

N : Natural numbers

(1, 2, 3, ...)

W : Whole numbers

(0, 1, 2, ...)

I or Z: Integers

(-3, -2, -1, 0, 1, 2, 3 ...)

Q : Rational numbers

(p/q , p, q are integers, $q \neq 0$)

R : Real numbers

(All numbers, including irrationals like $\sqrt{3}$, $\sqrt{2} + \sqrt{3}$, $\sqrt[3]{5}$, etc.)

• A.M. = $\frac{a+b}{2}$

• G.M. = \sqrt{ab}

• A.M. \geq G.M.

Test of Divisibility

Shortcuts to check the given number is divisible by 2, 3, 5, 4, 7, 8, 9, 10, 11 and 13

To check number is prime

- Choose 'K' such that $K^2 \geq l$
- Find the primes less than K
- If those do not divide 'l', then 'l' is prime

Counting number of zeros at the end of $n!$ is integral value of

$$\left(\frac{n}{5} + \frac{n}{5^2} + \frac{n}{5^3} + \dots \right)$$

Number System

Even numbers: 2, 4, 6, ...

Odd numbers: 1, 3, 5, ...

Prime numbers

Divisible by 1 and itself

Co-Prime numbers

Their H.C.F. is 1

Composite numbers

Have more than two factors

(It can be both Odd and Even)

e.g., 4, 6, 8, 9, 10, ...

• Term in A.P. are $a, a + d, a + 2d \dots$

• Term in G.P. are $a, ar, ar^2 \dots$

A.P.

• $T_n = a + (n - 1)d$

• $S_n = \frac{n}{2} [2a + (n - 1)d]$

• $S_n = \frac{n}{2} (a + l)$

(Where l = last term)

G.P.

• $T_r = ar^{n-1}$

• $S_n = \frac{a(1 - r^n)}{1 - r}, r < 1$

• $S_n = \frac{a(r^n - 1)}{r - 1}, r > 1$

Division Algorithm

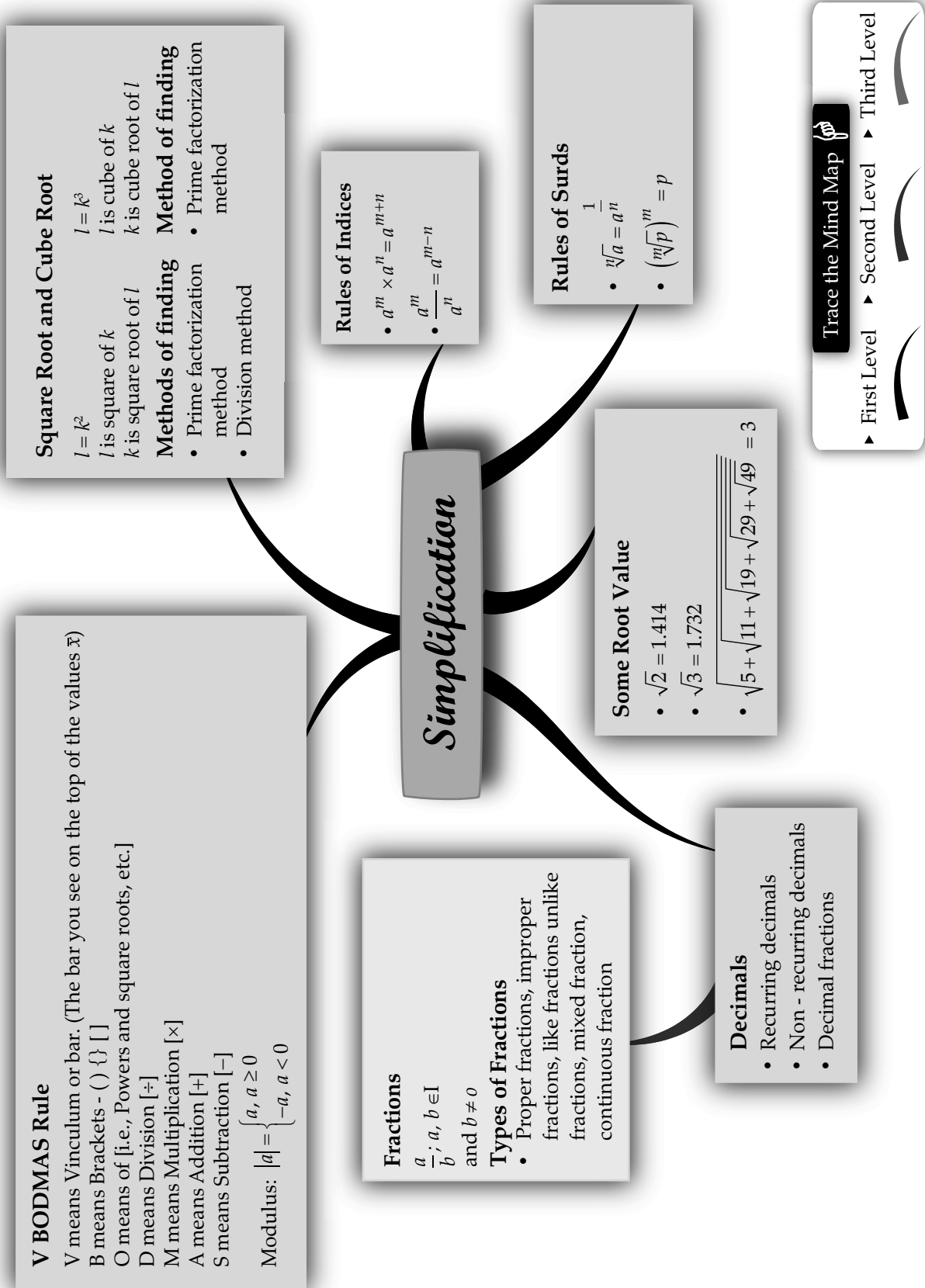
Dividend = Divisor \times Quotient + Remainder

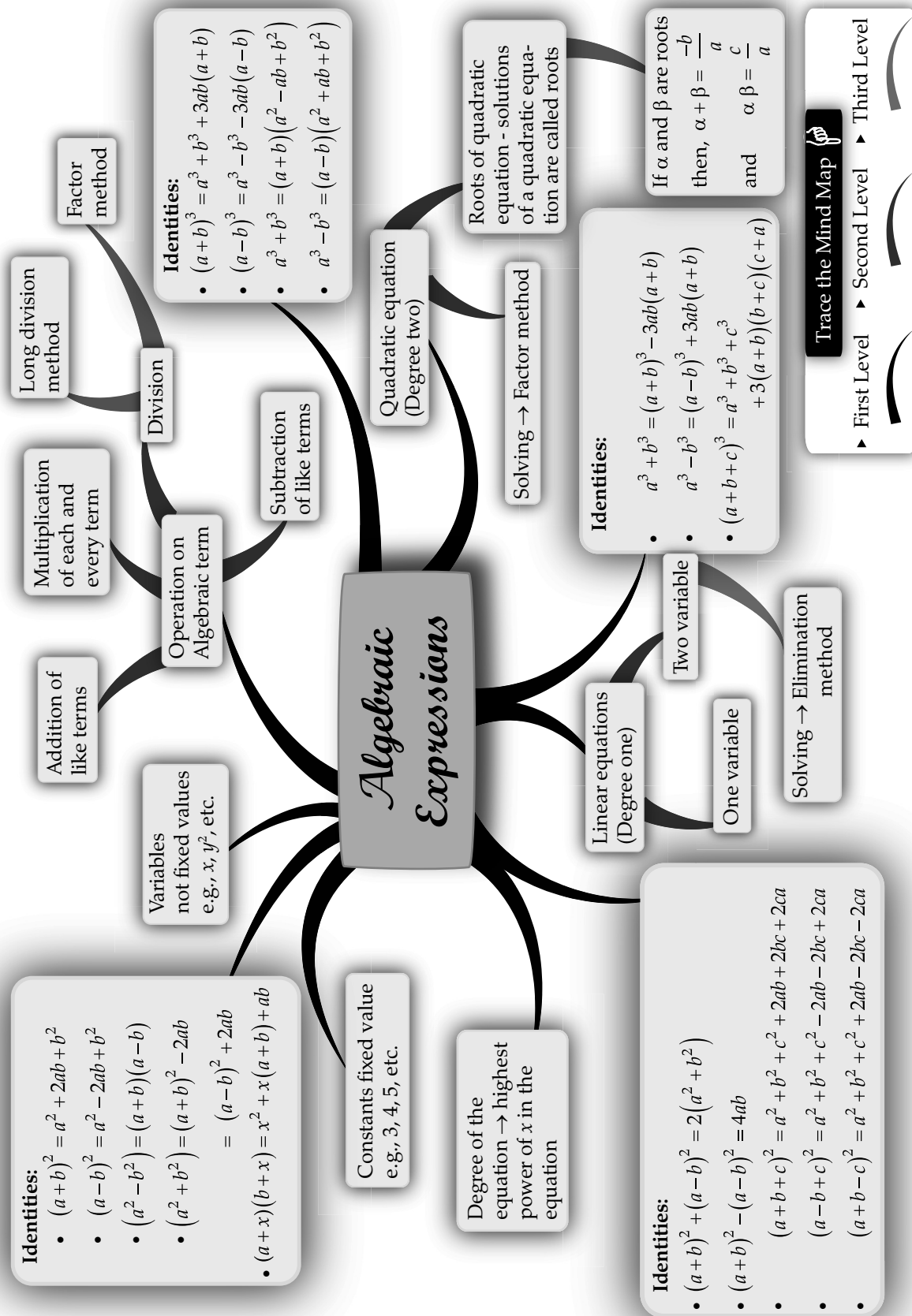
H.C.F. and L.C.M.

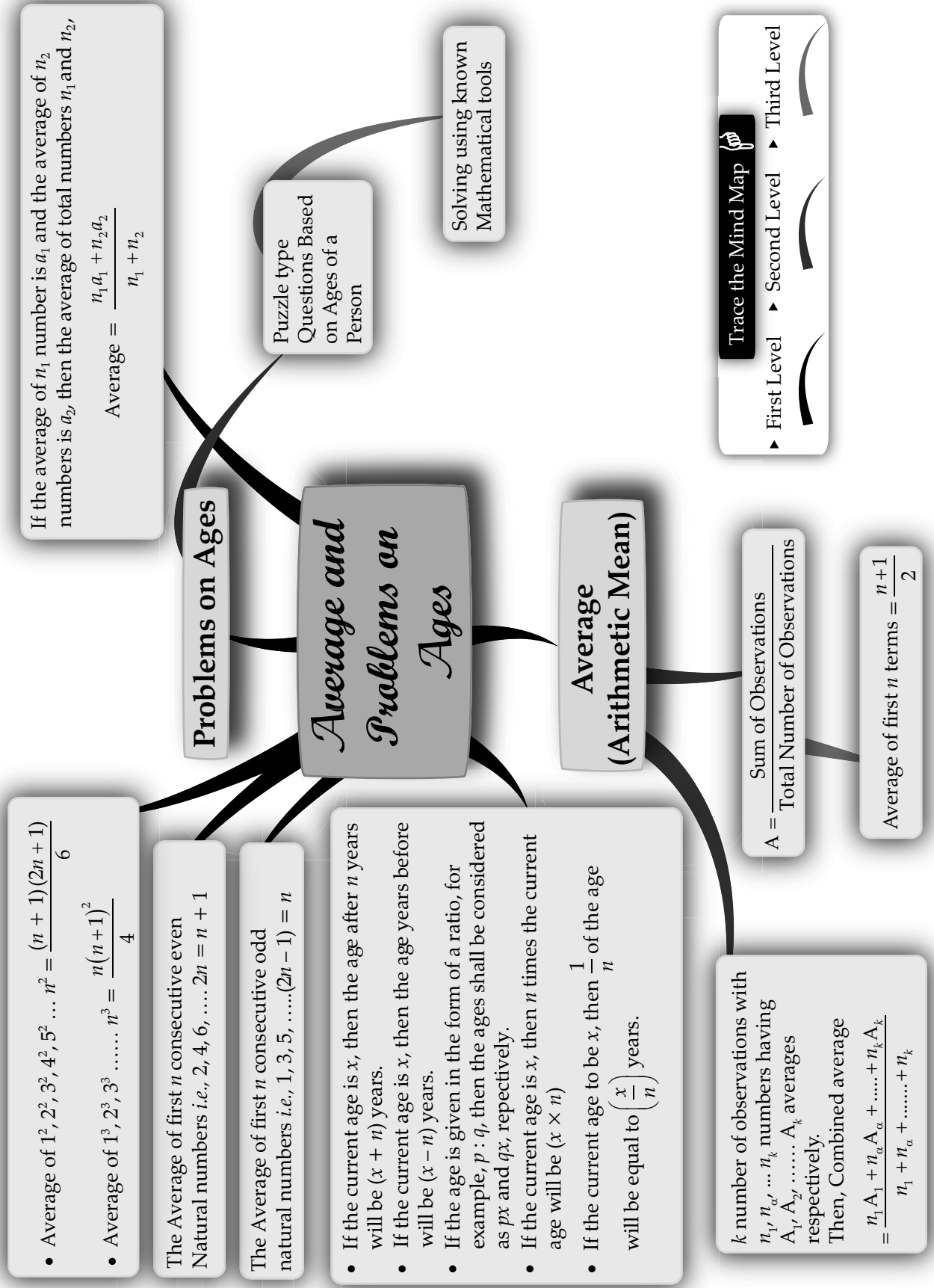
- Highest Common Factor
- Least Common Multiple
- Methods to find factorization / division
- $a \times b = \text{H.C.F.}(a, b) \times \text{L.C.M.}(a, b)$
- H.C.F. of fractions = $\frac{\text{H.C.F. of Numerators}}{\text{L.C.M. of Denominators}}$
- L.C.M. of fractions = $\frac{\text{L.C.M. of Numerators}}{\text{H.C.F. of Denominators}}$

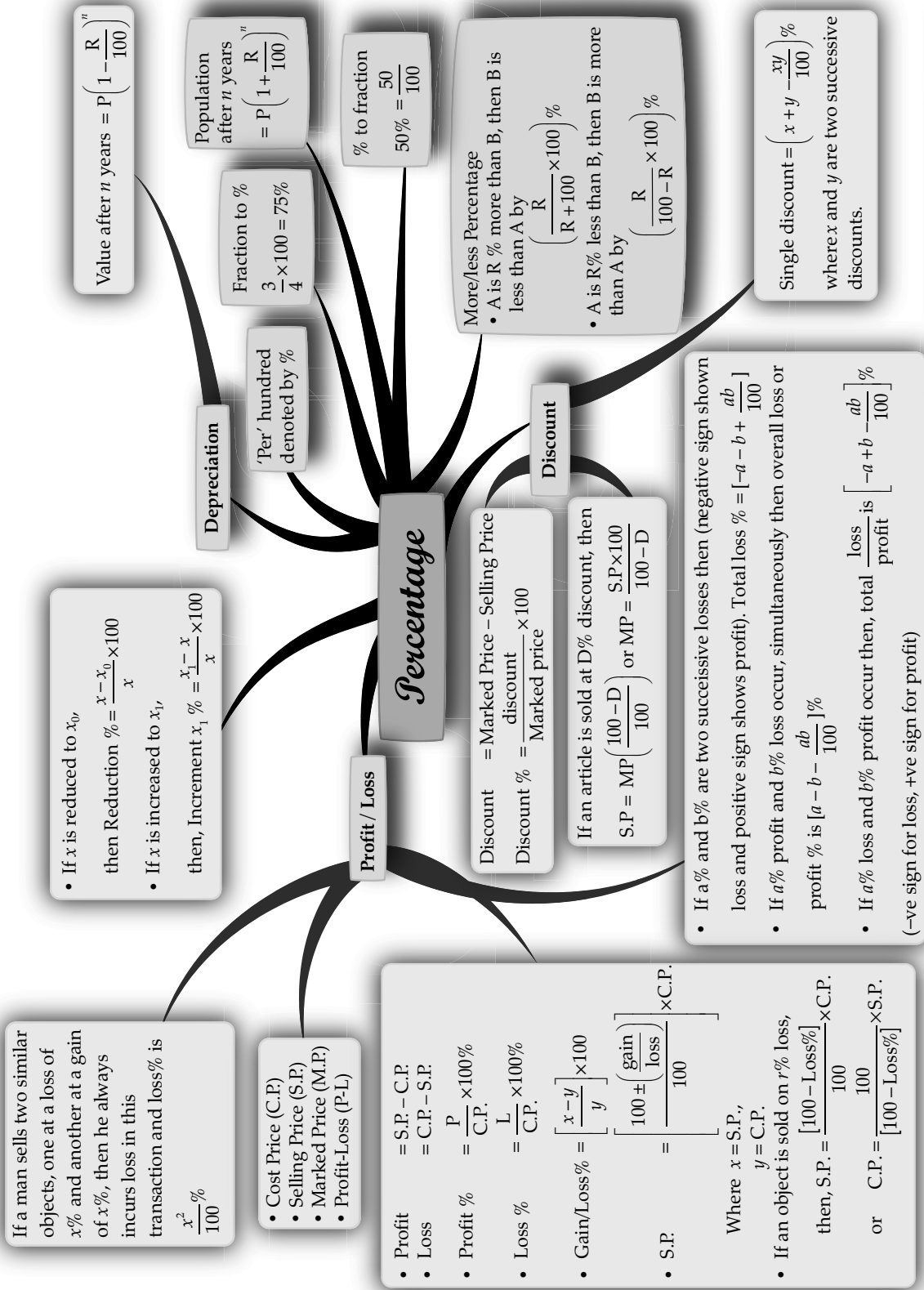
Trace the Mind Map

► First Level ► Second Level ► Third Level



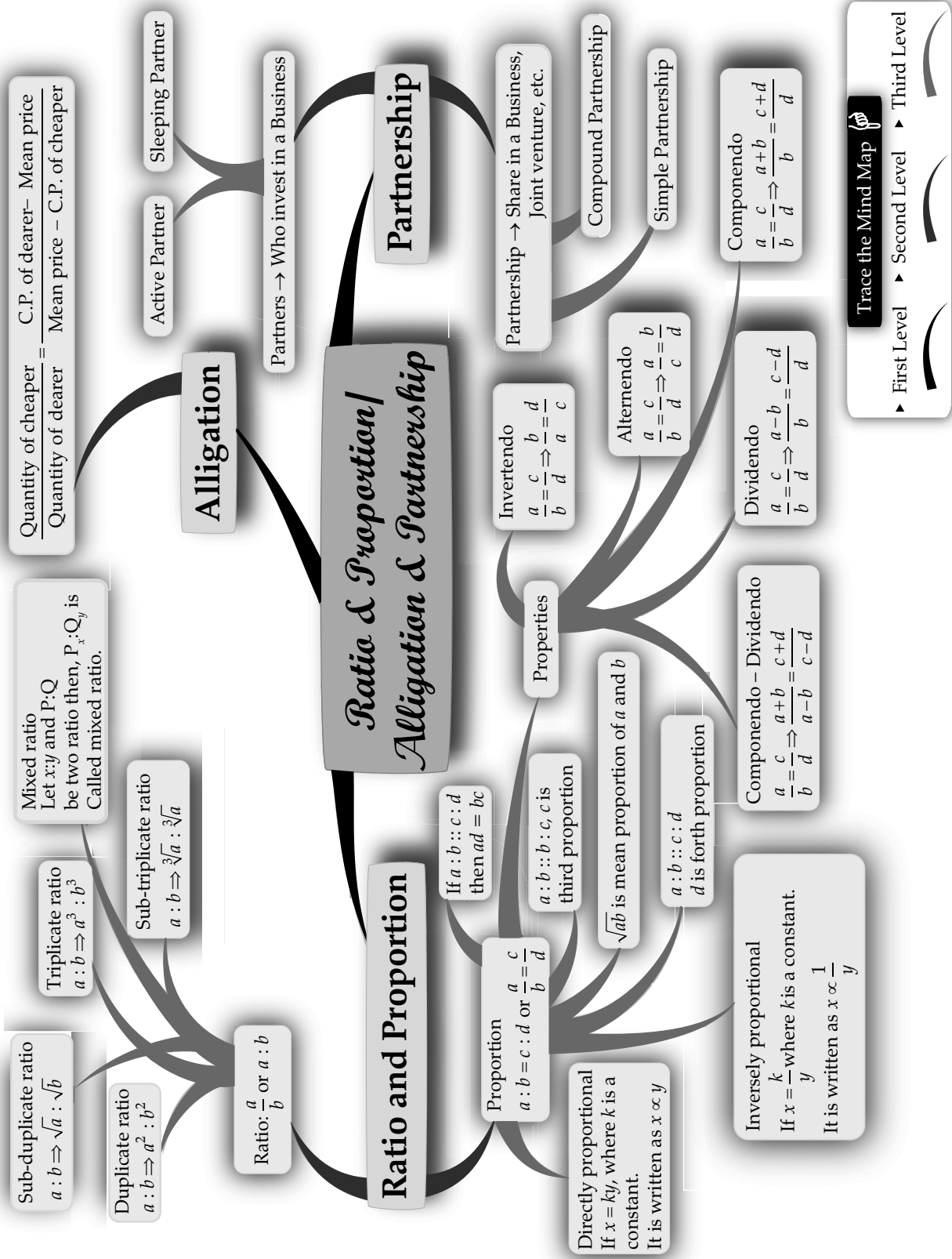


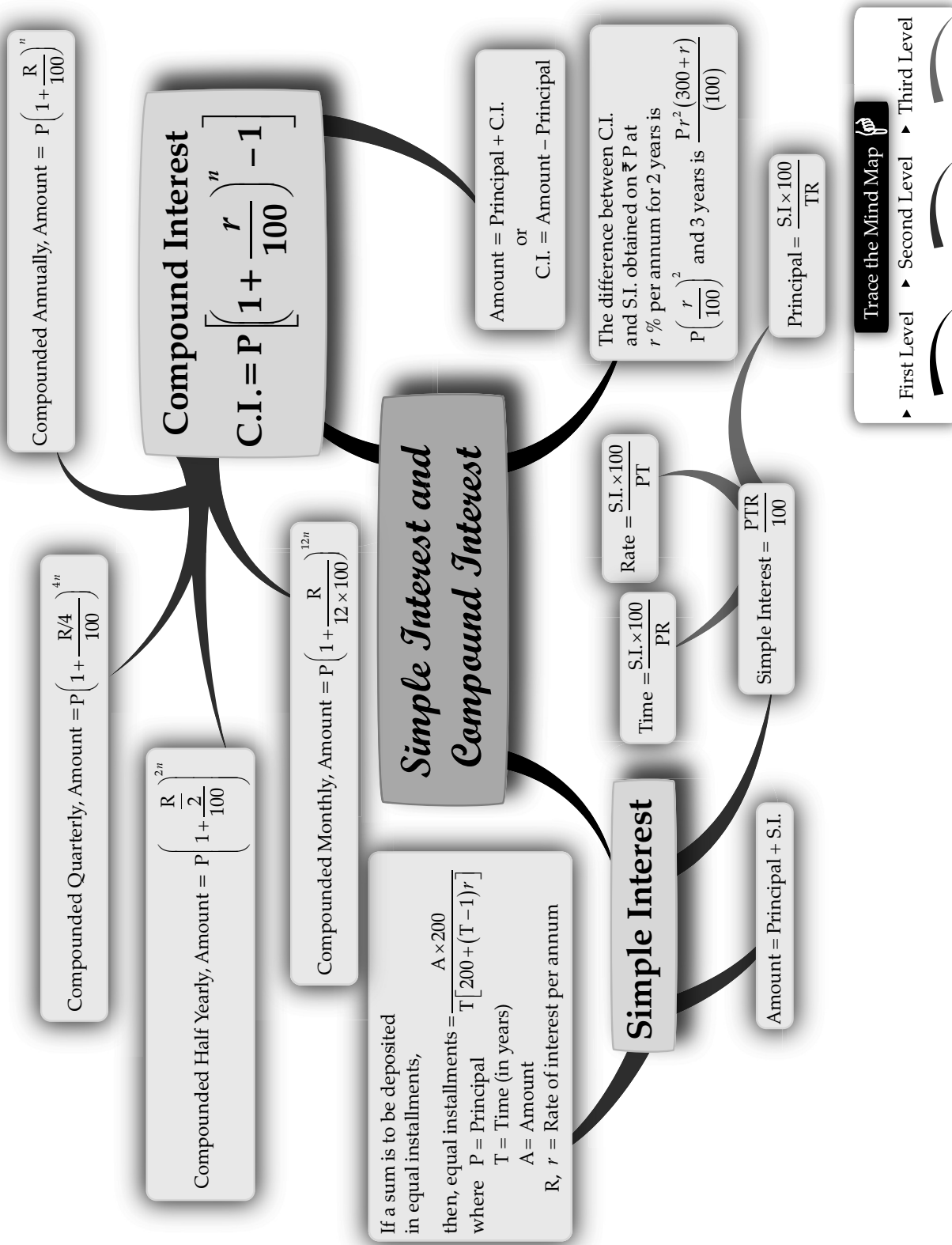


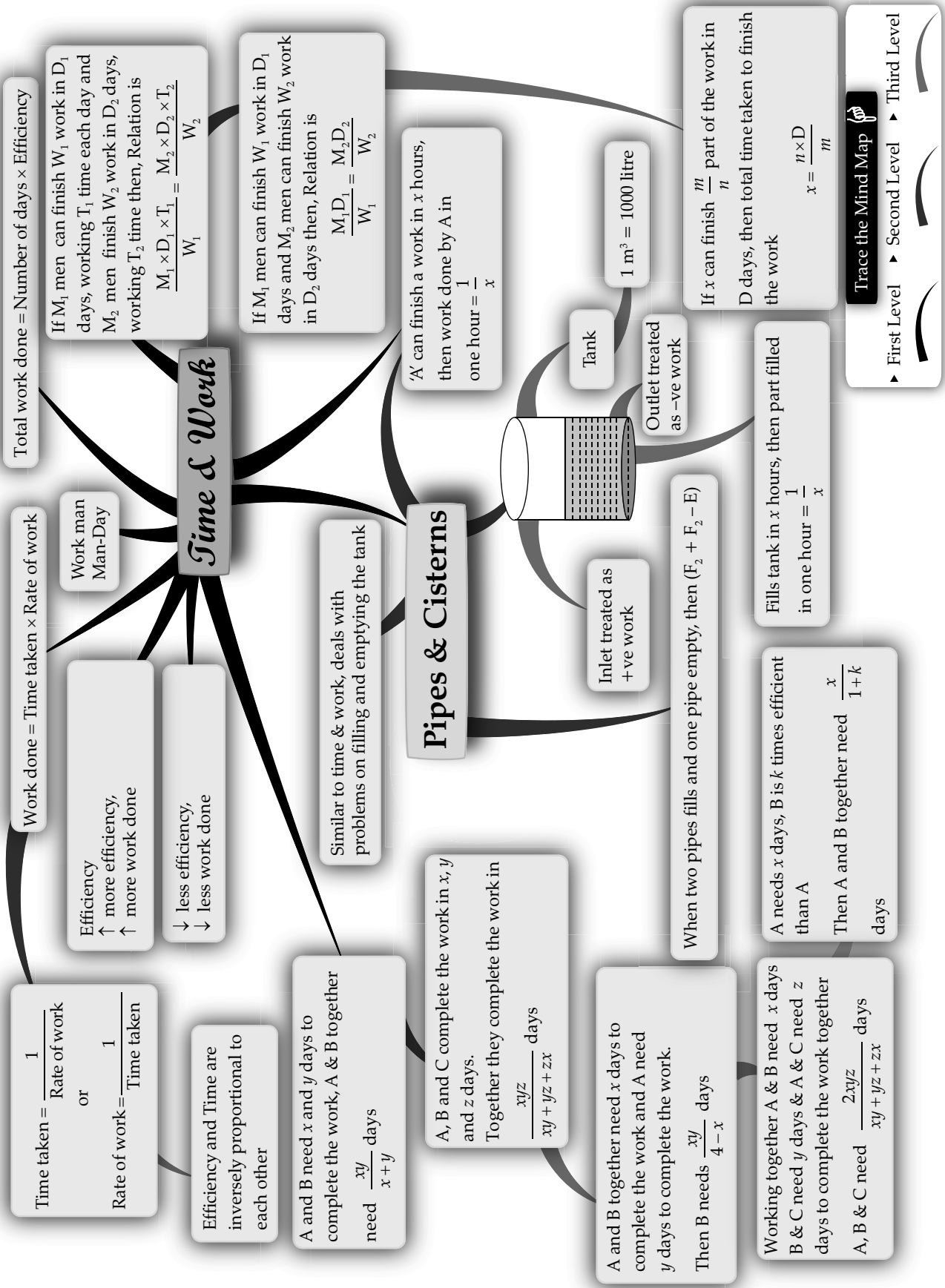


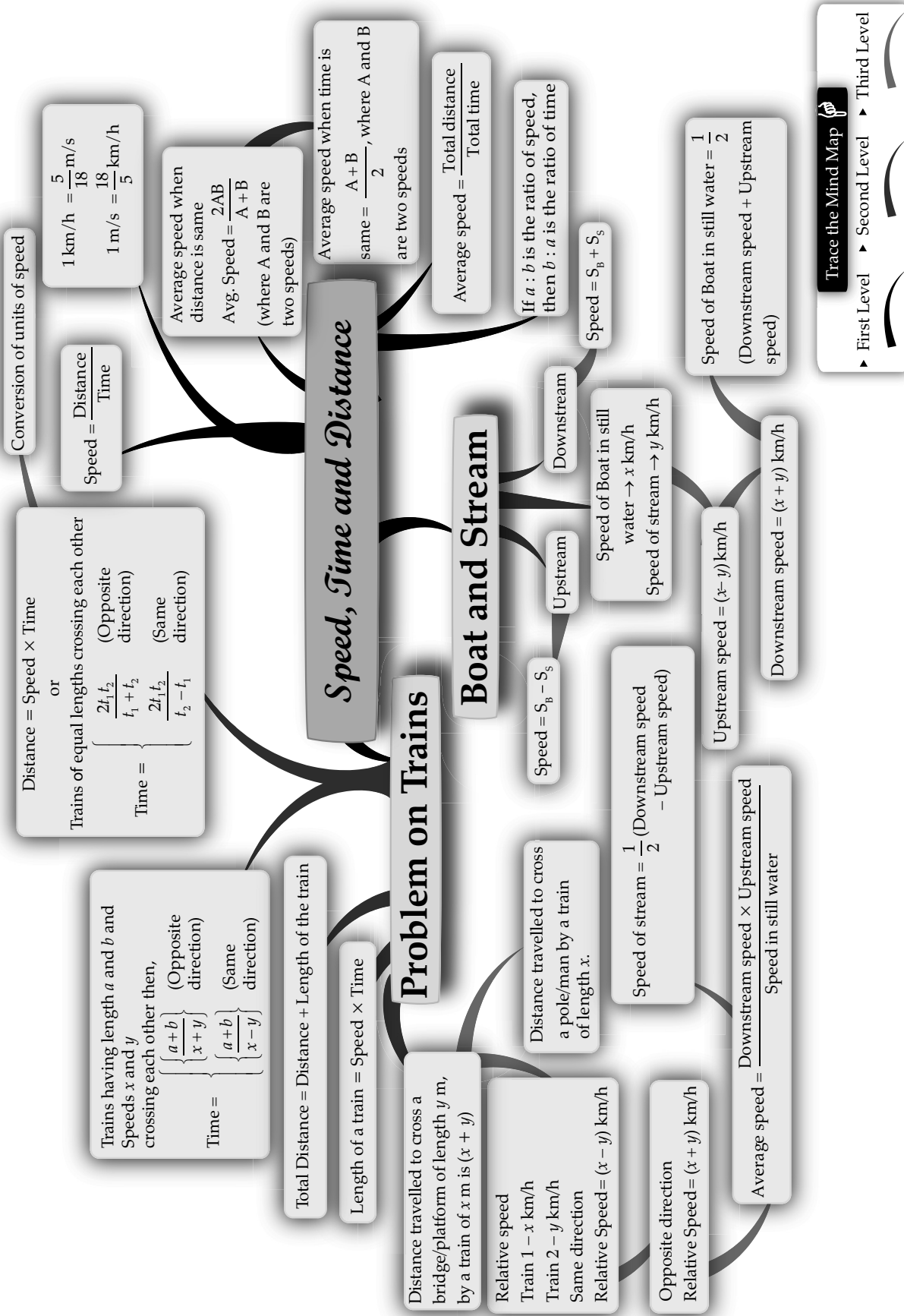
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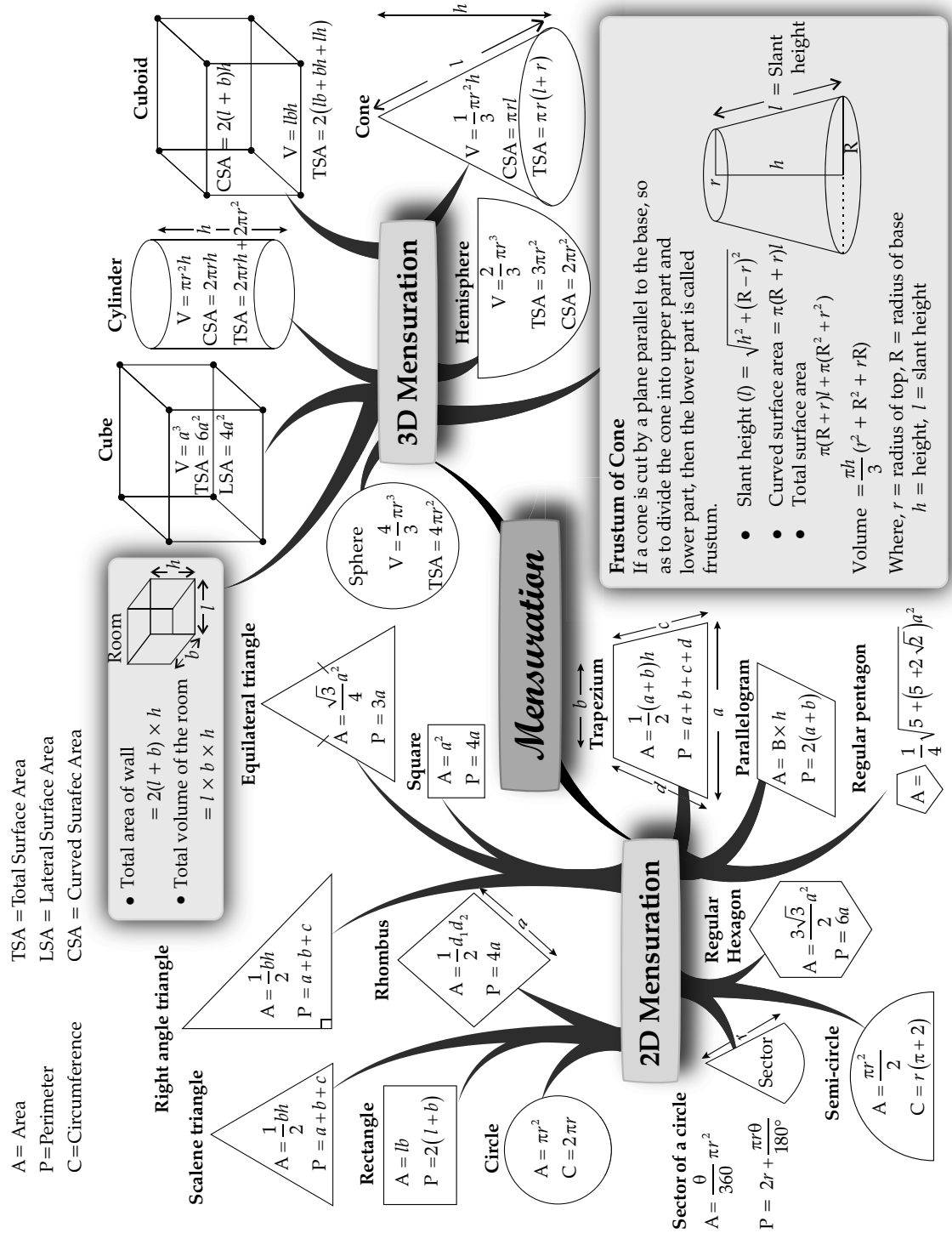
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Trace the Mind Map

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Trigonometry Ratios Table

Angles (In Degrees) Angles (In Radians)	0° 0	30° $\frac{\pi}{6}$	45° $\frac{\pi}{4}$	60° $\frac{\pi}{3}$	90° $\frac{\pi}{2}$
sin A	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1
cos A	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0
tan A	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	∞ (not defined)

Pythagoras theorem

Consider the triangle given below where a is the perpendicular, b is the base, c is the hypotenuse.



$$c^2 = a^2 + b^2$$

- On Y-axis $[90^\circ \pm \theta, 270^\circ \pm 0]$ $\sin \rightleftharpoons \cos, \sec \rightleftharpoons \text{cosec}$ and $\tan \rightleftharpoons \cot$

- On X-axis $[180^\circ \pm \theta, 360^\circ \pm 0]$ $\sin \rightarrow \sin, \cos \rightarrow \cos$ similarly, for other trigonometric ratios.

Fundamental relation

- $\frac{1}{\sin \theta} = \text{cosec } \theta$
- $\frac{1}{\cos \theta} = \text{sec } \theta$
- $\frac{1}{\tan \theta} = \cot \theta$

Radian

$$R^C = \left(\frac{180}{\pi} \right)^\circ$$

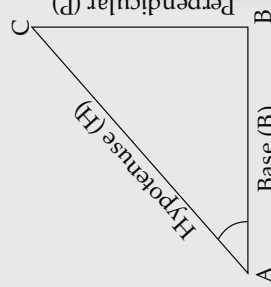
Degree

$$180^\circ = \pi^C$$

Trigonometry

Trigonometry Formulas

- $\sin A = \frac{BC}{AC} = \frac{P}{H}$
- $\cos A = \frac{AB}{AC} = \frac{B}{H}$
- $\tan A = \frac{BC}{AB} = \frac{P}{B}$
- $\text{cosec } A = \frac{AC}{BC} = \frac{H}{P}$
- $\sec A = \frac{AC}{AB} = \frac{H}{B}$
- $\cot A = \frac{AB}{BC} = \frac{B}{P}$

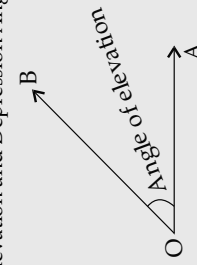
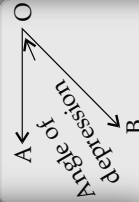


- Angle in Degrees = Angle in Radians $\times \frac{180^\circ}{\pi}$
- 1 radians = $\frac{180^\circ}{\pi}$

Trigonometric Identities

- $\sin^2 \theta + \cos^2 \theta = 1$
- $1 + \tan^2 \theta = \sec^2 \theta$
- $1 + \cot^2 \theta = \text{cosec}^2 \theta$
- $\tan \theta = \frac{\sin \theta}{\cos \theta}$

Height and Distance
Elevation and Depression Angles



Trigonometric Functions

- $\sin \left(\frac{\pi}{2} - \theta \right) = \cos \theta$ ($\because \frac{\pi}{2} = 90^\circ$)
- $\cos \left(\frac{\pi}{2} - \theta \right) = \sin \theta$
- $\tan \left(\frac{\pi}{2} - \theta \right) = \cot \theta$
- $\cot \left(\frac{\pi}{2} - \theta \right) = \tan \theta$
- $\sec \left(\frac{\pi}{2} - \theta \right) = \text{cosec } \theta$
- $\text{cosec} \left(\frac{\pi}{2} - \theta \right) = \sec \theta$

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