the average of a data set.The mode is the most common number in a data set.
- The median is the middle of the set of numbers.

CHAPTER-14

PROBABILITY

Revision Notes

- Probability is a branch of mathematics that deals with calculating the likelihood of a given event's occurrence.
- A random experiment is an experiment or a process for which the outcome cannot be predicted with certainty. *e.g.*

(i) tossing a coin, (ii) throwing a dice, (iii) selecting a card and (iv) selecting an object etc.

- Outcome associated with an experiment is called an event. *e.g.*, (i) Getting a head on tossing a coin, (ii) getting a face card when a card is drawn from a pack of 52 cards.
- The events whose probability is one are called sure/ certain events.
- The events whose probability is zero are called impossible events.
- An event with only one possible outcome is called an elementary event.
- In a given experiment, if two or more events are equally likely to occur or have equal probabilities, then they are called equally likely events.
- Probability of an event always lies between 0 and 1.

- Probability can never be negative and more than one.
- A pack of playing cards consists of 52 cards which are divided into 4 suits of 13 cards each. Each suit consists of an ace, one king, one queen, one jack and 9 other cards numbered from 2 to 10. Four suits are spades, hearts, diamonds and clubs.
- King, queen and jack are face cards.
- The sum of the probabilities of all elementary events of an experiment is 1.
- Two events A and B are said to be complementary to each other if the sum of their probabilities is 1.
- Probability of an event E, denoted as P(E), is given by:

$P(E) = \frac{\text{Number of outcomes favourable to } E}{\text{Total possible number of outcomes}}$

- For an event E, $P(\overline{E}) = 1 P(E)$, where the event \overline{E} representing 'not E' is the complement of the event E.
- For A and B two possible outcomes of an event,
 - (i) If P(A) > P(B), then event A is more likely to occur than event B.
 - (ii) If P(A) = P(B), then events A and B are equally likely to occur.

©=₩ Know the Facts

The experimental or empirical probability of an event is based on what has actually happened while the theoretical probability of the event attempts to predict what will happen on the basis of certain assumptions.

- As the number of trials in an experiment go on increasing, we may expect the experimental and theoretical probabilities to be nearly the same.
- When we speak of a coin, we assume it to be 'fair ' i.e., it is symmetrical so that there is no reason for it to come down more often on one side than the other. We call this property of the coin as being 'unbiased'.
- In the case of experiment we assume that the experiments have equally likely outcomes.
- A deck of playing cards consists of 4 suits : spades (♠), hearts (♥), diamonds (♠) and clubs (♣). Clubs and spades are of black colour, while hearts and diamonds are of red colour.

Fundamental

By the phrase '**random toss**', we mean that the coin is allowed to fall freely without any **bias** or **interference**.

