

Benchmarking Traditional PTI Design Against Advanced Finite Element Method on a Ribbed 40x70 Slab-on-Ground and Design of a Wafflemat Using FEM Approach

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Learning Objectives

At the end of this presentation, you will be able to...

- Assess differences between traditional PTI and FEM design methods for slab-on-ground foundations
- Understand FEM design approach
- Evaluate a Wafflemat design
- Confidently apply FEM-based design method to non-traditional slabs

Demand for cost-effective and well performing foundations on expansive soils is very high, however, the existing PTI method of design is very restrictive and does not allow for the implementation of innovative foundation solutions.



Existing Design Methodology Extremely Limited

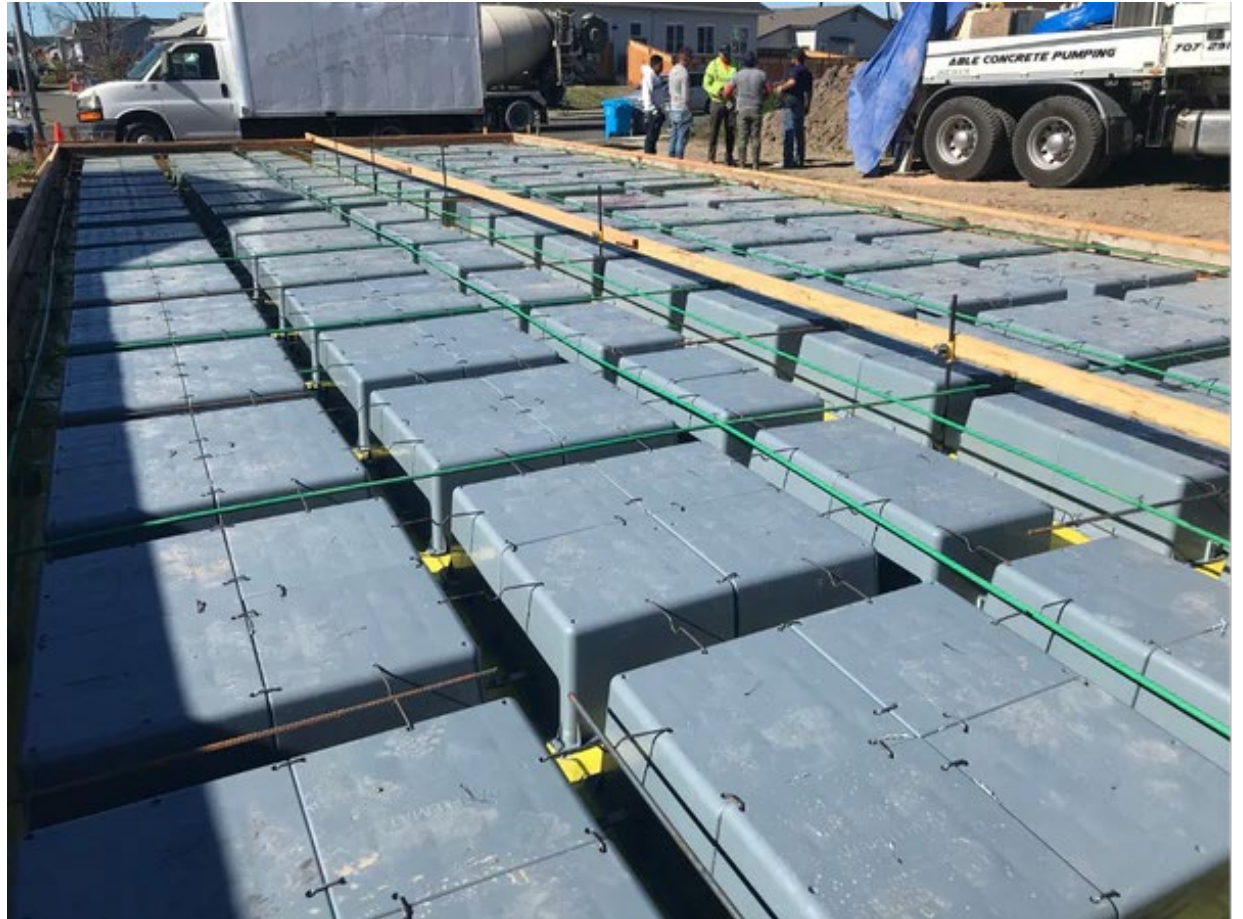
- Prescriptive and not performance-based
- Limited to rectangular shapes
- Overly conservative – worst-case rectangle governs
- Maximum allowable difference in beam depths not greater than 1.2
- Moment calculation discontinuity for Center Lift $e_m > 5$ ft
- Is not set up to analyze and check any other configuration...

PTISlab 3.5 Software Limitations

The PTI design method has been implemented by many companies using their own spreadsheets. For our comparison, we chose PTISlab 3.5 as one of the commonly used and commercially available implementations of the PTI design method.

- Can only model rectangular slabs
- Cannot model beams spaced closer than 6 ft apart
- No flexibility in tendon profiling or placement
- No flexibility in detailed load modeling

An alternative design approach needs to be accepted so that new, innovative solutions can be evaluated and approved.



We are not the first to recognize the need for a more flexible and improved design methodology.

PTI Journal

Industry News

**SLAB-ON-GROUND ALTERNATIVE DESIGN
(SOGAD): A BLEND OF ART AND SCIENCE**

By

JACK W. GRAVES JR., BRIAN M. JUEDES, AND
RYNE C. STOKER



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Leveraging Capabilities of Advanced Finite Element Analysis

A finite element analysis may be performed in lieu of the specific structural design formulas and procedures for slabs on expansive soils presented in this chapter. The finite element model should consider the interaction of the concrete foundation and the soil (see 1.2). The expansive characteristics of the soil should be established using the criteria specified in Chapter 3.

PTI Section 6.1.13

Agenda

- Detailed comparison of PTISlab 3.5 vs FEM design for ribbed 40 x 70 slab
- Parametric study of different soil conditions
- Proposed design method using FEM
- Use of new design method to check and design 40 x 70 Wafflemat slab
- Concluding remarks

Outline of Design Procedure using GTK PTISlab Software

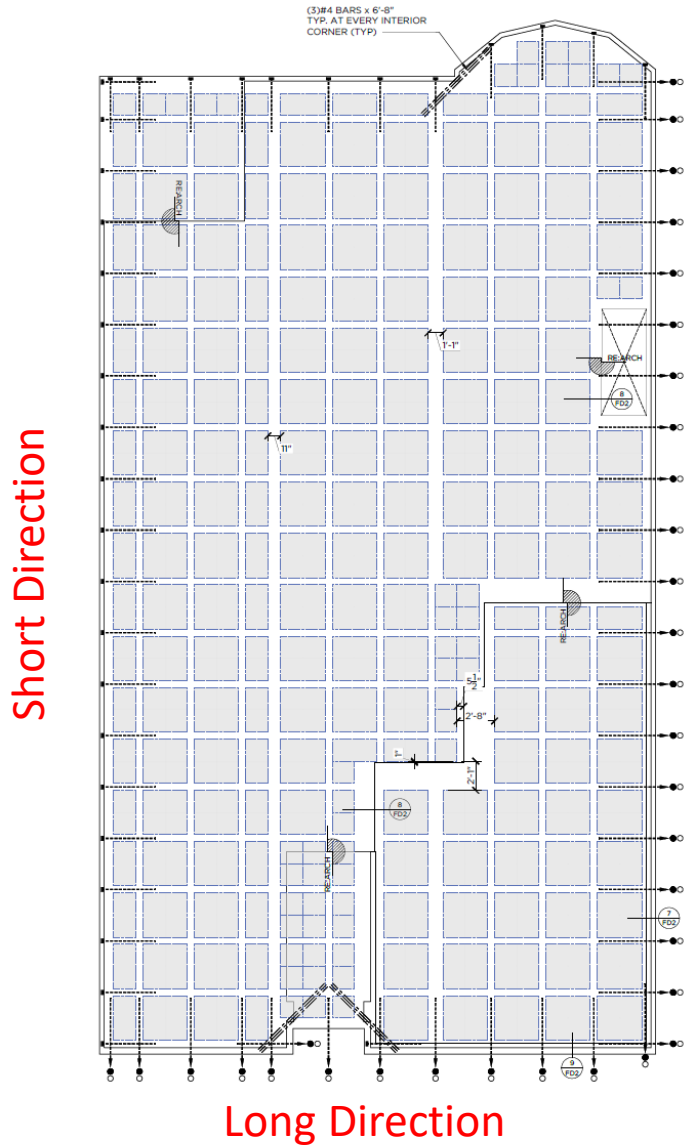
- Soil bearing pressure check
 - Based on Load/Area
- Center lift design checks
 - Bending stress
 - Stiffness
 - Shear stress
 - Cracked moment capacity
- Edge lift design checks
 - Bending stress
 - Stiffness
 - Shear stress
 - Cracked moment capacity

Project: 40x70 Foundation

PVR 4.5" with a 2ft embedment depth

Select Soil Parameters:

	Edge Lift	Center Lift
Edge Moisture Distance, ft (em)	3.5	6.7
Differential Soil Movement, inches (ym)	2.1	1.5



PTISlab 3.5 Input Data: Ribbed Foundation Analysis Model

Slab Dimensions :

40.00 FT x 70.00 FT x 4.00 Inches

Material Properties

Concrete Strength, f'_c : 4,000 PSI
 Tendon Strength, F_{pu} : 270 KSI
 Tendon Diameter : 1 / 2 Inch

Material Quantities

Concrete Volume : 69.8 Cubic Yards
 Prestressing Tendon : 1,392 Linear Feet
 Number of End Anchorages : 52

In the LONG direction ...

	<u>Type I Beam</u>	<u>Type II Beam</u>
Quantity of Beams :	2	3
Depth of Beams :	28.0 Inches	24.0 Inches
Width of Beams :	10.0 Inches	10.0 Inches
Tendons per Beam :	1	1
Beam Tendon Centroid :	2.25 Inches	2.25 Inches
Beam Spacing :	10.00 Feet O.C.	
Number of Slab Tendons :	5	
Slab Tendon Spacing :	9.00 Feet O.C.	
Slab Tendon Centroid :	2.25 Inches from top of slab	

In the SHORT direction ...

	<u>Type I Beam</u>	<u>Type II Beam</u>
Quantity of Beams :	2	6
Depth of Beams :	28.0 Inches	24.0 Inches
Width of Beams :	10.0 Inches	10.0 Inches
Tendons per Beam :	1	1
Beam Tendon Centroid :	2.25 Inches	2.25 Inches
Beam Spacing :	10.00 Feet O.C.	
Number of Slab Tendons :	8	
Slab Tendon Spacing :	9.43 Feet O.C.	
Slab Tendon Centroid :	2.25 Inches from top of slab	

Soil Properties

Allowable Bearing Pressure : 1,500.0 PSF

	<u>Center Lift</u>	<u>Edge Lift</u>
Edge Moisture Variation Distance, e_m :	6.70 Feet	3.50 Feet
Differential Soil Movement, y_m :	1.500 Inches	2.100 Inches

Load, Deflection and Subgrade Properties

Slab Loading

Uniform Superimposed Total Load : 40.00 PSF
 Total Perimeter Load : 1,200.00 PLF

Stiffness Coefficients

Center Lift : 480
 Edge Lift : 960

Prestress Calculation

Subgrade Friction calculated by method prescribed in PTI Manual

Prestress Loss : 15.0 KSI

Subgrade Friction Coefficient : 0.75

PTISlab 3.5 Analysis Parameters: Ribbed Foundation Analysis Model

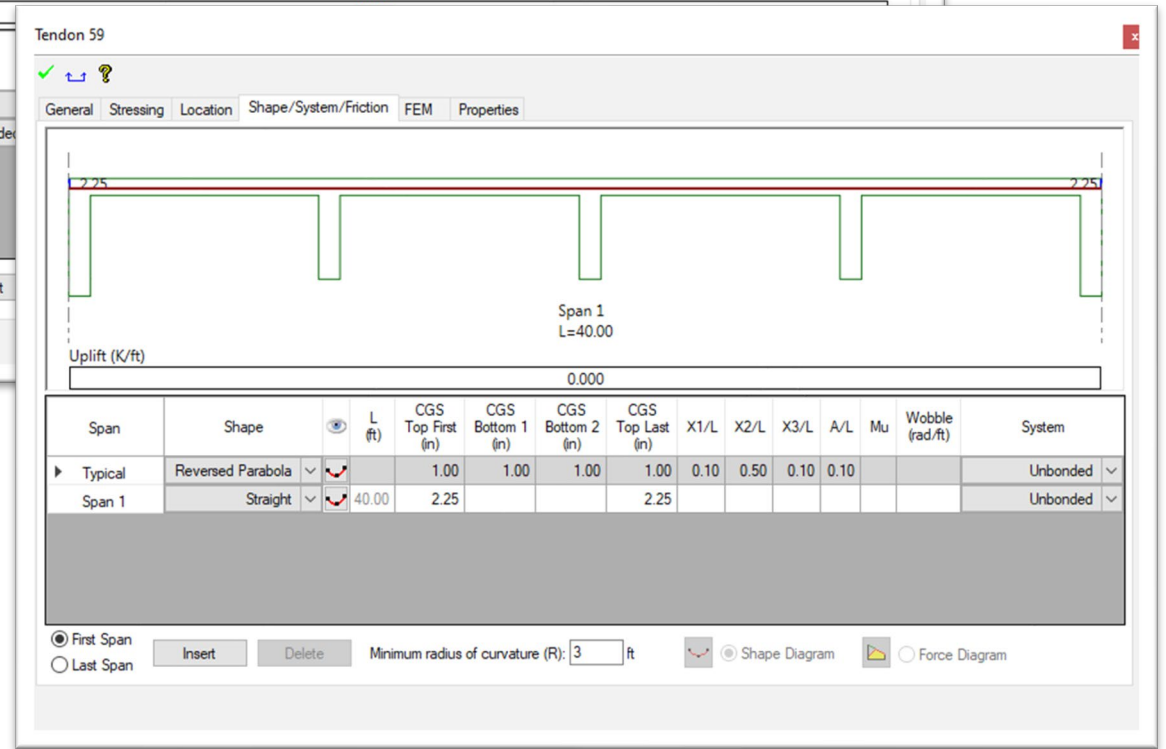
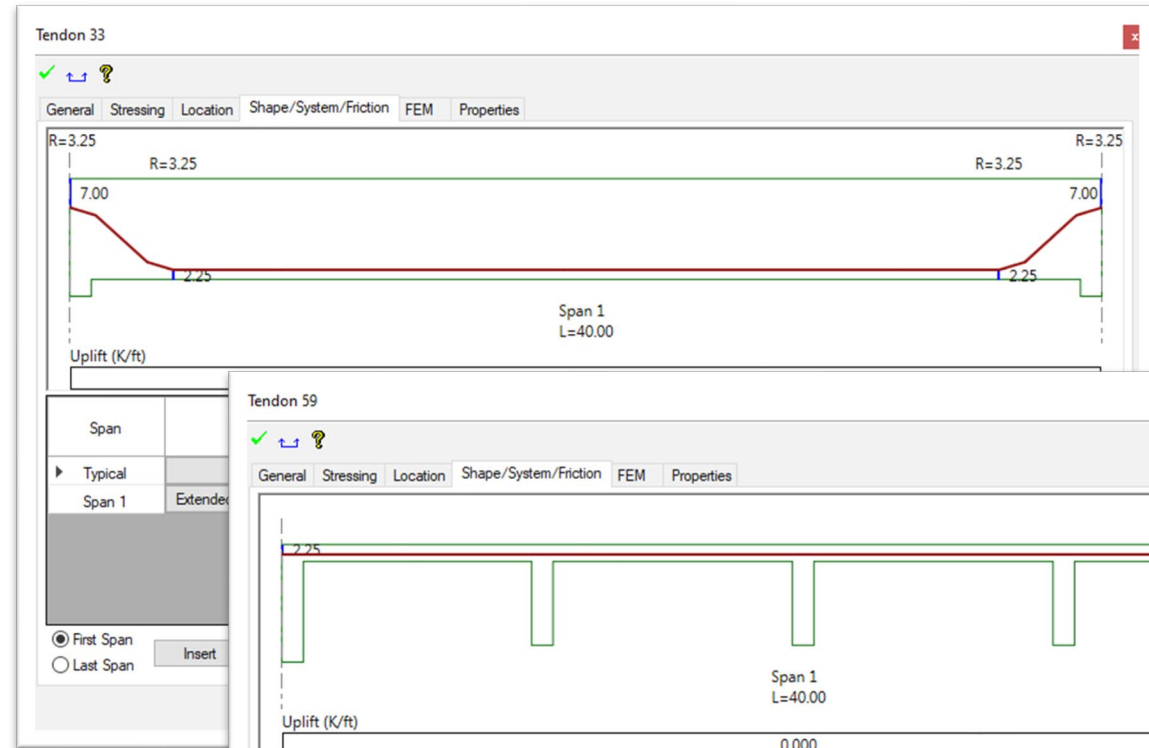
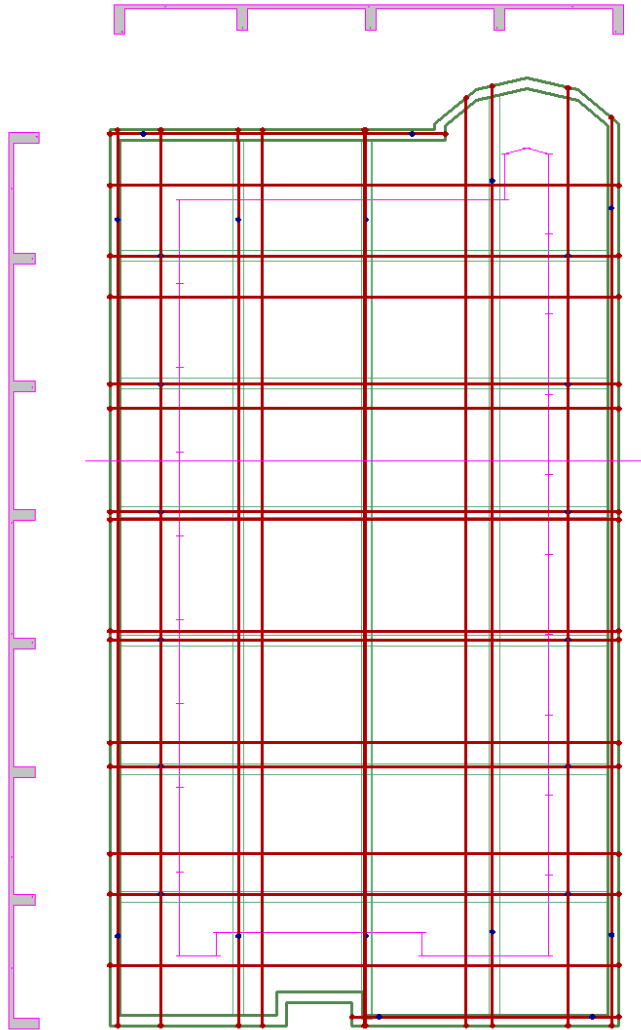
	Short Direction	Long Direction
Cross Sectional Area (Inch ²) :	5,053	3,010
Moment of Inertia (Inch ⁴) :	245,897	161,491
Section Modulus, Top (Inch ³) :	39,560	24,203
Section Modulus, Bottom (Inch ³) :	12,977	8,441
Center of Gravity of Concrete - from top (Inch) :	6.22	6.67
Center of Gravity of Prestressing Tendons - from top (Inch) :	12.58	12.90
Eccentricity of Prestress (Inch) :	-6.37	-6.23
Beta Distance (Feet) :	11.55	10.40
Equivalent Beam Depth (Inches) :	25.16	25.80

Note: All Calculations above and other reported values which depend on depths use the equivalent depths as shown above.

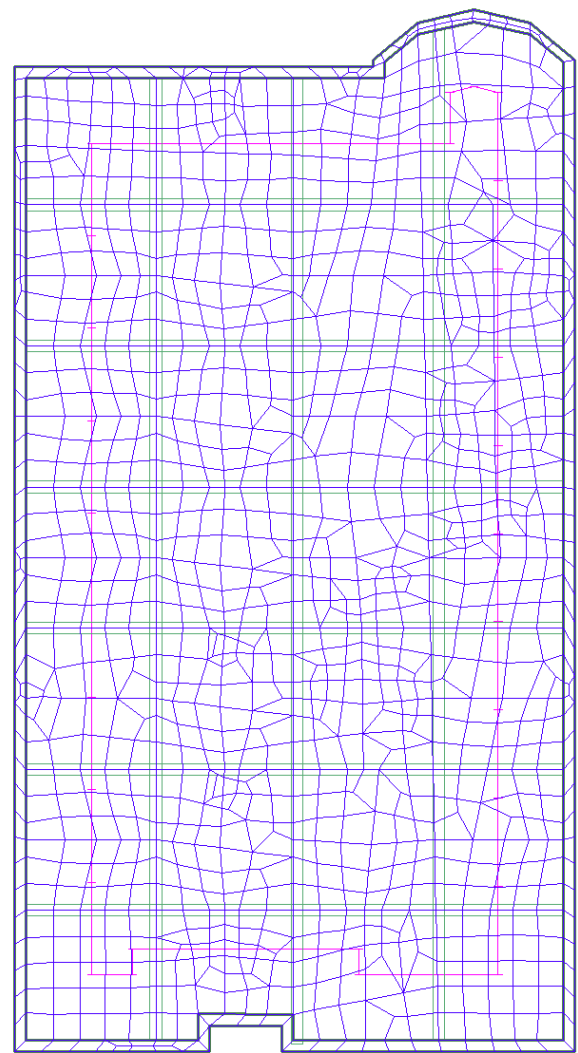
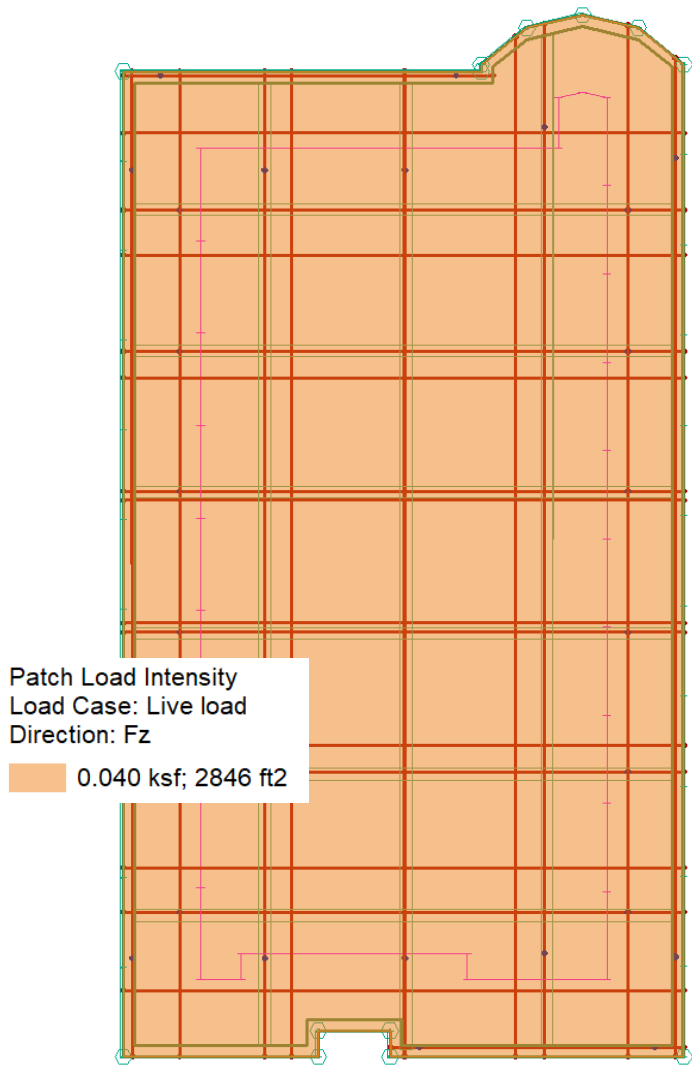
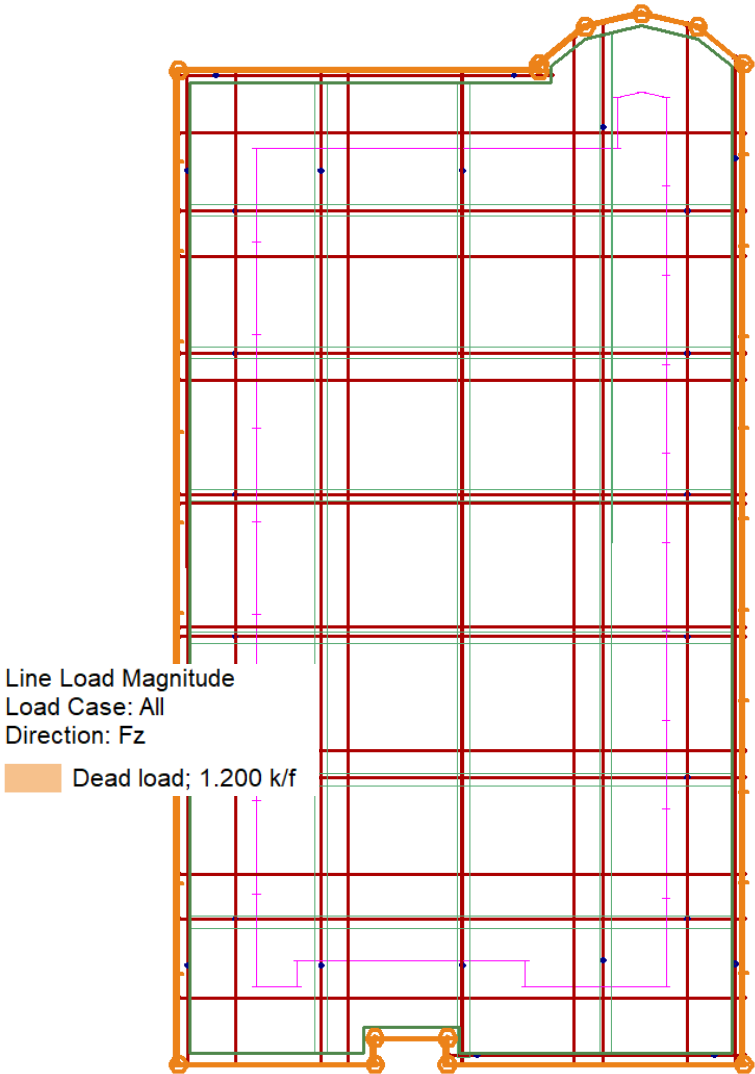
Jacking Force :

33.05 KIPS

3D Finite Element Ribbed Foundation Analysis Model



3D Finite Element Ribbed Foundation Analysis Model



PTISlab - Soil Bearing Analysis

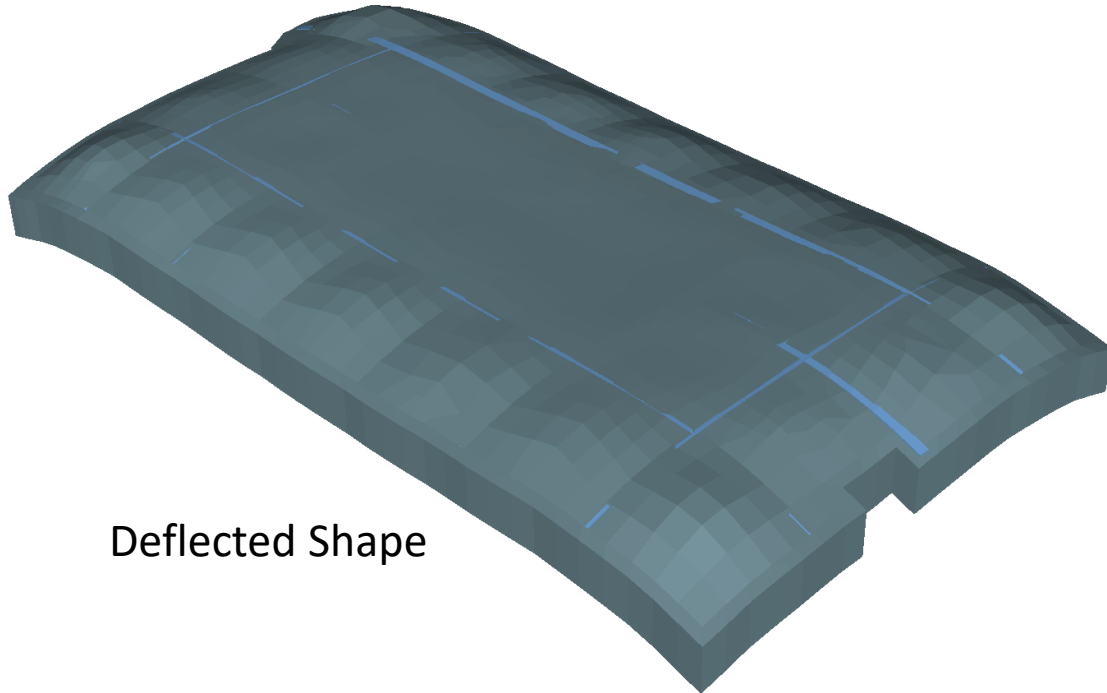
- Assumes uniform soil support
- Equally distributes all load to supporting soil
- Max pressure on soil 163 PSF << allowable 1,500 PSF

Soil Bearing Analysis

Total Applied Load	385,266 LB
Bearing Area	2,367 FT ²
Applied Pressure on Soil	163 PSF
Soil Pressure Safety Factor	0.00

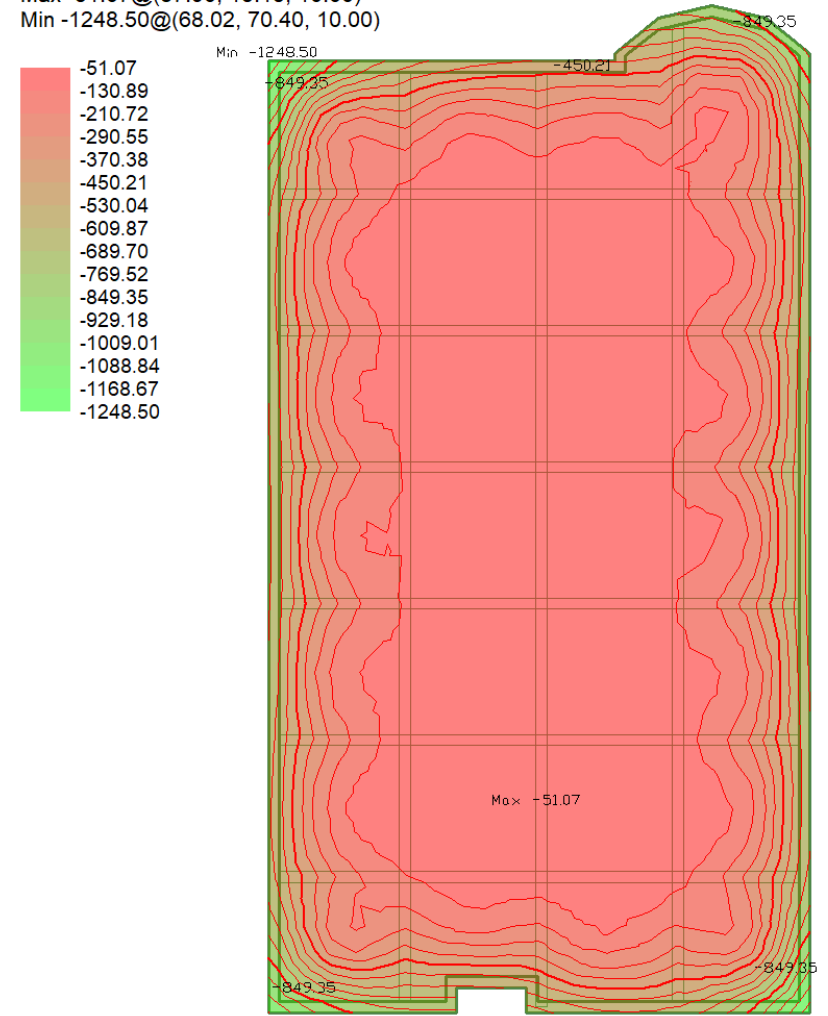
FEM - Soil Bearing Analysis

- Assumes uniform soil support
- Max pressure on soil 1,249 PSF < allowable 1,500 PSF



Deflected Shape

Slab, Stress (contour map), Soil pressure (Psf)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Max -51.07@(87.90, 15.15, 10.00)
Min -1248.50@(68.02, 70.40, 10.00)



PTISlab – Effective Prestress Calculations

- Effective PT force/tendon at Beta distance
 - Short direction
 - **22.93 kips**
 - Long direction
 - **23.58 kips**
- We assume the same valued in the FEM model

Prestress Summary

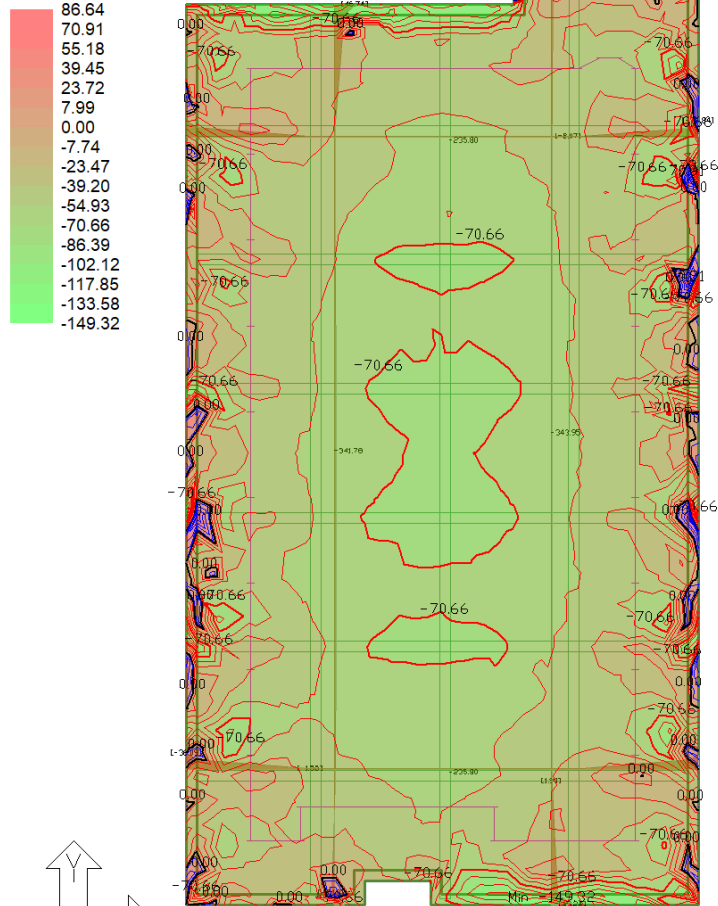
Subgrade Friction calculated by method prescribed in PTI Manual

	Short Direction	Long Direction
Number of Slab Tendons	8	5
Number of Beam Tendons	8	5
Spacing of Slab Tendons (Feet)	9.43	9.00
Center of Gravity of Concrete (from top of slab) (Inch)	6.22	6.67
Center of Gravity of Tendons (from top of slab) (Inch)	12.58	12.90
Eccentricity of Prestressing (Inch)	-6.37	-6.23
Minimum Effective Prestress Force (K)	323.5	163.7
Beta Distance Effective Prestress Force (K)	366.8	235.8
Minimum Effective Prestress (PSI)	64	54
Beta Distance Effective Prestress (PSI)	73	78

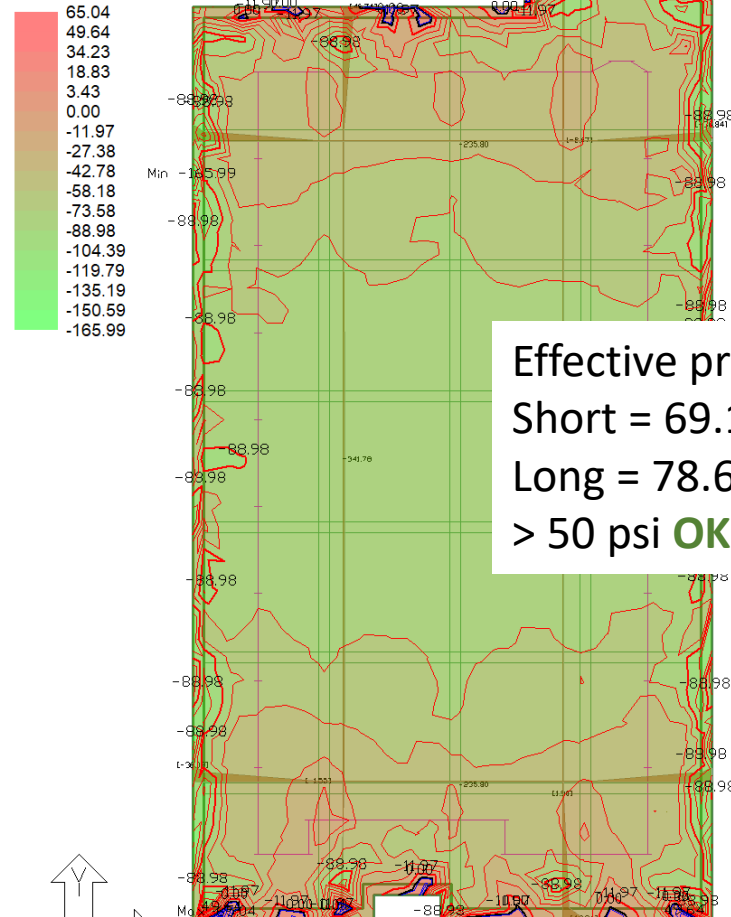
FEM – Effective Prestress Calculations

Exact same PT force applied to FEM model as in PTSlab.

Slab, Stress (contour map), Mid-depth along XX (Psi)
 Load Combination: Effective PT (NO_CODE_CHECK)
 Max 86.64@(93.57, 70.90, 10.00)
 Min -149.32@(96.65, 0.02, 10.00)

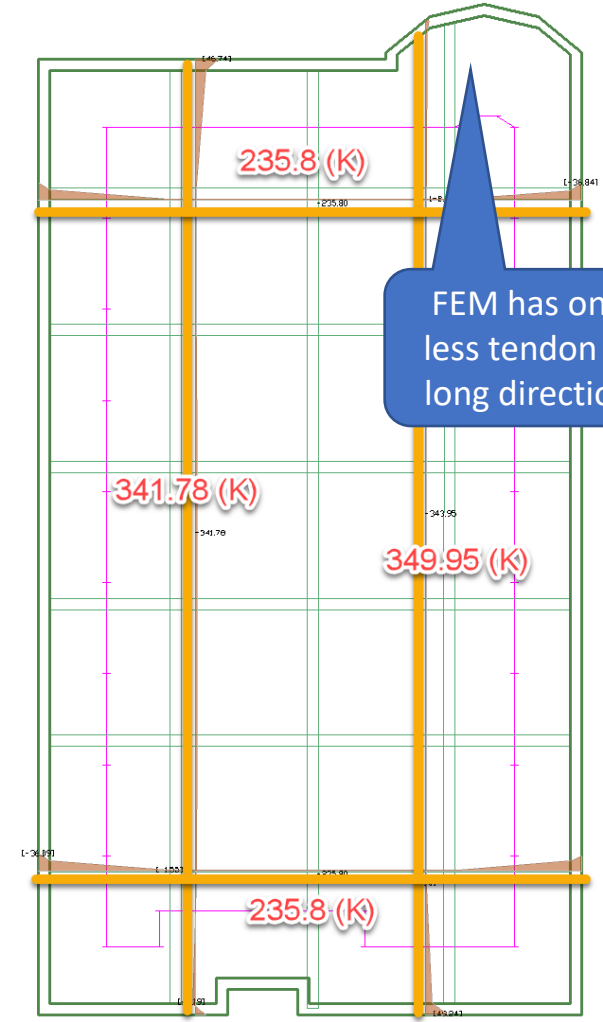


Slab, Stress (contour map), Mid-depth along YY (Psi)
 Load Combination: Effective PT (NO_CODE_CHECK)
 Max 65.04@(69.94, 0.02, 10.00)
 Min -165.99@(68.02, 56.95, 10.00)

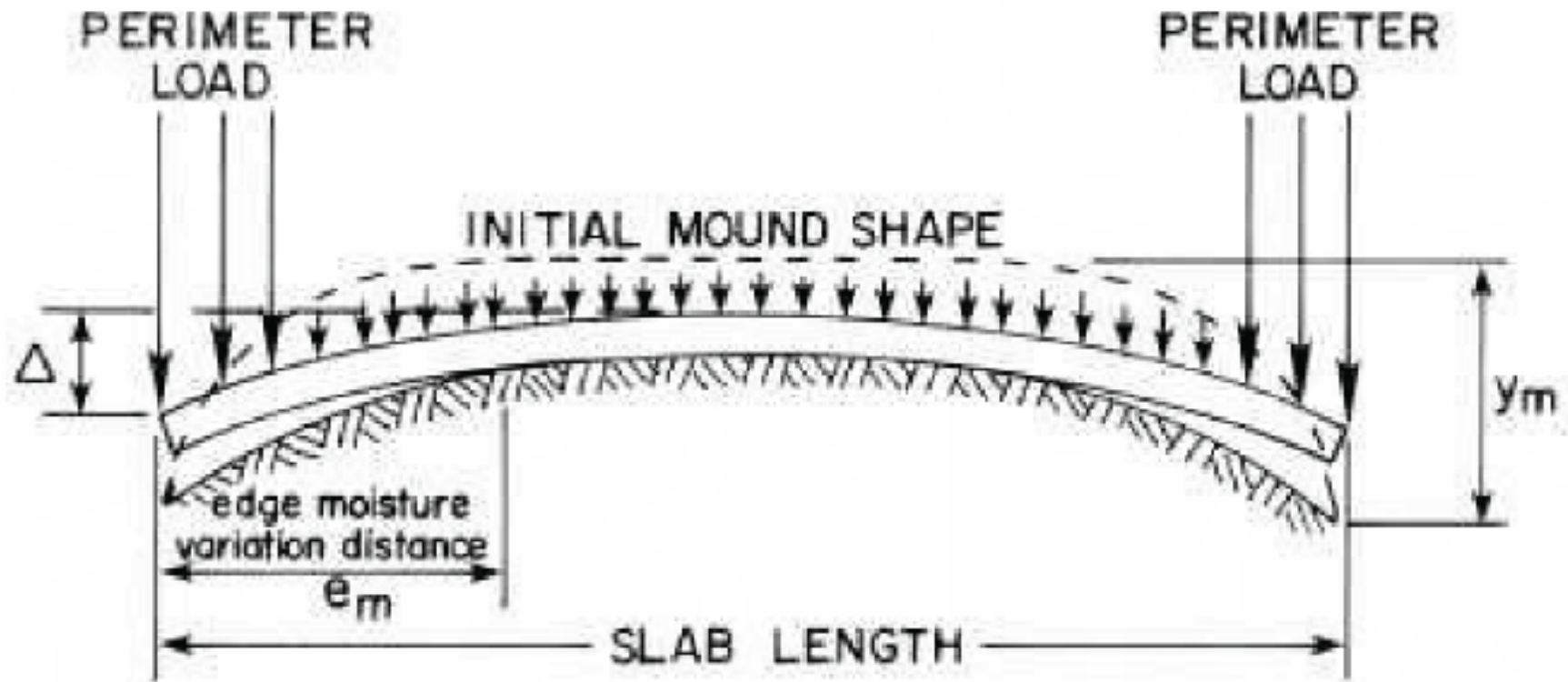


Effective prestress:
 Short = 69.16 psi
 Long = 78.6 psi
 > 50 psi **OK**

Manual Design Sections, Actions, Axial (Kip)
 Load Combination: Effective PT (NO_CODE_CHECK)
 Tension positive
 Max: -235.80
 Min: -343.95



Center Lift Mode



PTI Figure 3.5

PTISlab – Moment Analysis – Center Lift Mode

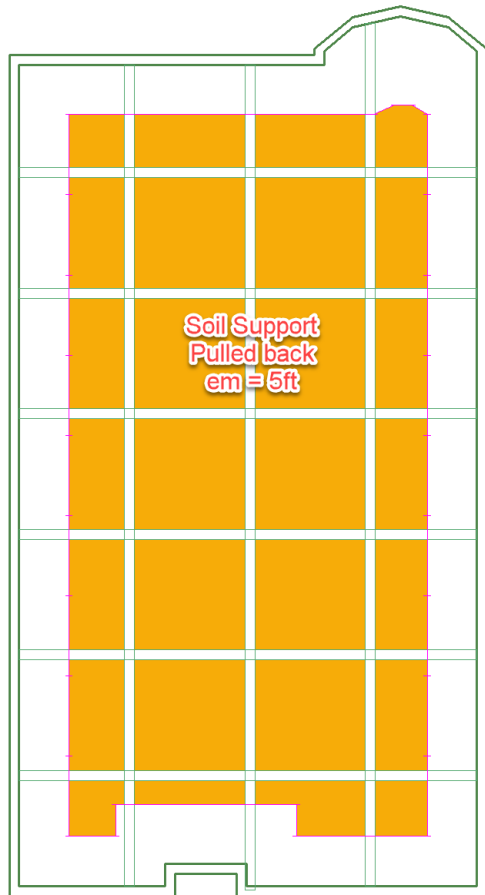
Moment Analysis - Center Lift Mode

Maximum Moment, Short Dir. (calculated with $E_m=5.0$ per PTI 4.3.2) 10.10 FT-K/FT
 Maximum Moment, Long Dir. (calculated with $E_m=5.0$ per PTI 4.3.2) 9.62 FT-K/FT

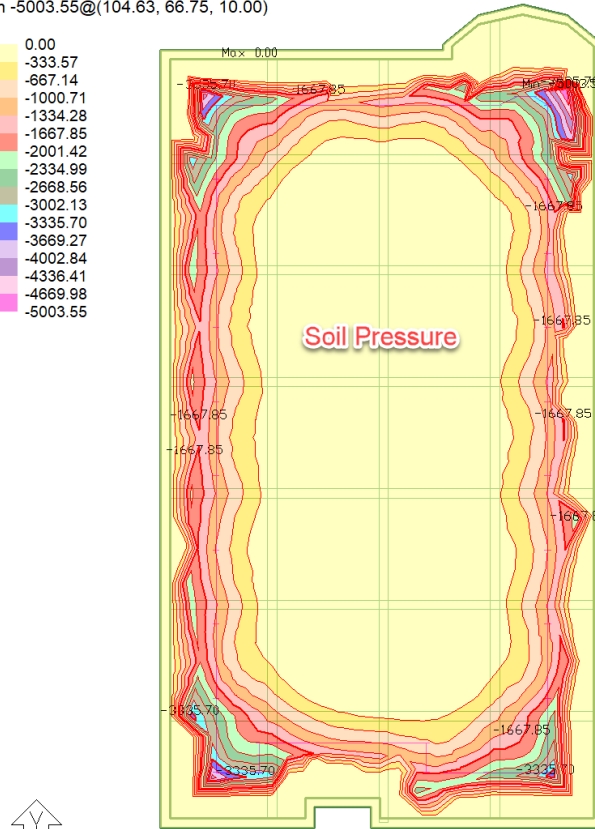
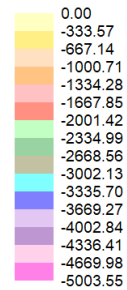
	Tension in Top Fiber (KSI)		Compression in Bottom Fiber (KSI)	
	Short Direction	Long Direction	Short Direction	Long Direction
Allowable Stress	-0.379	-0.379	Allowable Stress	1.800
Actual Stress	-0.167	-0.150	Actual Stress	0.307

FEM– Center Lift Mode – Analysis Method

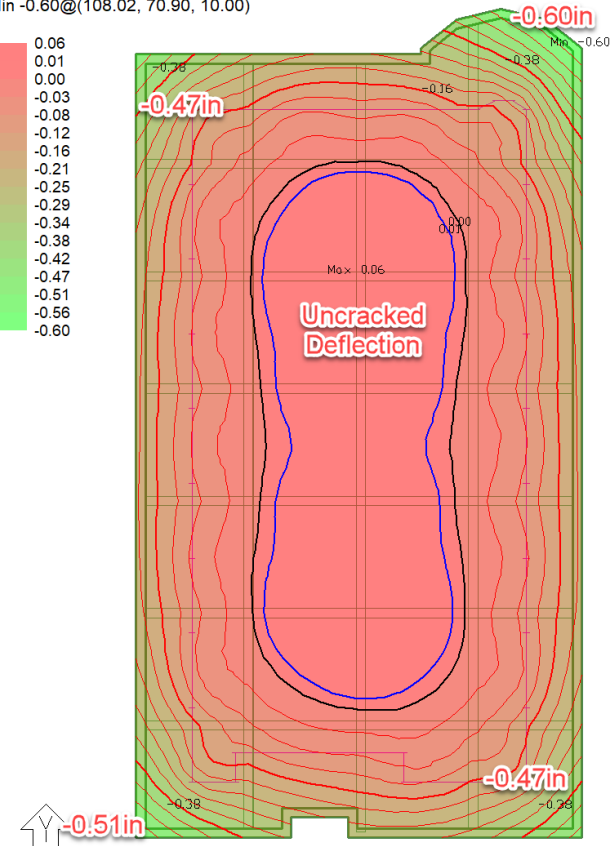
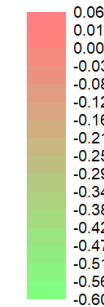
To simulate Center Lift Mode, soil support is removed the distance of em (5ft) from perimeter of slab.



Slab, Stress (contour map), Soil pressure (Psf)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Max 0.00@(76.18, 69.56, 10.00)
Min -5003.55@(104.63, 66.75, 10.00)

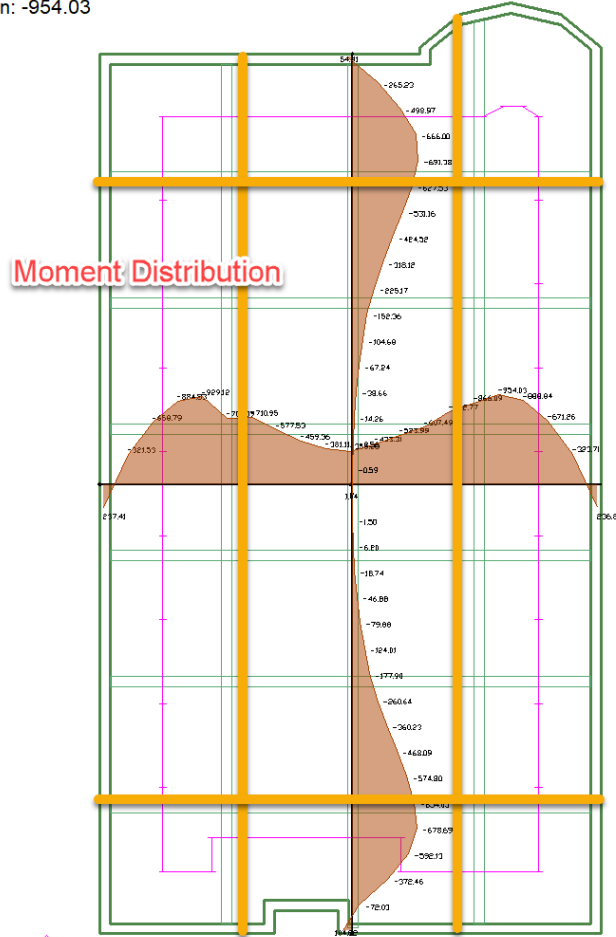


Slab, Deformation, Z-Translation (in)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Max 0.06@(87.92, 50.45, 10.00)
Min -0.60@(108.02, 70.90, 10.00)

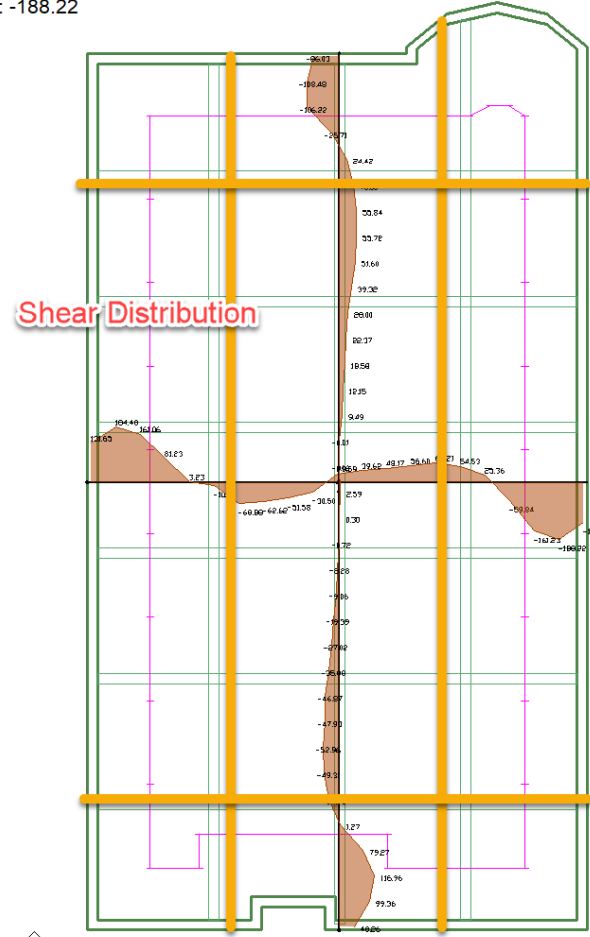


FEM – Moment Analysis – Center Lift Mode

Design Sections, Actions, Bending (Kip-ft)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Max: 237.41
Min: -954.03



Design Sections, Actions, Shear (Kip)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Max: 184.48
Min: -188.22

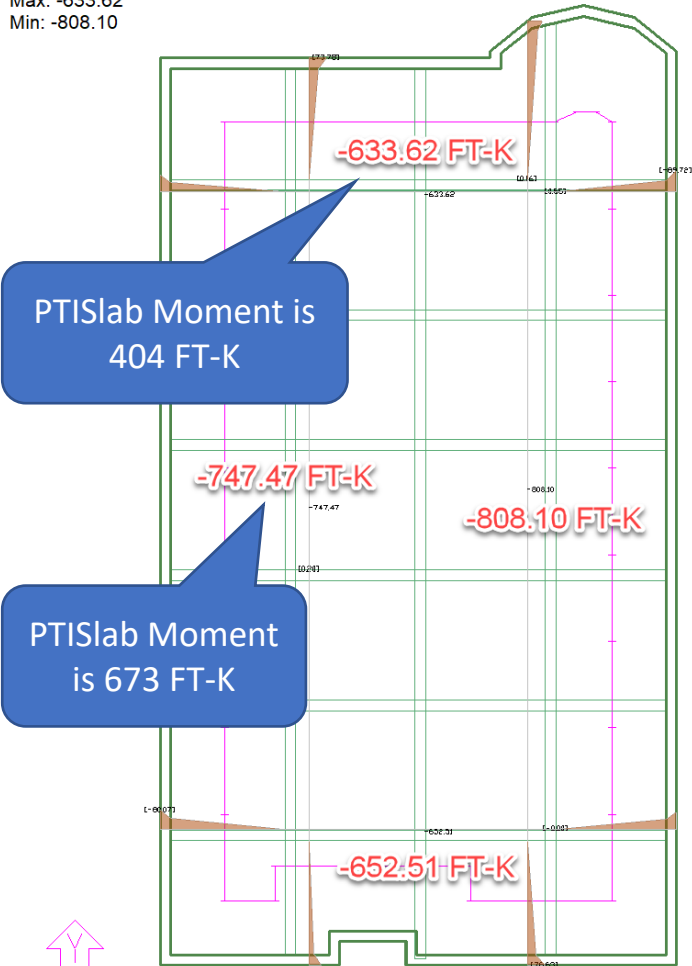


Maximum moments and shears don't coincide with Beta distance.

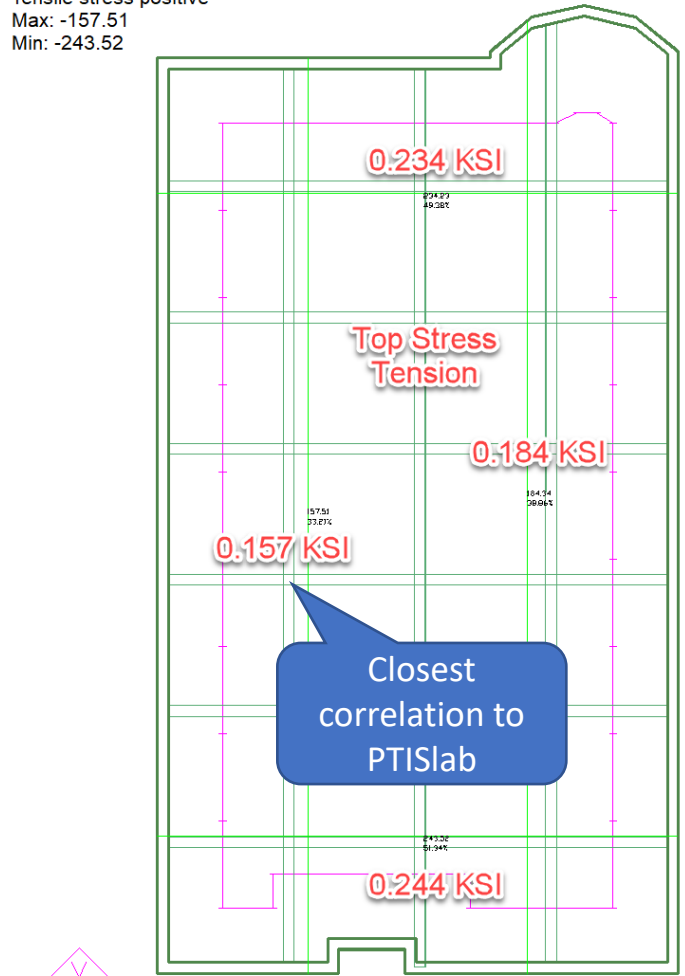
FEM – Moment Analysis @ Beta – Center Lift Mode

Stresses @ beta distance pass.

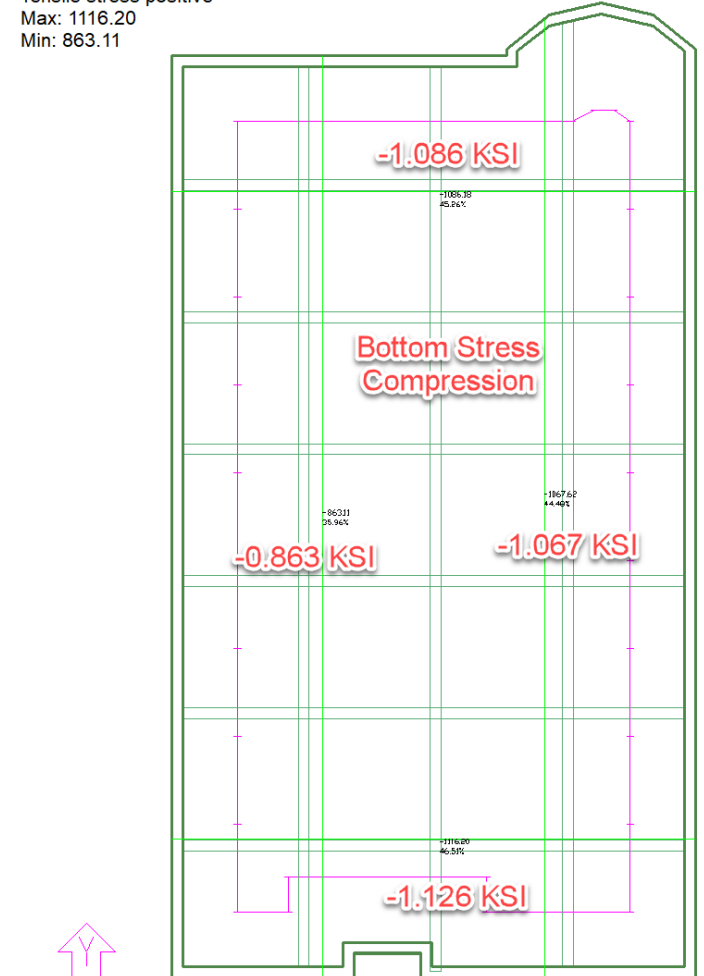
Manual Design Sections, Actions, Bending (Kip-ft)
 Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
 Max: -633.62
 Min: -808.10



Manual Design Sections, Stresses, Top (Psi)
 Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
 Tensile stress positive
 Max: -157.51
 Min: -243.52

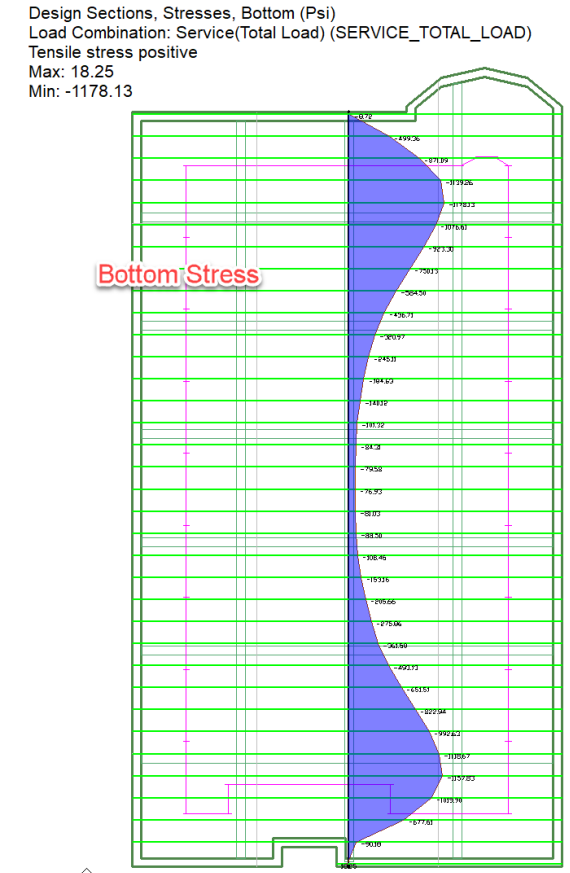
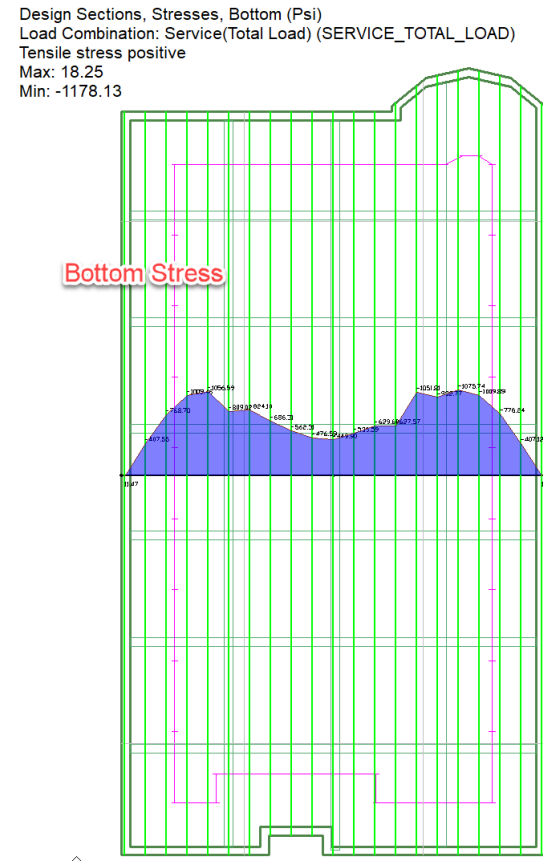
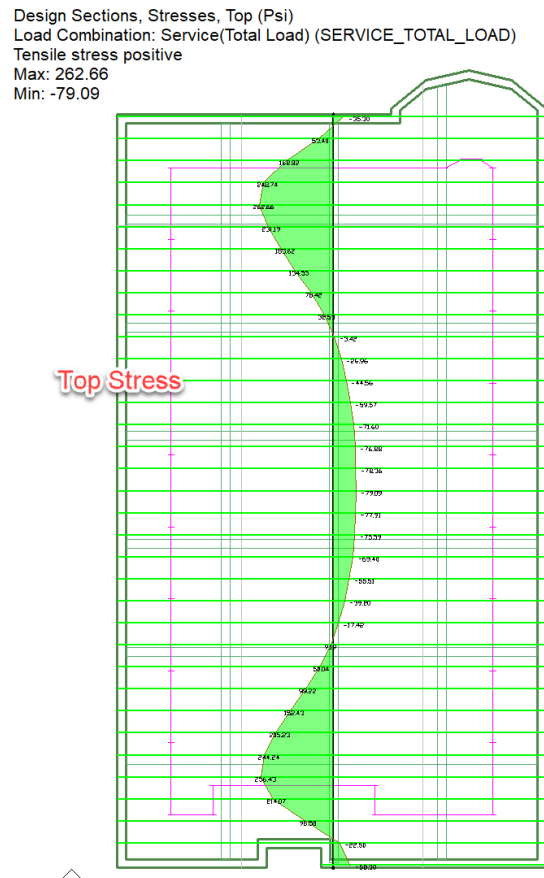
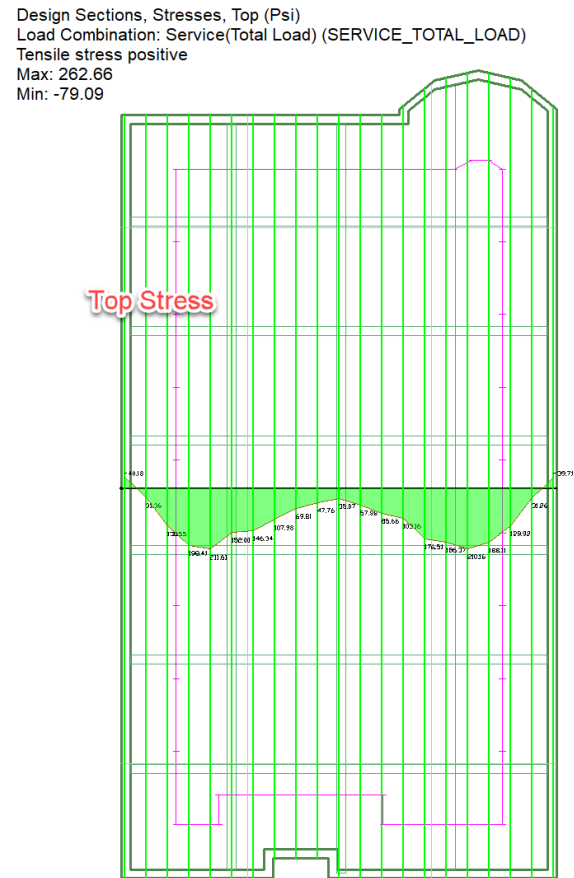


Manual Design Sections, Stresses, Bottom (Psi)
 Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
 Tensile stress positive
 Max: 1116.20
 Min: 863.11



FEM – Moment Analysis @ All Sections – Center Lift Mode

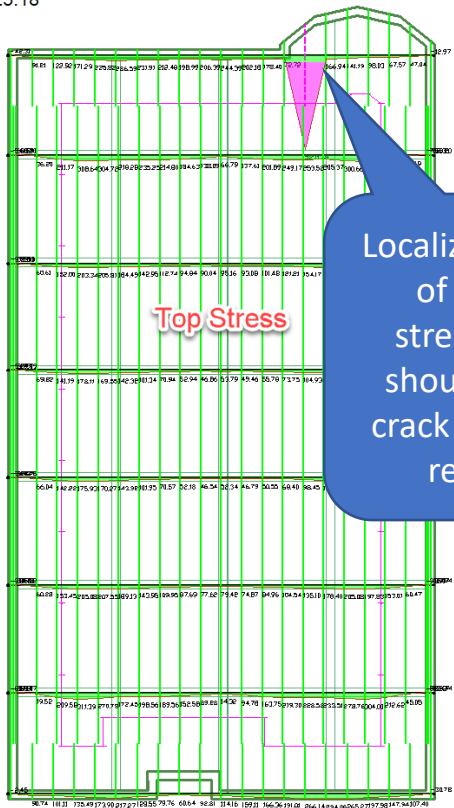
All slab stresses are within allowable limits if integrated over entire slab width.



FEM – Moment Analysis @ Detailed – Center Lift Mode

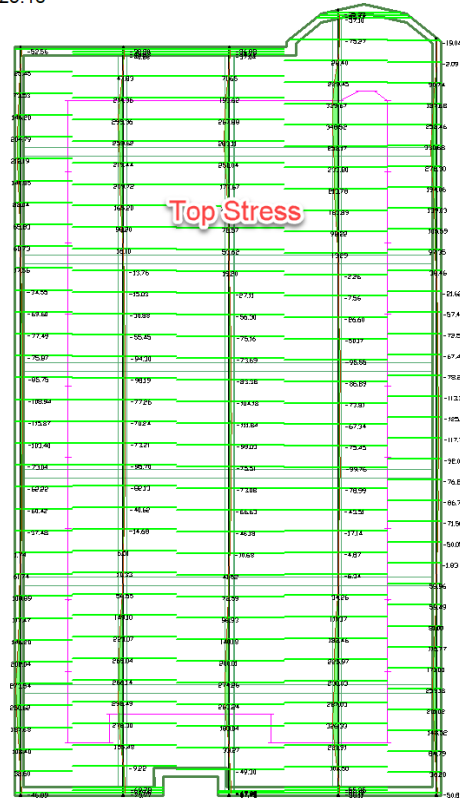
FEM can provide more detailed and localized stress distribution, a useful guide for added rebar placement.

Design Sections, Stresses, Top (Psi)
 Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
 Tensile stress positive
 Max: 5231.48
 Min: -125.18



Localized area of high stresses – should add crack control rebar

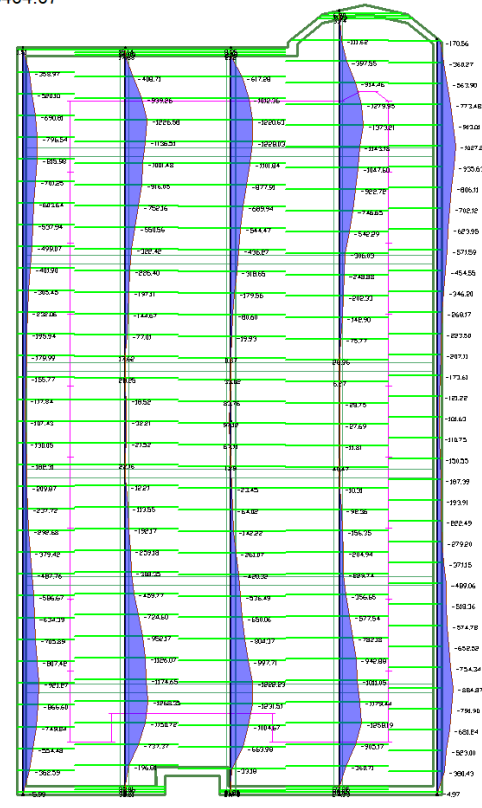
Design Sections, Stresses, Top (Psi)
 Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
 Tensile stress positive
 Max: 5231.48
 Min: -125.18



Design Sections, Stresses, Bottom (Psi)
 Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
 Tensile stress positive
 Max: 97.12
 Min: -5404.07



Design Sections, Stresses, Bottom (Psi)
 Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
 Tensile stress positive
 Max: 97.12
 Min: -5404.07



PTISlab – Stiffness Analysis – Center Lift Mode

Stiffness Analysis - Center Lift Mode

Based on a Stiffness Coefficient of 480

Available Moment of Inertia (Inch⁴)
Required Moment of Inertia (Inch⁴)
Required Moment of Inertia controlled by

Short Direction	Long Direction
245,897	161,491
108,632	92,193
Width	6*Beta

FEM – Stiffness Analysis – Based on I – Center Lift Mode

Design Section

General Location/Mechanical Properties Design Sections Other Properties

Mechanical properties

Cross-sectional area	5.06e+03 in ²
Moment of inertia	2.46e+05 in ⁴
Distance of centroid to top fiber	6.17e+00 in
Distance of centroid to bottom fiber	2.18e+01 in
Coordinates of centroid	x=9.55e+02 in y=4.23e+02 in
Length	8.44e+02 in

Short Direction

Short direction:

- Required 108,632 (in⁴)
- Available 246,000 (in⁴)
- **OK**

Long direction:

- Required 92,193 (in⁴)
- Available 161,000 (in⁴)
- **OK**

Design Section

General Location/Mechanical Properties Design Sections Other Properties

Mechanical properties

Cross-sectional area	3.00e+03 in ²
Moment of inertia	1.61e+05 in ⁴
Distance of centroid to top fiber	6.63e+00 in
Distance of centroid to bottom fiber	2.14e+01 in
Coordinates of centroid	x=1.06e+03 in y=7.20e+02 in
Length	4.80e+02 in

Long Direction

Design Section Zoom

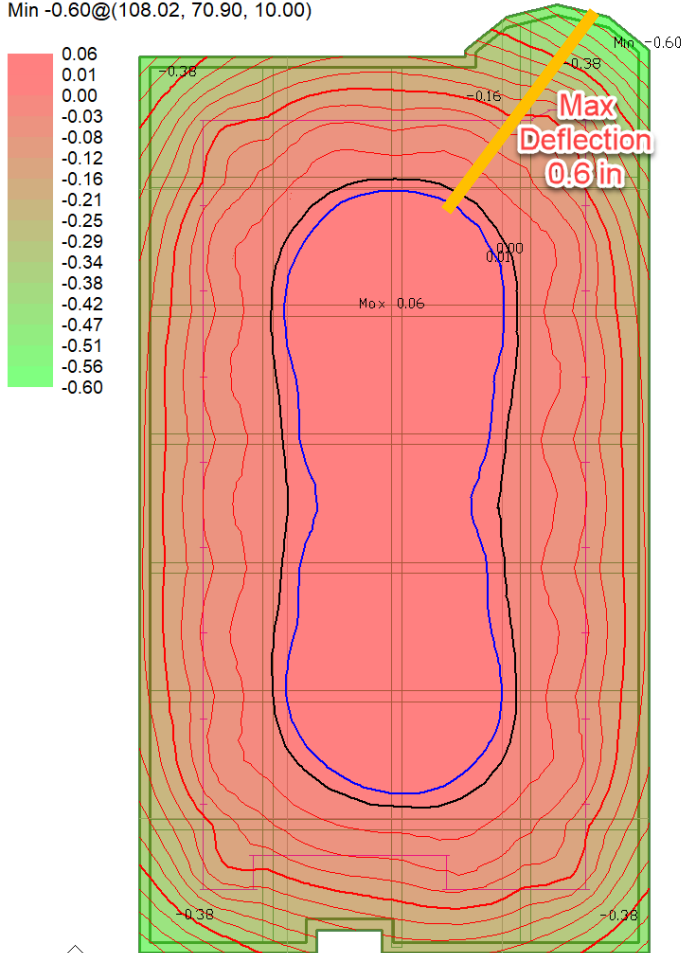
OK

Design Section Zoom

OK

FEM – Stiffness Analysis – Based on Deflection – Center Lift Mode

Slab, Deformation, Z-Translation (in)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Max 0.06@(87.92, 50.45, 10.00)
Min -0.60@(108.02, 70.90, 10.00)



Can use actual deflection to check deflection criteria.

- Stiffness coefficient 480
- Max allowable deflection 0.9 in
(based on 18 ft cantilever deflection)
- Max deflection 0.6 in **OK**

PTISlab – Shear Analysis – Center Lift Mode

Shear Analysis - Center Lift Mode

Maximum Shear, Short Direction
Maximum Shear, Long Direction

2.37 K/FT

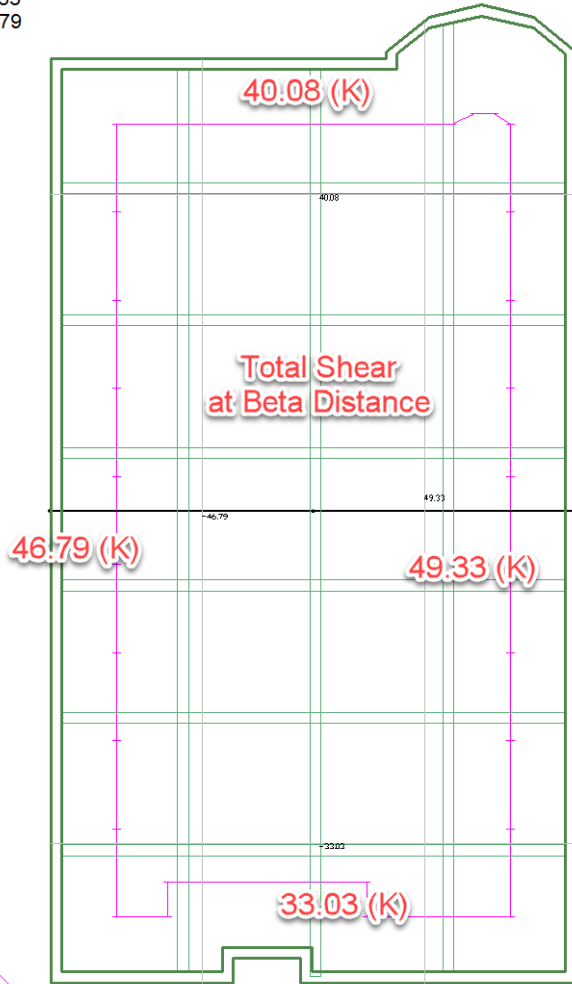
2.22 K/FT

Allowable Shear Stress (PSI)
Actual Shear Stress (PSI)

	Short Direction	Long Direction
	166	167
	12	12

FEM – Shear Analysis – Center Lift Mode

Manual Design Sections, Actions, Shear (Kip)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Max: 49.33
Min: -46.79



Allowable shear stress:

- Short direction 165 psi
- Long direction 167 psi

Max shear capacity:

- Short direction 331 K
- Long direction 214 K

Shear @ Beta

- Short direction 47 K **OK**
- Long direction 41 K **OK**

Max shear demand

- Short direction 188 K **OK**
- Long direction 117 K **OK**

PTISlab – Cracked Section Analysis – Center Lift Mode

Cracked Section Analysis - Center Lift Mode

Cracked Section Capacity (FT-K)
0.5 Moment (FT-K)

Short Direction	Long Direction
399.7	256.9
353.6	192.4

FEM – Cracked Section Analysis – Center Lift Mode

Short direction:

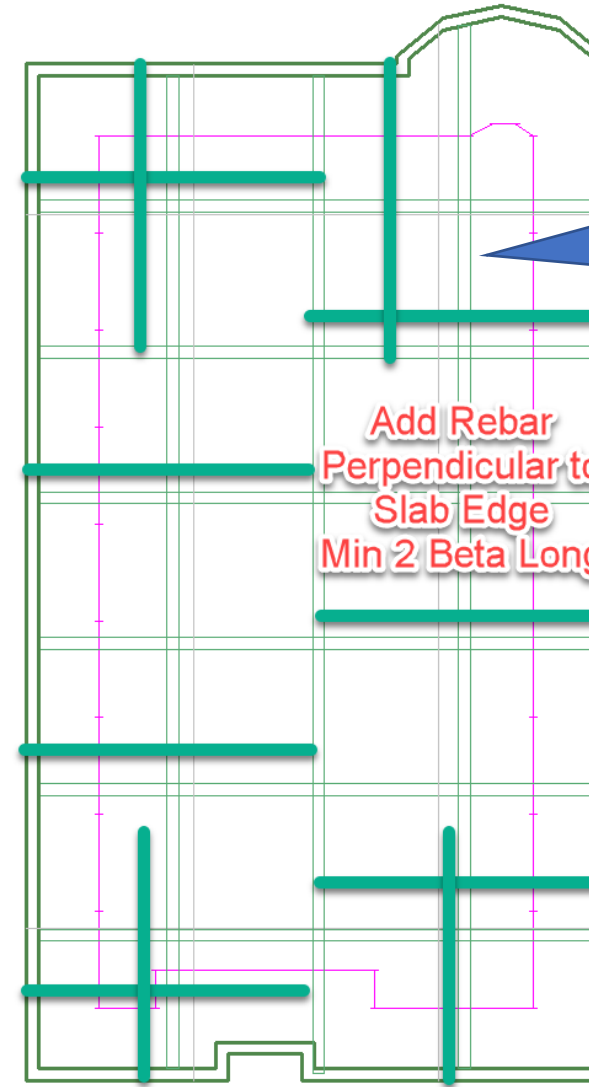
Design section moment capacity	
Positive moment	400.20 k-ft
Negative moment	-387.74 k-ft

0.5 M @ Beta	404 K-FT NG
0.5 M Max	477 K-FT NG

Long direction:

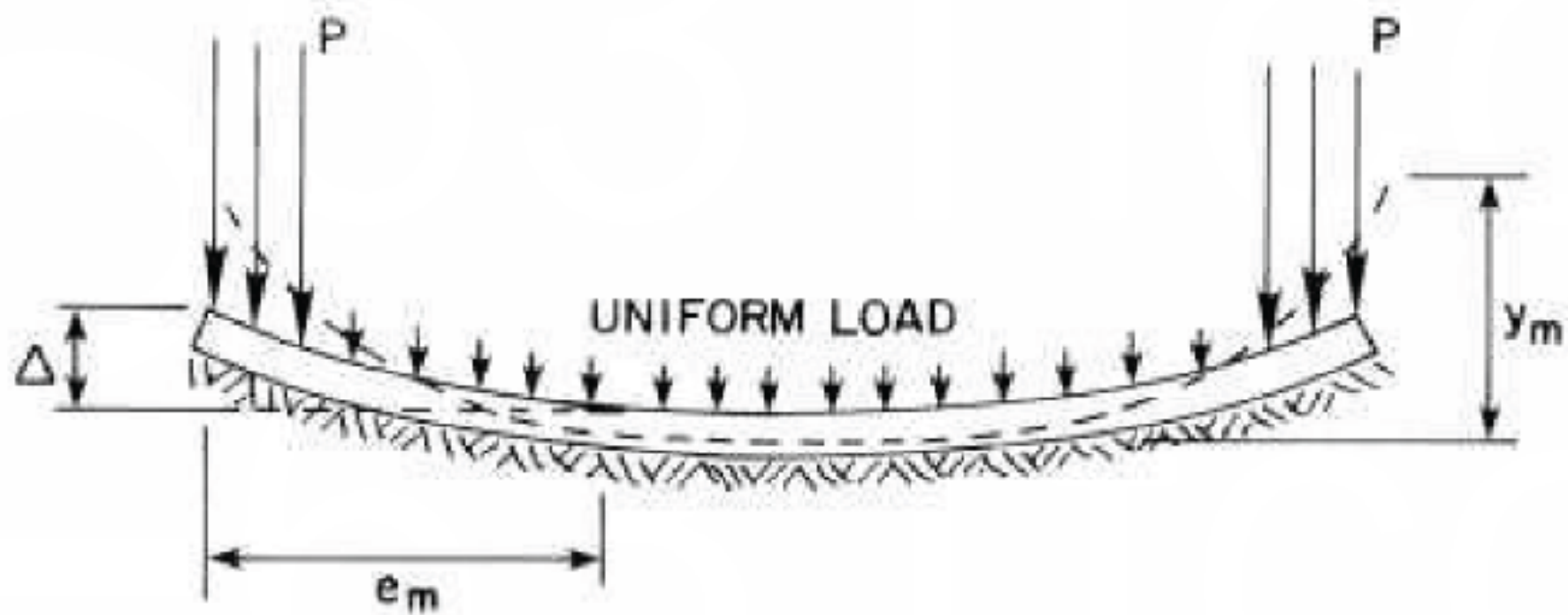
Design section moment capacity	
Positive moment	299.97 k-ft
Negative moment	-548.30 k-ft

0.5 M @ Beta	327 K-FT NG
0.5 M Max	345 K-FT NG



To meet PTI 6.9, add rebar or increase PT

Edge Lift Mode



PTI Figure 3.5

PTISlab – Moment Analysis – Edge Lift Mode

Moment Analysis - Edge Lift Mode

Maximum Moment, Short Direction

8.44 FT-K/FT

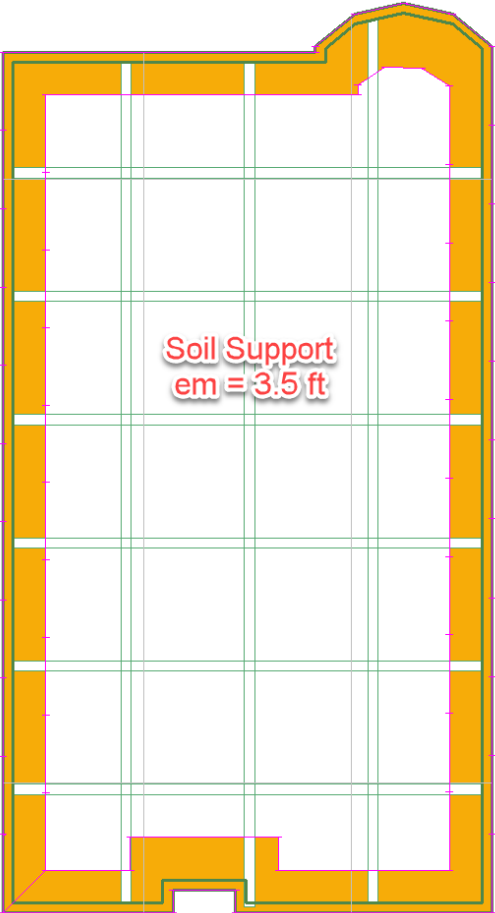
Maximum Moment, Long Direction

7.01 FT-K/FT

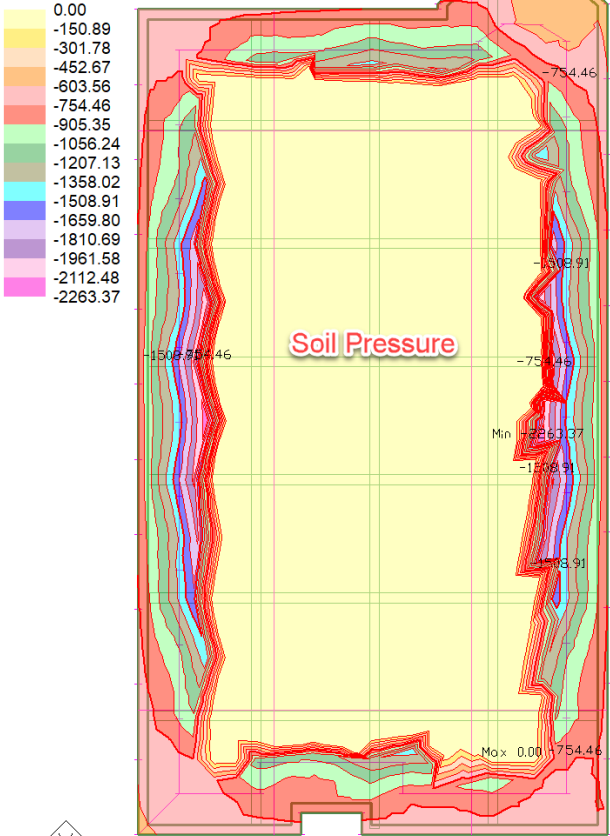
	Tension in Bottom Fiber (KSI)			Compression in Top Fiber (KSI)	
	Short Direction	Long Direction		Short Direction	Long Direction
Allowable Stress	-0.379	-0.379	Allowable Stress	1.800	1.800
Actual Stress	-0.294	-0.146	Actual Stress	0.193	0.157

FEM– Edge Lift Mode – Analysis Method

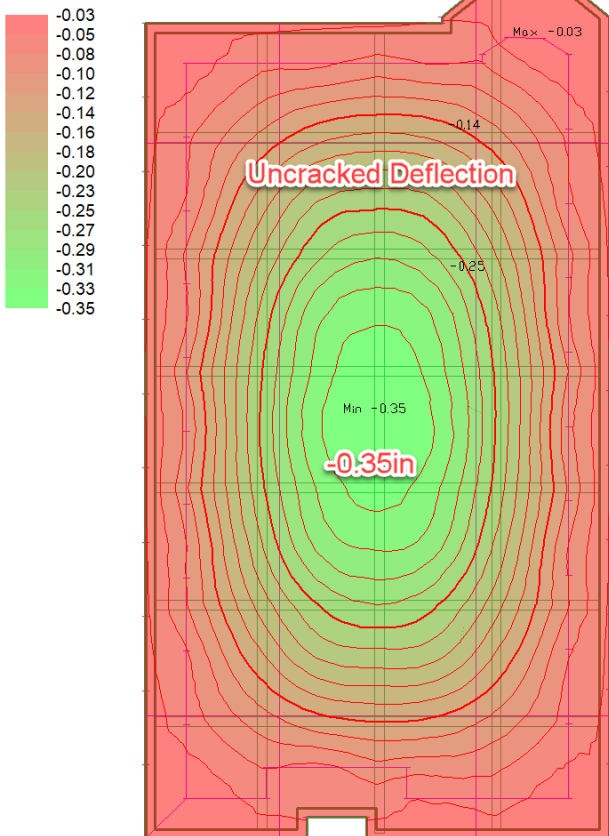
To simulate Edge Lift Mode, heaving soil support is limited to outer distance em (3ft) from perimeter of slab.



Slab, Stress (contour map), Soil pressure (Psf)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Max 0.00@(99.99, 6.46, 10.00)
Min -2263.37@(102.25, 33.61, 10.00)



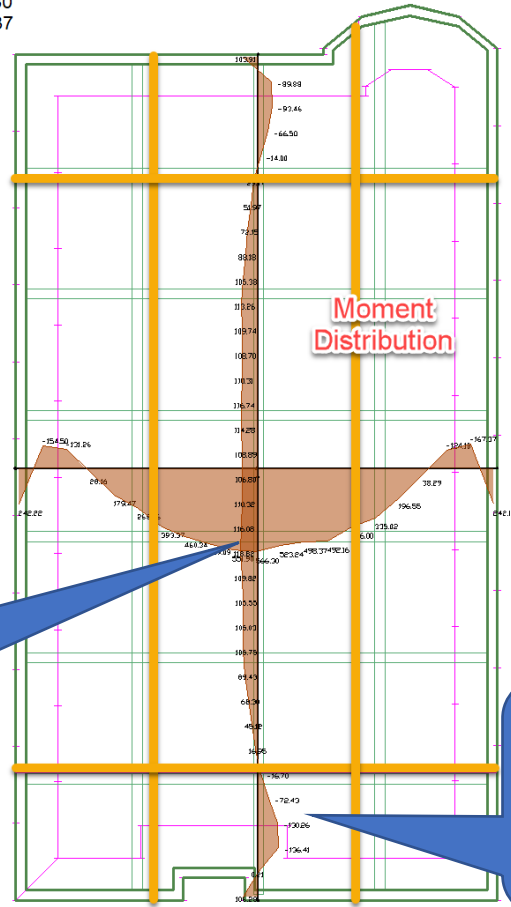
Slab, Deformation, Z-Translation (in)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Max -0.03@(102.79, 69.02, 10.00)
Min -0.35@(87.91, 36.52, 10.00)



FEM – Moment Analysis – Edge Lift Mode

Maximum moments and shears don't coincide with Beta distance.

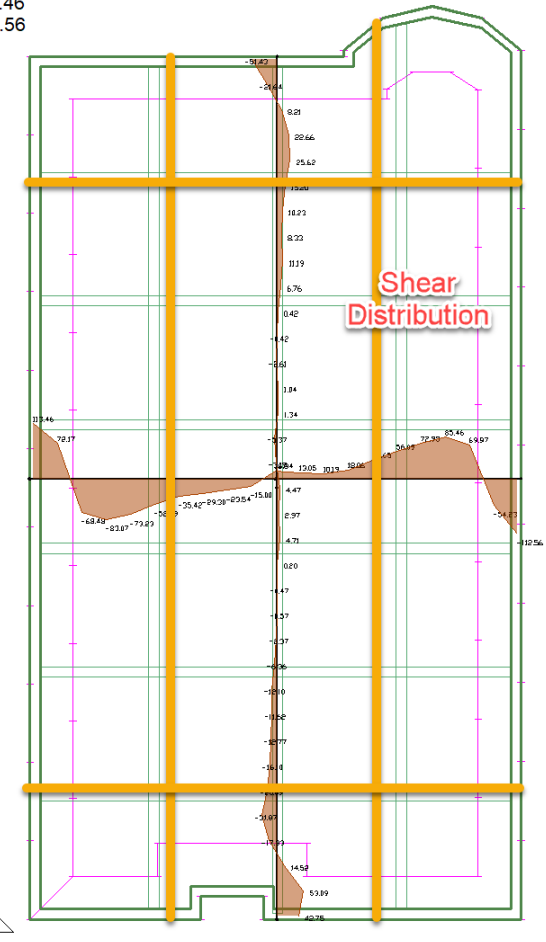
Design Sections, Actions, Bending (Kip-ft)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Max: 566.30
Min: -167.37



FEM Max value is 566.3
PTI value is 590.8

FEM Max value is 130.3
PTI value is 280.4

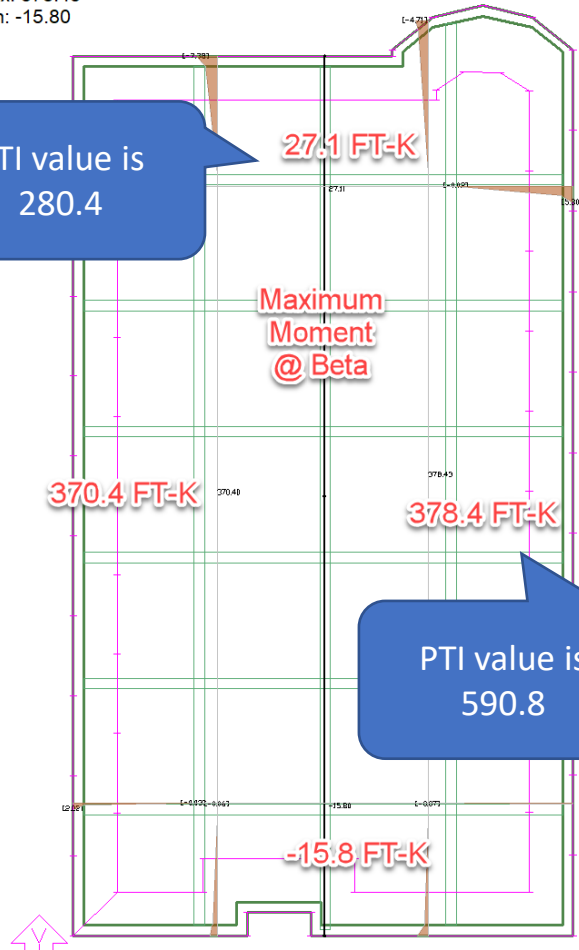
Design Sections, Actions, Shear (Kip)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Max: 113.46
Min: -112.56



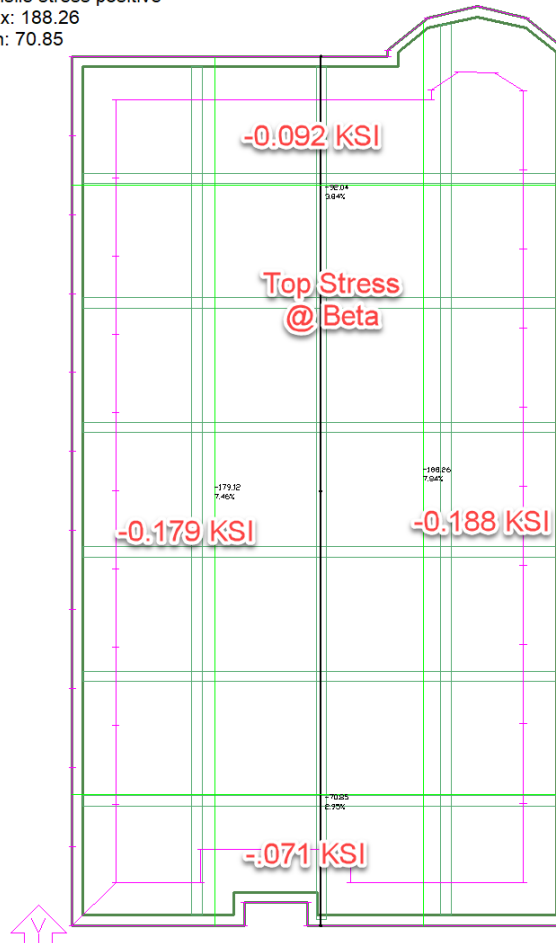
FEM – Moment Analysis @ Beta – Edge Lift Mode

Stresses @ beta distance pass.

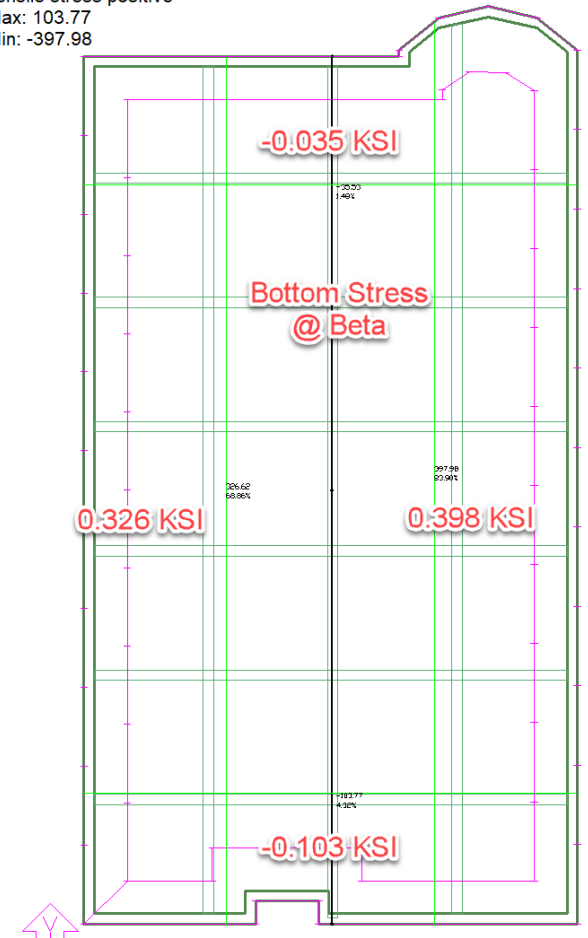
Manual Design Sections, Actions, Bending (Kip-ft)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Max: 378.43
Min: -15.80



Manual Design Sections, Stresses, Top (Psi)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Tensile stress positive
Max: 188.26
Min: 70.85



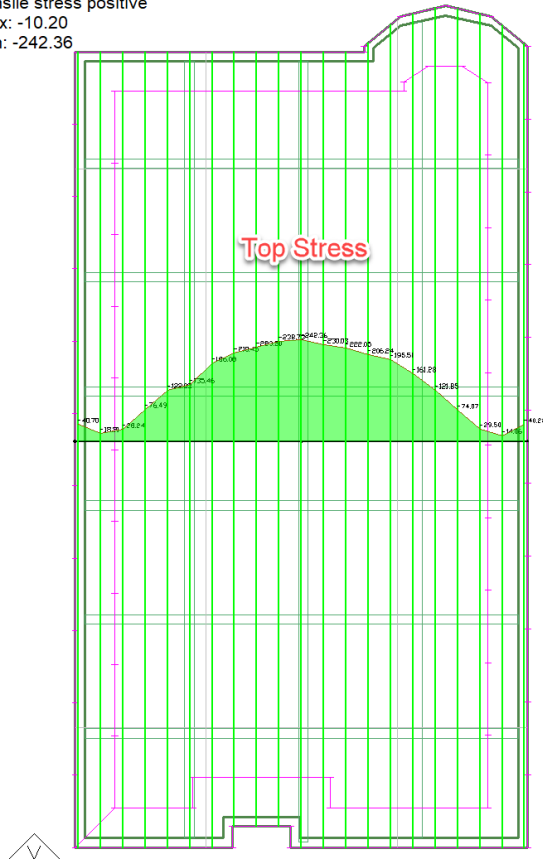
Manual Design Sections, Stresses, Bottom (Psi)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Tensile stress positive
Max: 103.77
Min: -397.98



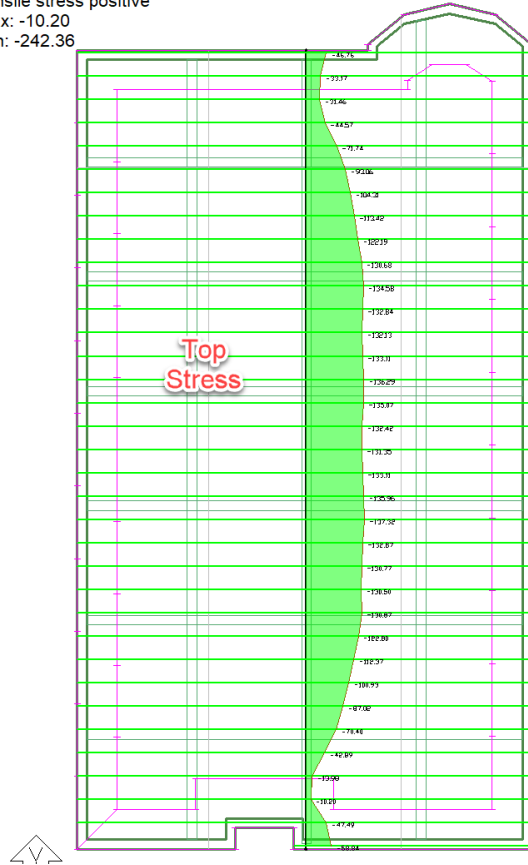
FEM – Moment Analysis @ All Sections – Edge Lift Mode

When checking stress distribution in slab, short direction bottom stresses in beams **exceed** cracking stress.

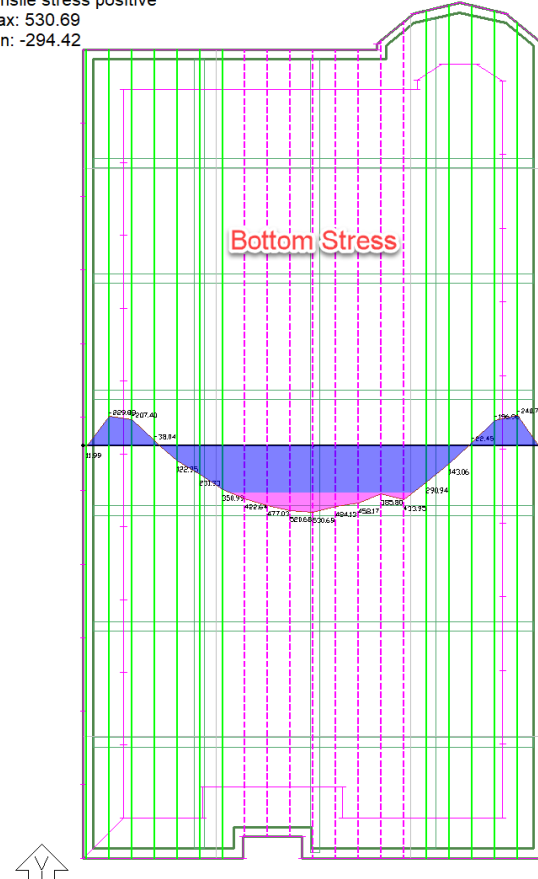
Design Sections, Stresses, Top (Psi)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Tensile stress positive
Max: -10.20
Min: -242.36



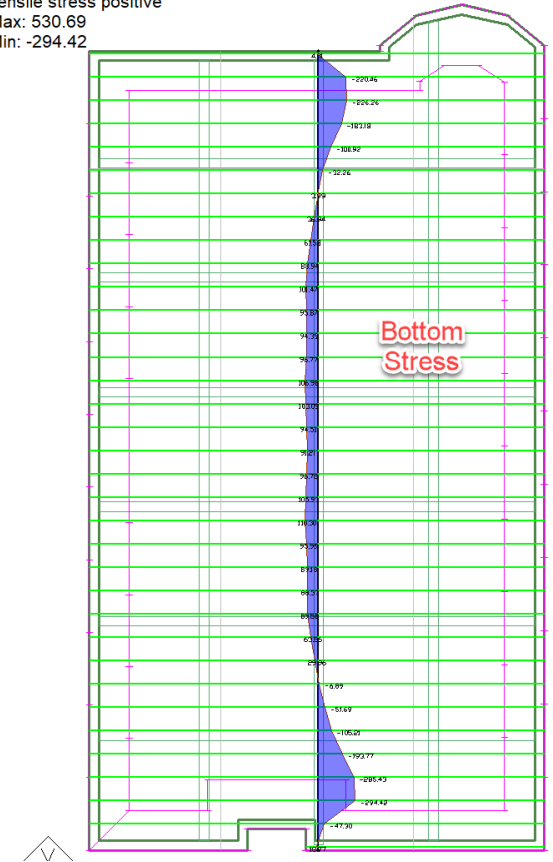
Design Sections, Stresses, Top (Psi)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Tensile stress positive
Max: -10.20
Min: -242.36



Design Sections, Stresses, Bottom (Psi)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Tensile stress positive
Max: 530.69
Min: -294.42



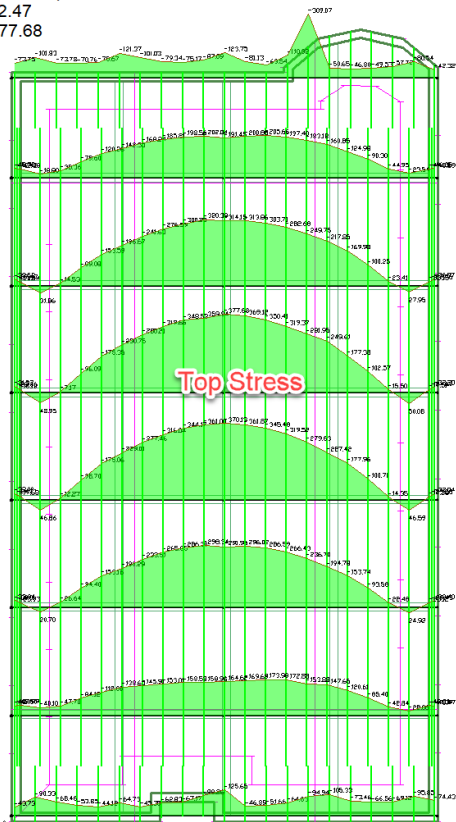
Design Sections, Stresses, Bottom (Psi)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Tensile stress positive
Max: 530.69
Min: -294.42



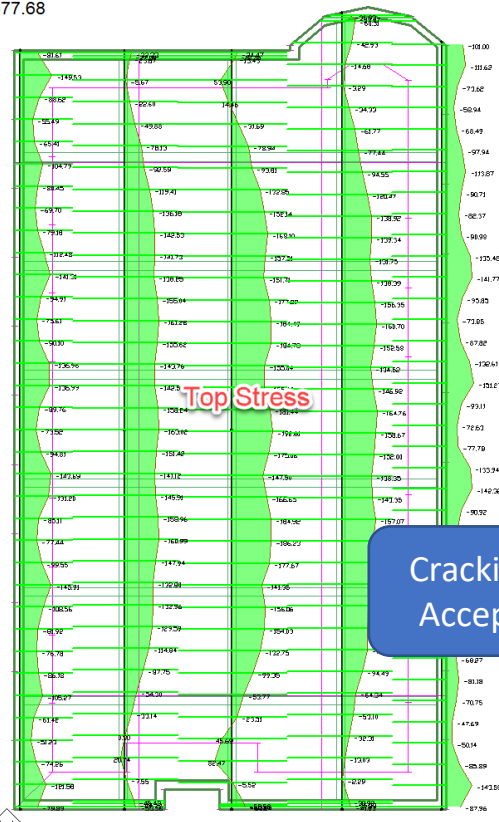
FEM – Moment Analysis @ Detailed – Edge Lift Mode

FEM can provide more detailed and localized stress distribution, a useful guide for added rebar placement.

Design Sections, Stresses, Top (Psi)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Tensile stress positive
Max: 82.47
Min: -377.68

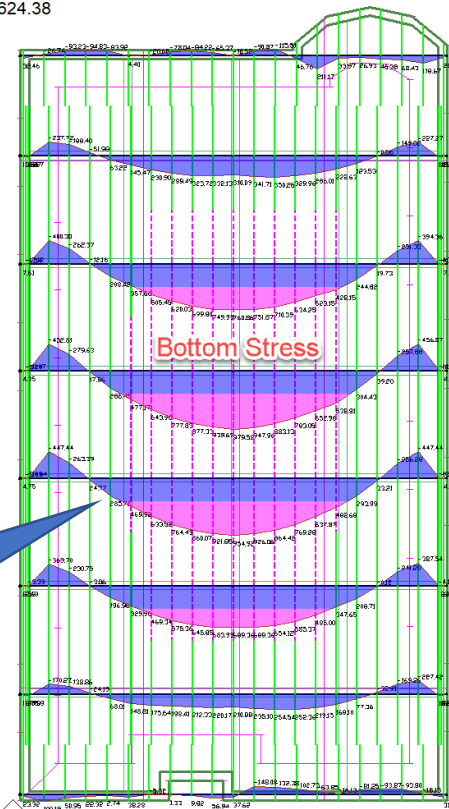


Design Sections, Stresses, Top (Psi)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Tensile stress positive
Max: 82.47
Min: -377.68

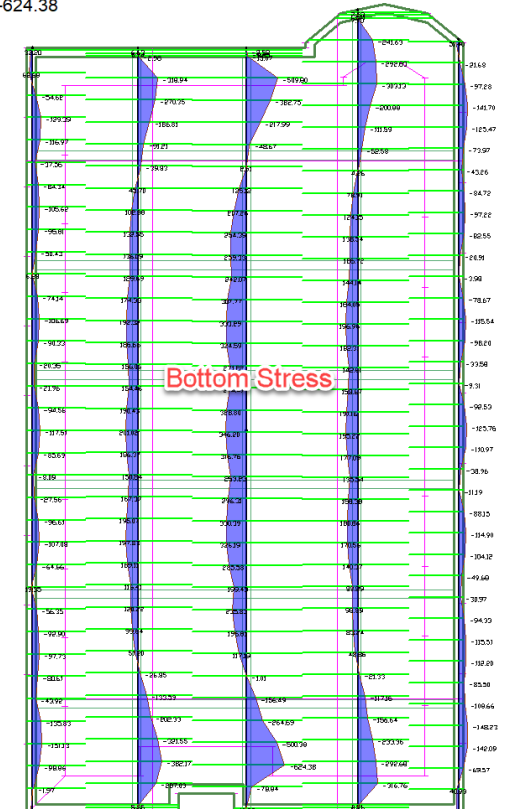


Cracking is Accepted

Design Sections, Stresses, Bottom (Psi)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Tensile stress positive
Max: 979.58
Min: -624.38



Design Sections, Stresses, Bottom (Psi)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Tensile stress positive
Max: 979.58
Min: -624.38



PTISlab – Stiffness Analysis – Edge Lift Mode

Stiffness Analysis - Edge Lift Mode

Based on a Stiffness Coefficient of 960

Available Moment of Inertia (Inch⁴)
Required Moment of Inertia (Inch⁴)
Required Moment of Inertia controlled by

Short Direction	Long Direction
245,897	161,491
181,583 Width	134,309 6*Beta

FEM – Stiffness Analysis – Using Required I – Edge Lift Mode

Design Section

✓ ↶ ?

General Location/Mechanical Properties Design Sections Other Properties

Mechanical properties

Cross-sectional area	5.06e+03 in ²
Moment of inertia	2.46e+05 in ⁴
Distance of centroid to top fiber	6.17e+00 in
Distance of centroid to bottom fiber	2.18e+01 in
Coordinates of centroid	x=9.55e+02 in y=4.23e+02 in
Length	8.44e+02 in

Short Direction

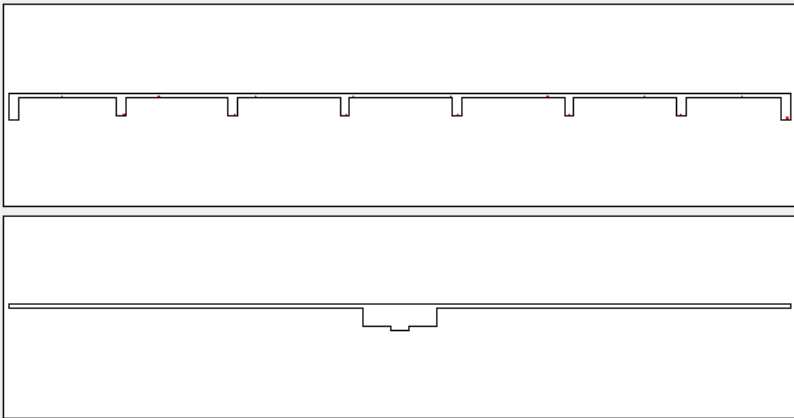
Short direction:

- Required 181,583 (in⁴)
- Available 246,000 (in⁴)
- **OK**

Long direction:

- Required 134,309 (in⁴)
- Available 161,000 (in⁴)
- **OK**

Design Section Zoom



OK

✓ ↶ ?

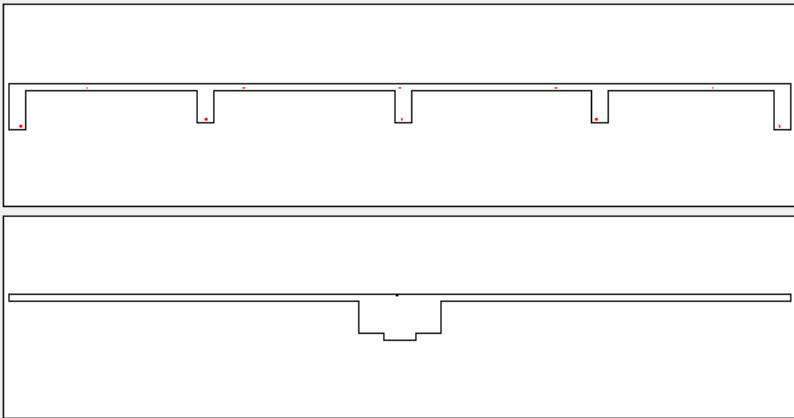
General Location/Mechanical Properties Design Sections Other Properties

Mechanical properties

Cross-sectional area	3.00e+03 in ²
Moment of inertia	1.61e+05 in ⁴
Distance of centroid to top fiber	6.63e+00 in
Distance of centroid to bottom fiber	2.14e+01 in
Coordinates of centroid	x=1.06e+03 in y=7.20e+02 in
Length	4.80e+02 in

Long Direction

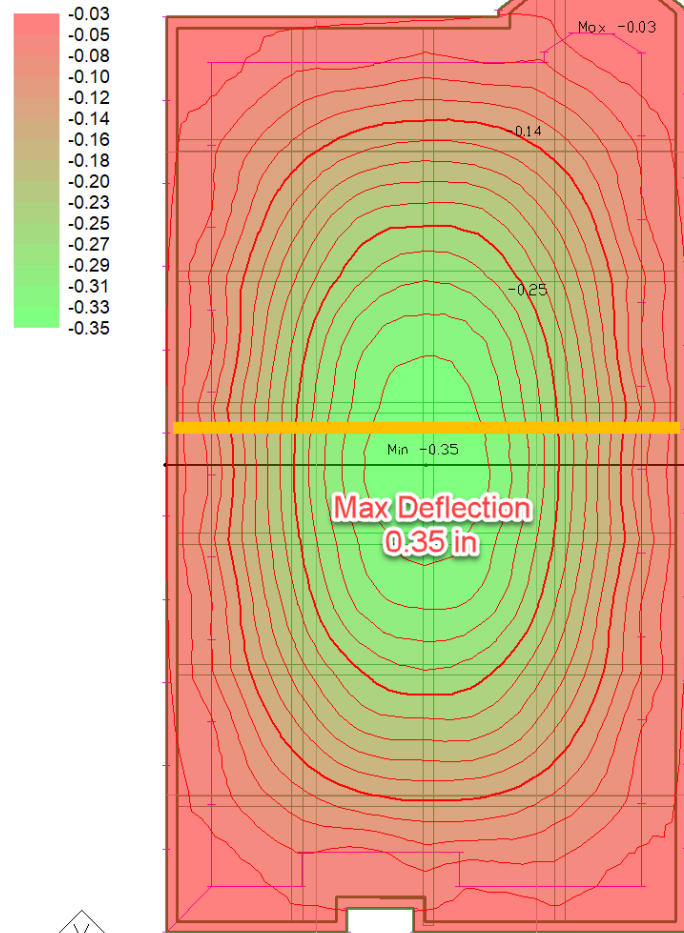
Design Section Zoom



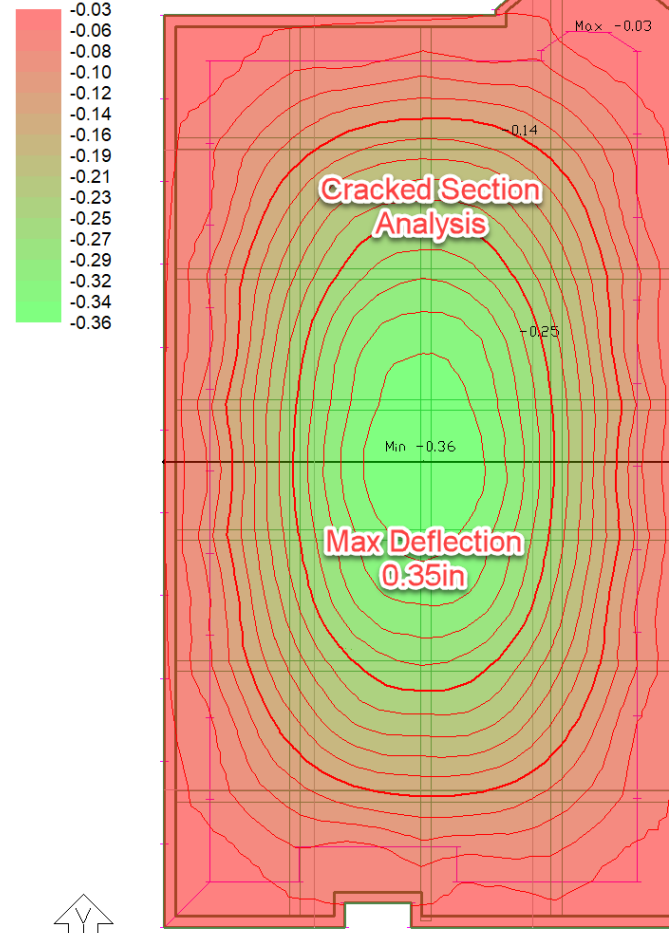
OK

FEM – Stiffness Analysis – Using Deflection – Center Lift Mode

Slab, Deformation, Z-Translation (in)
 Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
 Max -0.03@(102.79, 69.02, 10.00)
 Min -0.35@(87.91, 36.52, 10.00)



Slab, Deformation, Z-Translation (in)
 Load Combination: cracked_Cracked_Analysis
 Max -0.03@(102.79, 69.02, 10.00)
 Min -0.36@(87.91, 36.52, 10.00)



Use actual deflection to check deflection criteria.

- Stiffness coefficient 480
- Max allowable deflection 1.0 in
- Max deflection (uncracked) 0.35 in **OK**
- Max deflection (cracked) 0.36 in **OK**

PTISlab – Shear Analysis – Edge Lift Mode

Shear Analysis - Edge Lift Mode

Maximum Shear, Short Direction
Maximum Shear, Long Direction

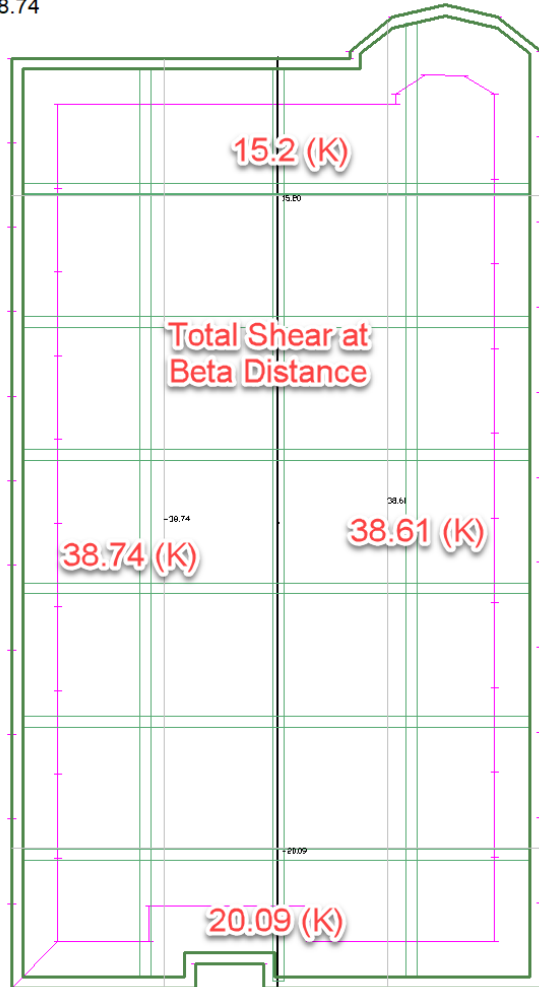
3.76 K/FT
3.95 K/FT

Allowable Shear Stress (PSI)
Actual Shear Stress (PSI)

	Short Direction	Long Direction
	166	167
	131	123

FEM – Shear Analysis – Edge Lift Mode

Manual Design Sections, Actions, Shear (Kip)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Max: 38.61
Min: -38.74



Allowable shear stress:

- Short direction 165 psi
- Long direction 167 psi

Max shear capacity:

- Short direction 331 K
- Long direction 214 K

Shear @ Beta

- Short direction 39 K **OK**
- Long direction 21 K **OK**

Max shear demand

- Short direction 112 K **OK**
- Long direction 53 K **OK**

PTISlab – Cracked Section Analysis – Edge Lift Mode

Cracked Section Analysis - Edge Lift Mode

Cracked Section Capacity (FT-K)
0.5 Moment (FT-K)

Short Direction	Long Direction
406.0	260.8
295.5	140.2

FEM – Cracked Section Analysis – Edge Lift Mode

Short direction:

Design section moment capacity

Positive moment 400.20 k-ft

Negative moment -387.74 k-ft

0.5 M @ Beta 189 K-FT **OK**

0.5 M Max 283 K-FT **OK**

Long direction:

Design section moment capacity

Positive moment 299.97 k-ft

Negative moment -548.30 k-ft

0.5 M @ Beta 14 K-FT **OK**

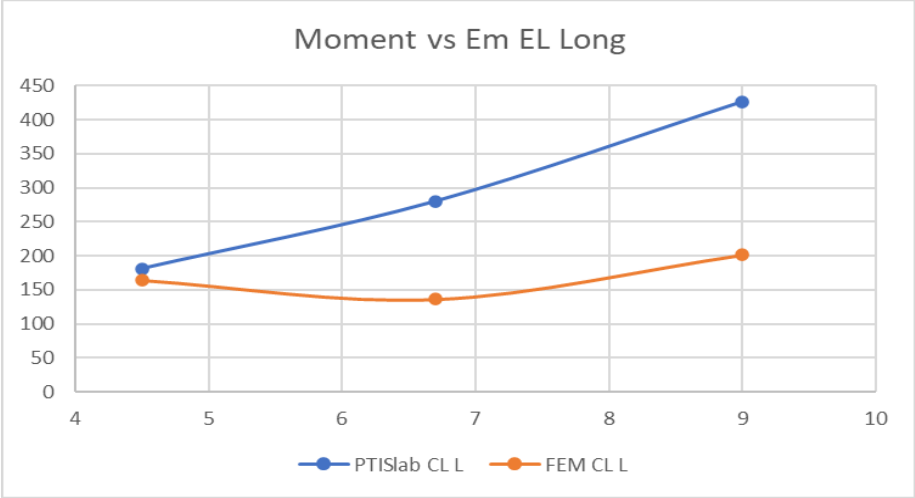
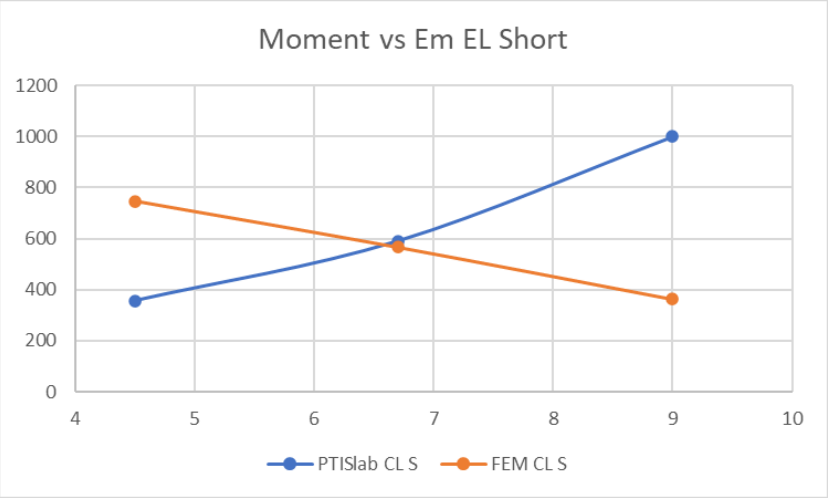
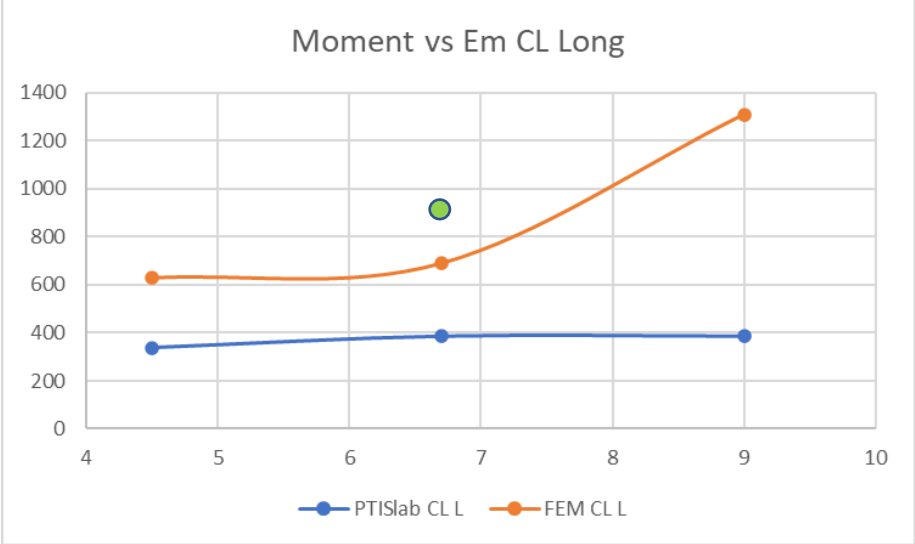
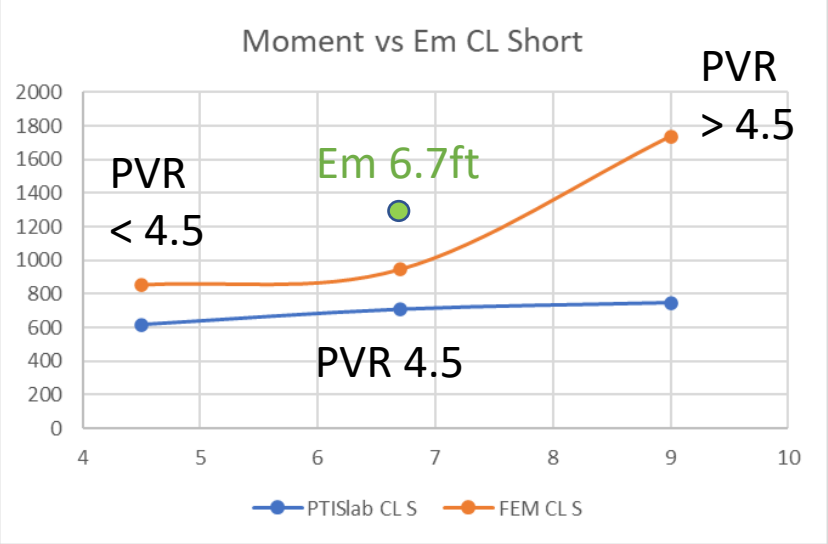
0.5 M Max -68 K-FT **OK**

Summary Table Comparing Design Values

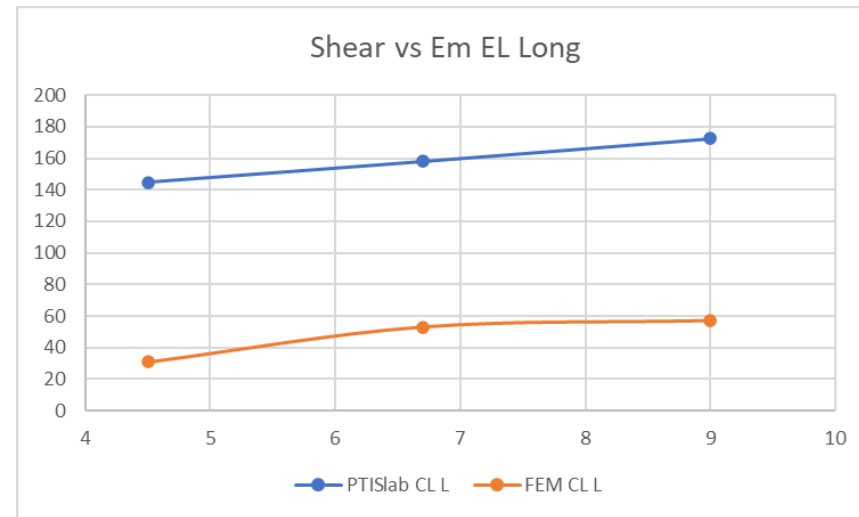
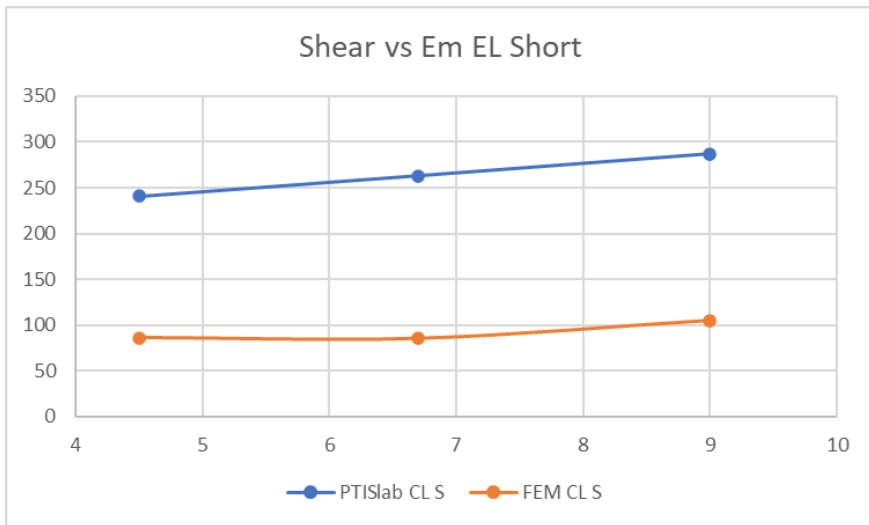
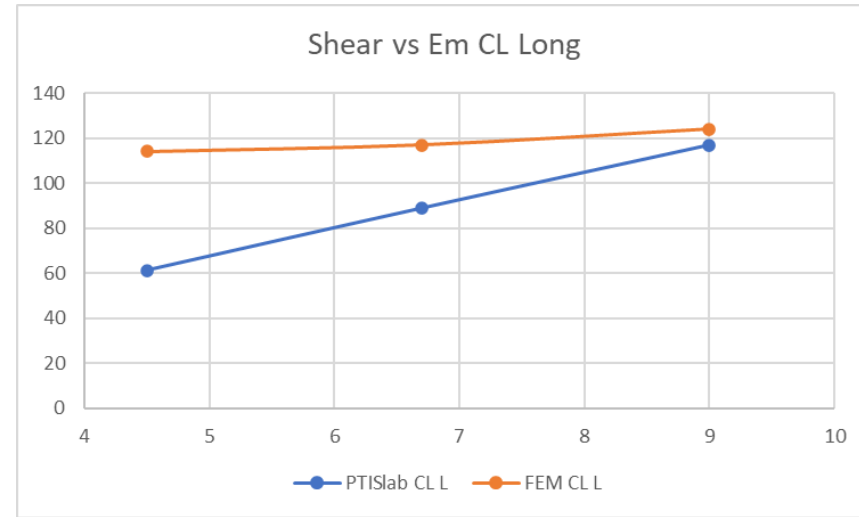
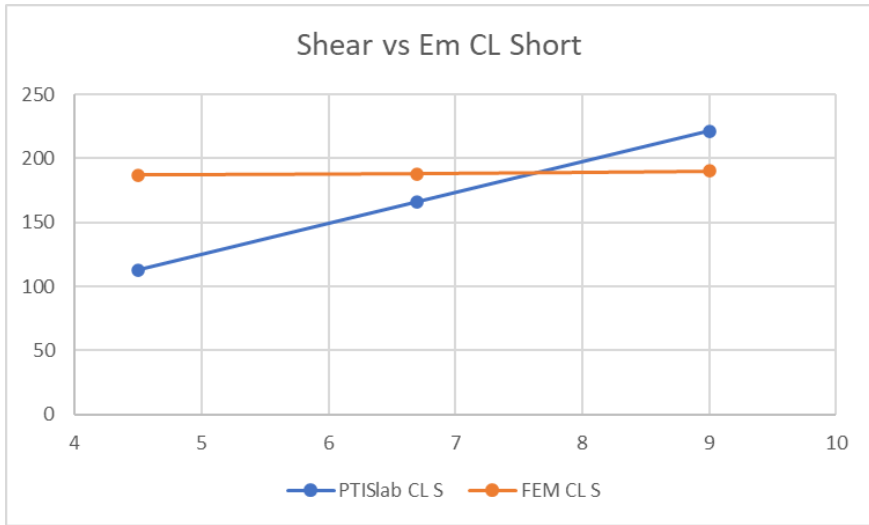
General Design Criteria	PTISlab 3.5	FEM CL Em Limited to 5ft	FEM CL Em 6.7ft
Soil Bearing (uniform) PSF	163	1249	Same
Effective Prestress PSI	64 / 54	69 / 78	Same
Center Lift Mode Design Criteria			
Max Moment @ Beta Short FT-K	707	808	1226
Max Moment @ Beta Long FT-K	384.8	653	928
Max Total Moment Short FT-K	707	946	1227
Max Total Moment Long FT-K	384.8	689	928
Stiffness Check Approach	Rq'd Moment of Inertia	0.6 in Deflection	1.02 in Deflection
Max Shear @ Beta Short K	166	49	29
Max Shear @ Beta Long K	89	40	33
Max Total Shear Short K	166	188	189
Max Total Shear Long K	89	117	122
Edge Lift Mode Design Criteria			
Max Moment @ Beta Short FT-K	591	378	n.a.
Max Moment @ Beta Long FT-K	280	27	n.a.
Max Total Moment Short FT-K	591	566	n.a.
Max Total Moment Long FT-K	280	136	n.a.
Stiffness Check Approach	Req'd Moment of Inertia	0.36 in Deflection	n.a.
Max Shear @ Beta Short K	263	39	n.a.
Max Shear @ Beta Long K	158	20	n.a.
Max Total Shear Short K	263	85	n.a.
Max Total Shear Long K	158	53	n.a.

- FEM values higher for soil bearing
- FEM higher for Center Lift (not limited to $e_m = 5\text{ft}$)
- PTISlab higher for Edge Lift (Soil / Slab interaction less understood)

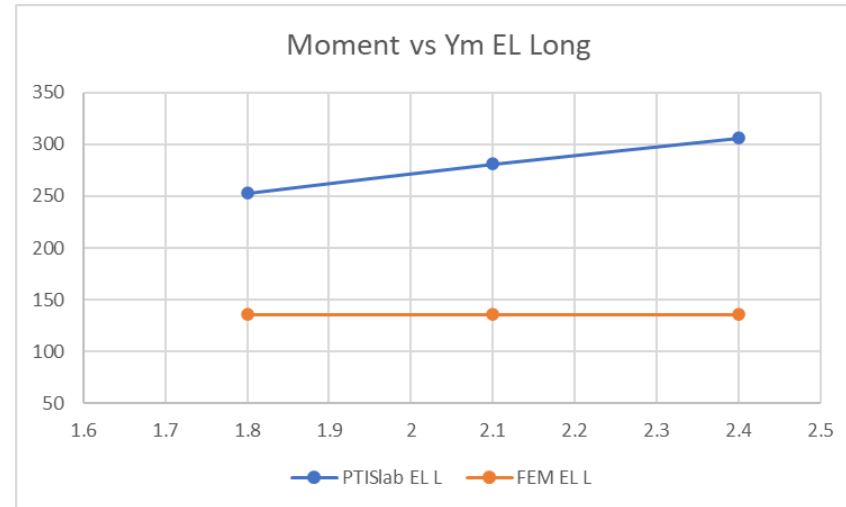
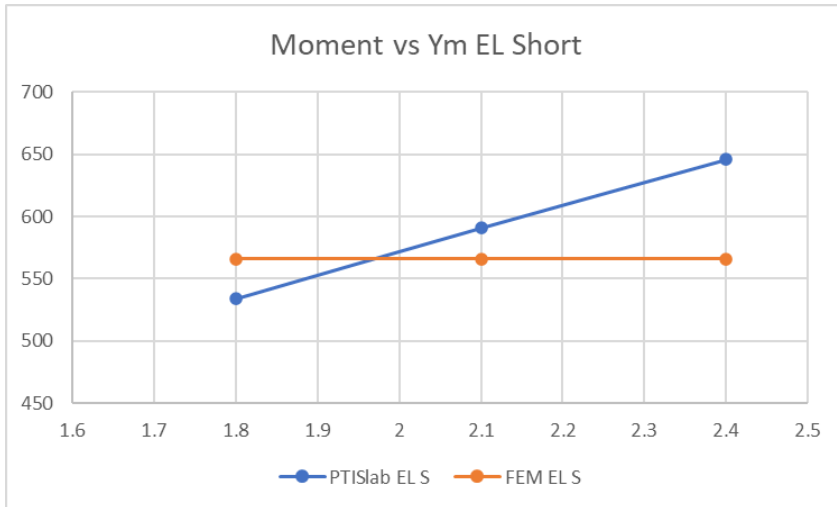
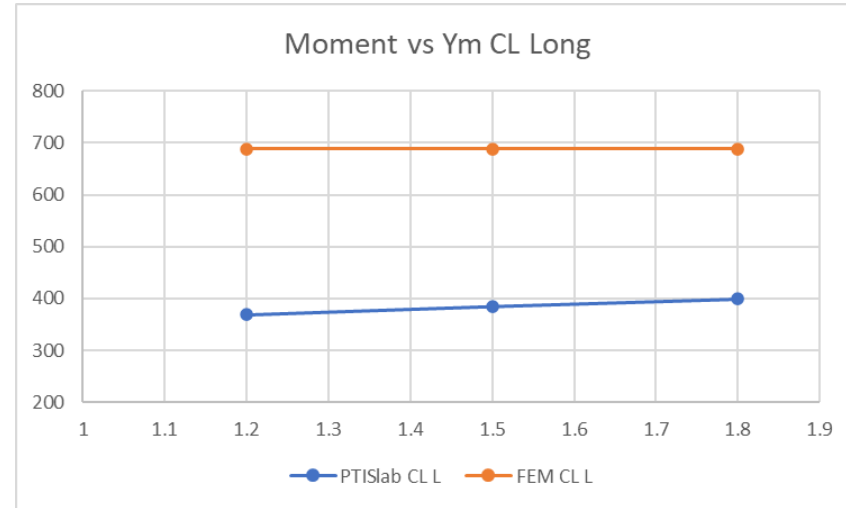
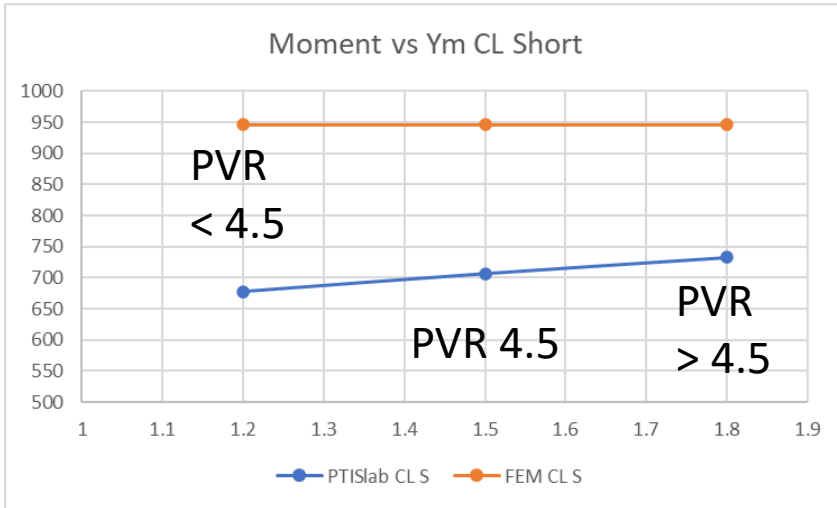
Parametric Study for Different E_m Soil Conditions - Moment



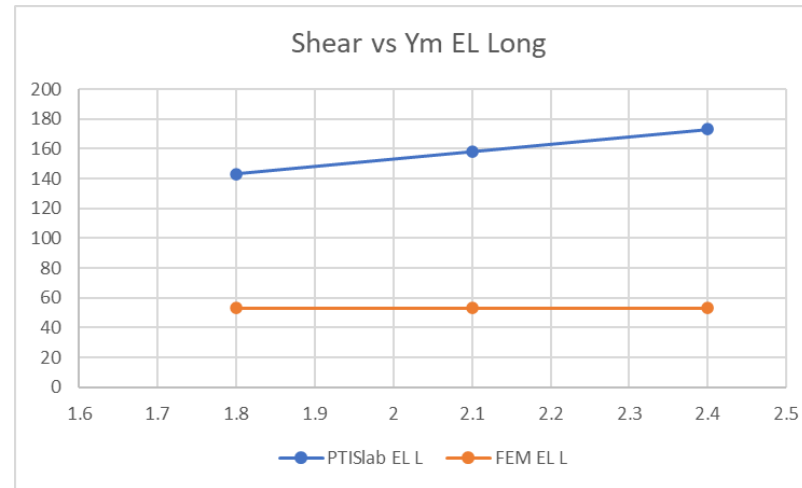
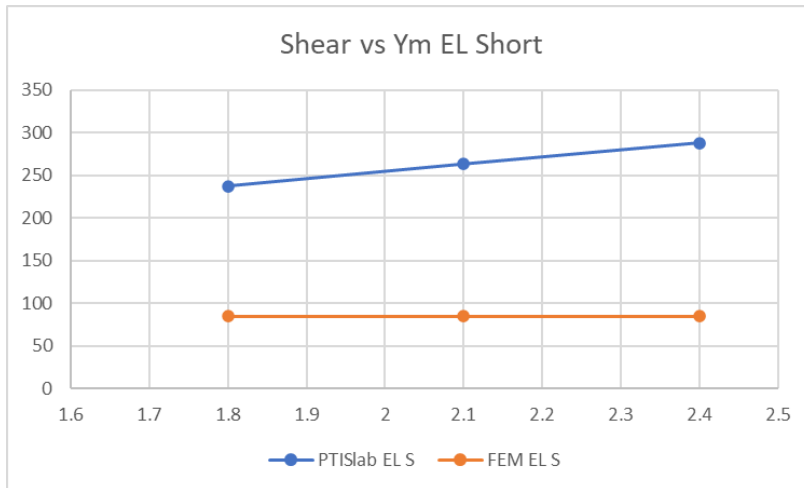
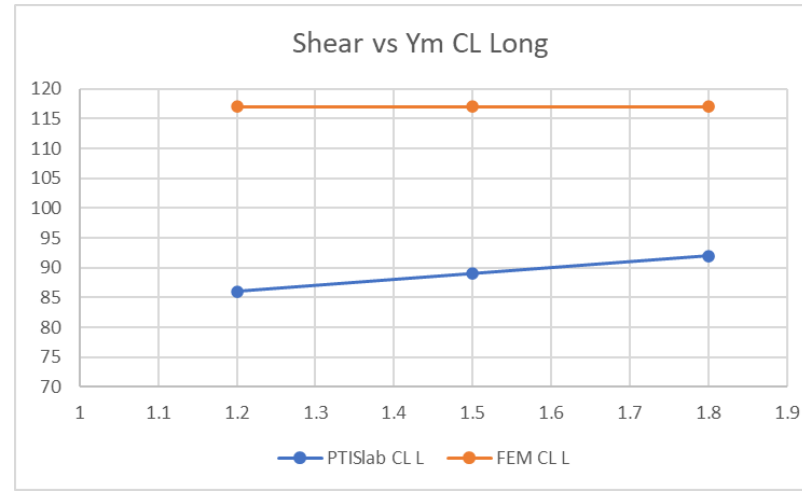
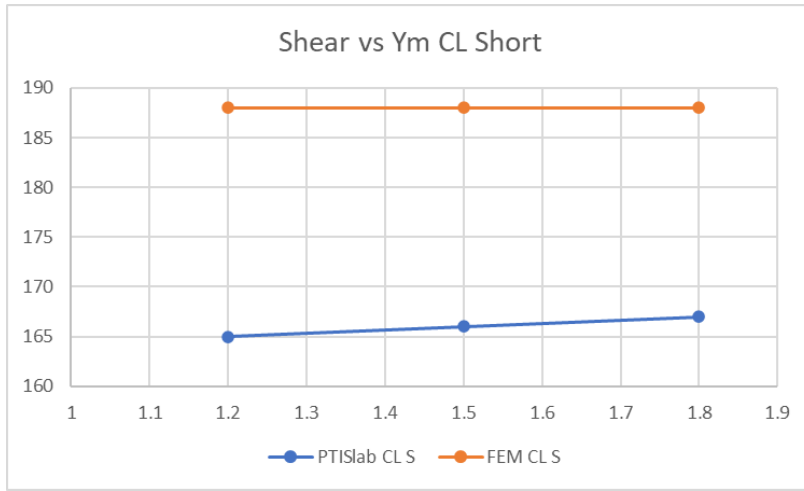
Parametric Study for Different E_m Soil Conditions - Shear



Parametric Study for Different Y_m Soil Conditions - Moment



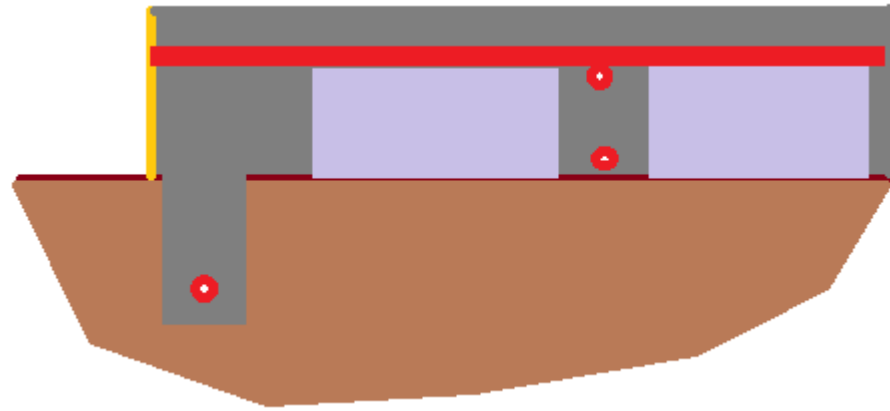
Parametric Study for Different Y_m Soil Conditions - Shear



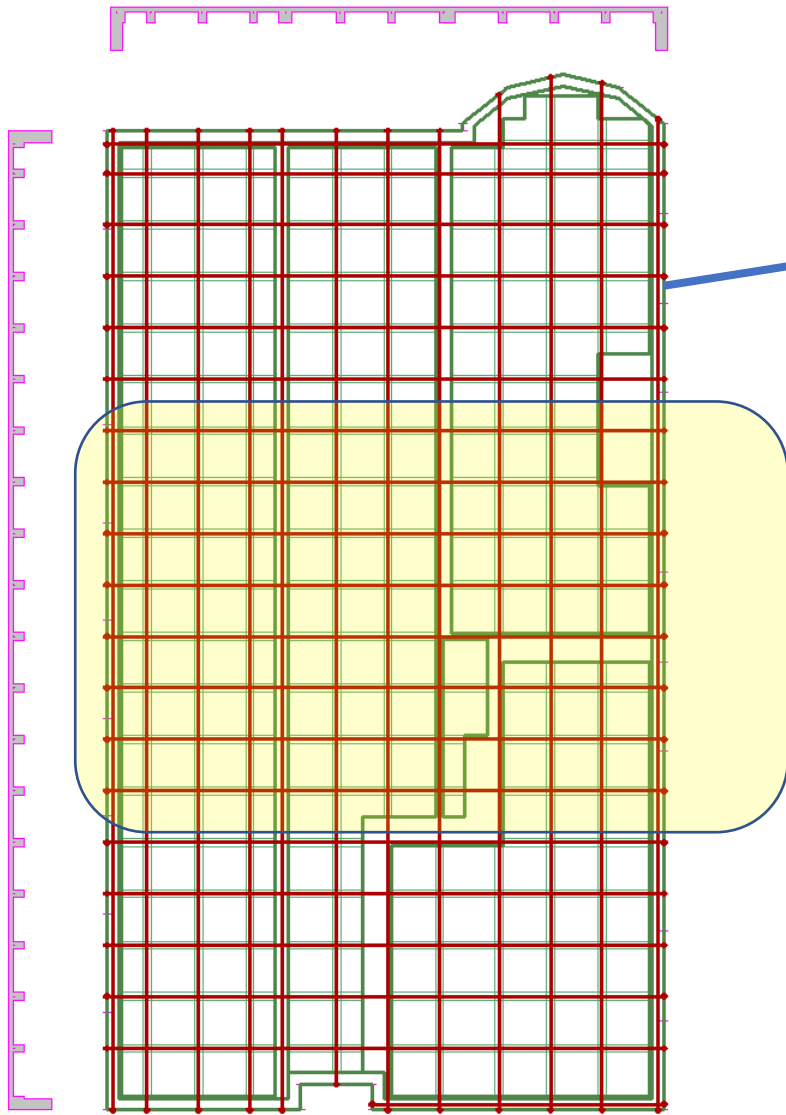
Best Practice for Using FEM to Design Slab-on-Ground Foundations

- Create base model with geometry, loading and tendons
- Reduce effective PT force to account for losses
- Check soil bearing pressure
- Check min 50 psi effective prestress requirement
- Model design strips to allow checking of slab at multiple sections
- Create Center Lift model by removing soil em from perimeter
 - Check moment stresses
 - Check stiffness
 - Check shear
 - Check cracking moment
- Create Edge Lift model by removing soil em from perimeter or by applying edge displacement
 - Calculated deflection limited to y_m
 - Run through all design checks

Wafflemat Construction Sequence



FEM Wafflemat Foundation Analysis Model



General Stressing Location Shape/System/Friction FEM Properties

4.00 4.00

Optimized Tendon Layout

Tendon 13

General Stressing Location Shape/System/Friction FEM Properties

R=8.58 R=8.58 R=8.58 R=8.58

4.00 3.00 3.00 4.00

Span 1
L=39.67

Uplift (K/ft)
0.267

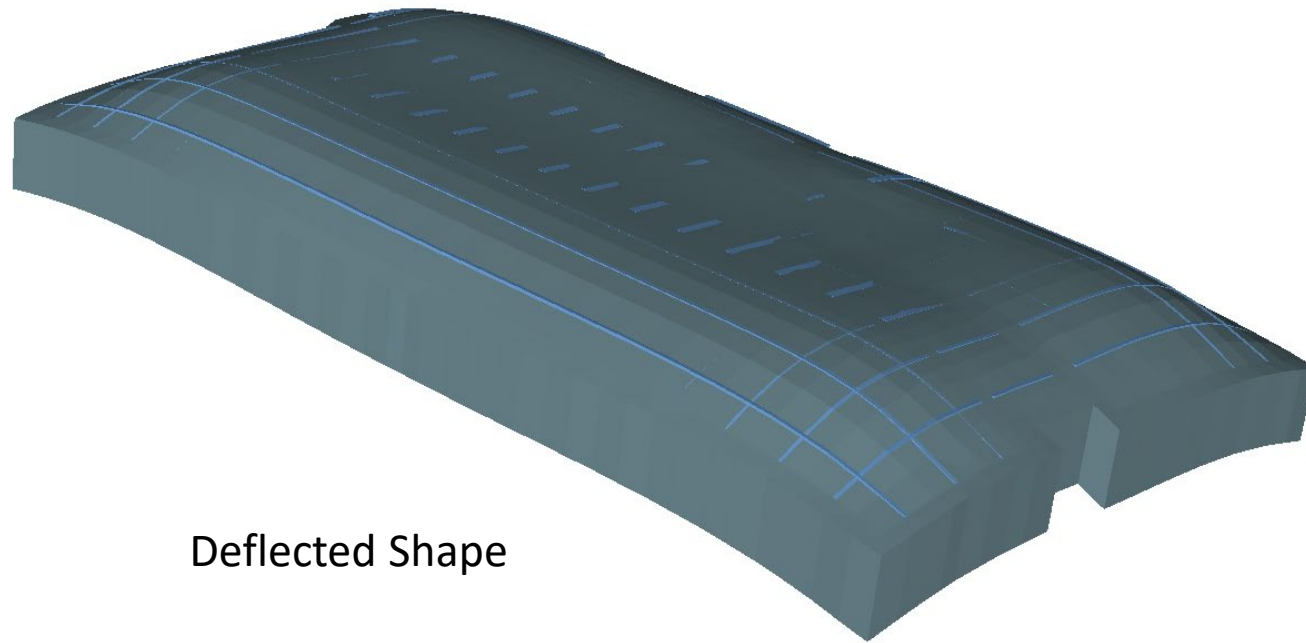
Span	Shape	L (ft)	CGS Top First (in)	CGS Bottom 1 (in)	CGS Bottom 2 (in)	CGS Top Last (in)	X1/L	X2/L	X3/L	A/L	Mu	Wobble (rad/ft)	System
Typical	Reversed Parabola		1.00	1.00	1.00	1.00	0.10	0.50	0.10	0.10			Unbonded
Span 1	Extended Reversed Parabola	39.67	4.00	3.00	3.00	4.00	0.10	0.10					Unbonded

First Span
 Last Span

Minimum radius of curvature (R): ft
 Shape Diagram
 Force Diagram

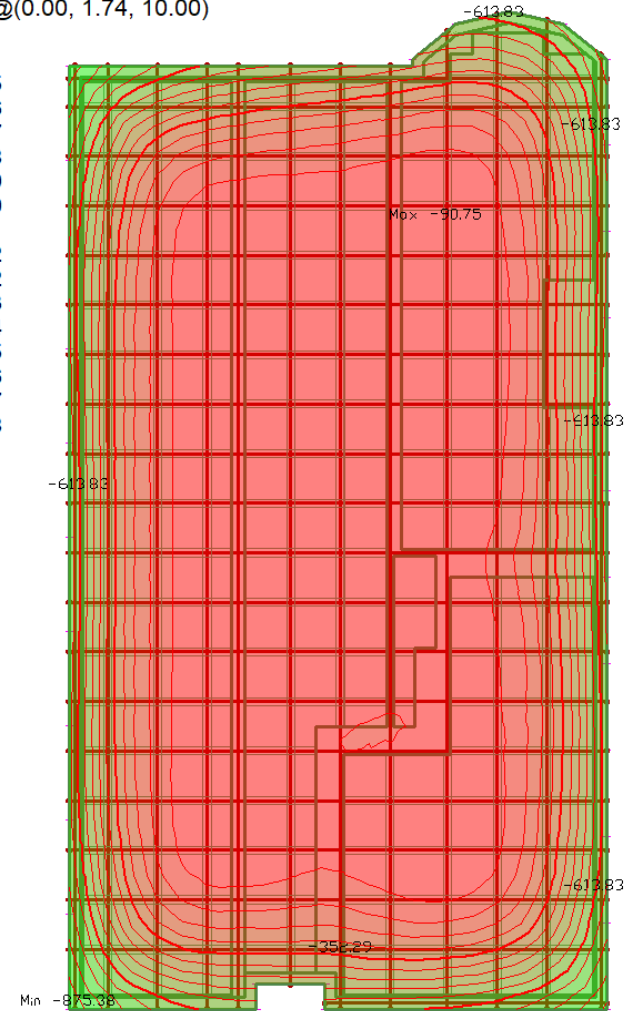
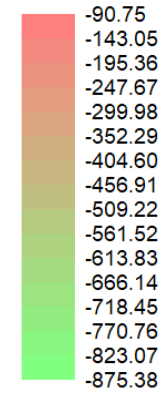
FEM - Soil Bearing Analysis

- Assumes uniform soil support
- Max pressure on soil 875 PSF < allowable 1,500 PSF **OK**



Deflected Shape

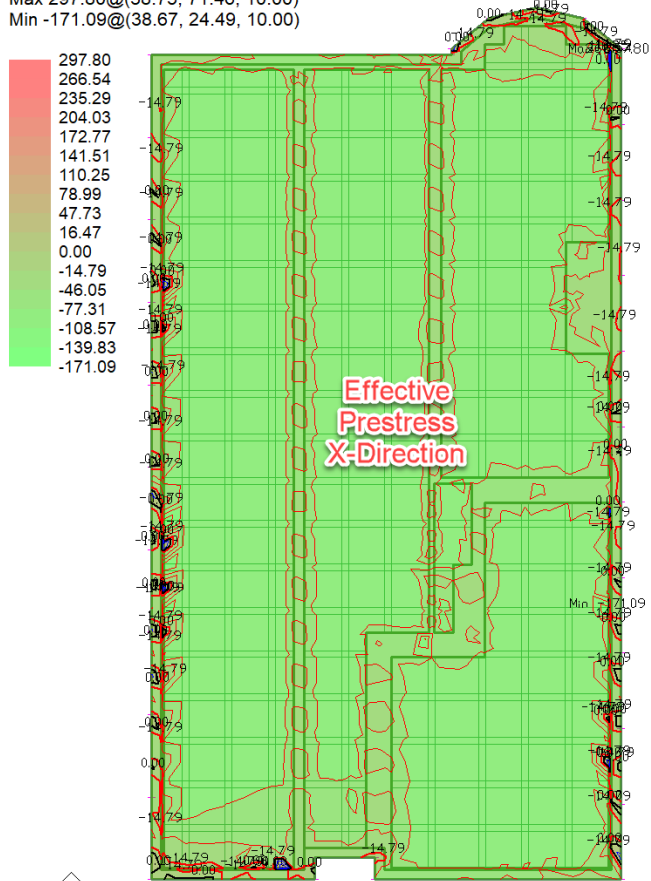
Slab, Stress (contour map), Soil pressure (Psf)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Max -90.75@(27.14, 59.93, 10.00)
Min -875.38@(0.00, 1.74, 10.00)



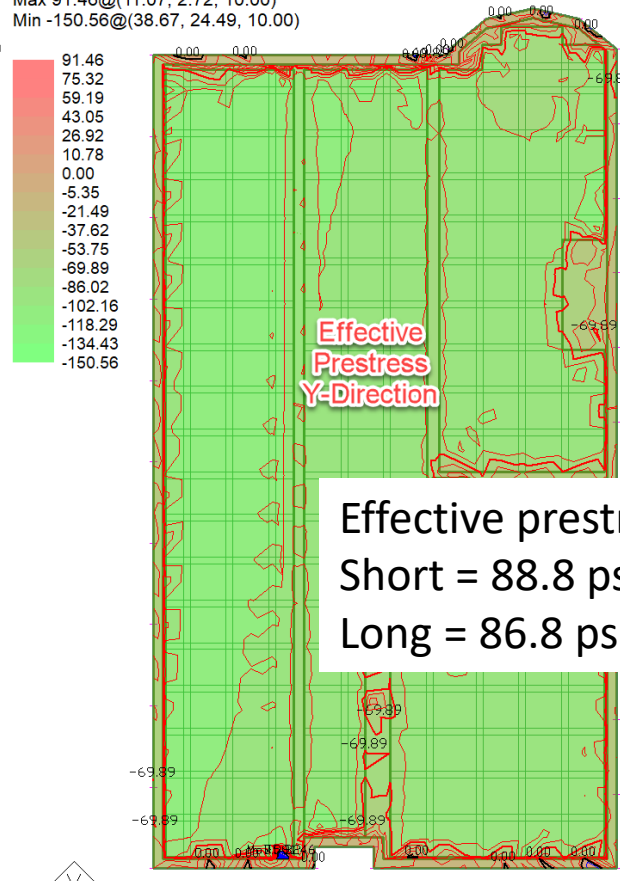
FEM – Effective Prestress Calculations

Reduced PT force applied to model.

Slab, Stress (contour map), Mid-depth along XX (Psi)
 Load Combination: PT Only (SERVICE_TOTAL_LOAD)
 Max 297.80@(38.75, 71.46, 10.00)
 Min -171.09@(38.67, 24.49, 10.00)

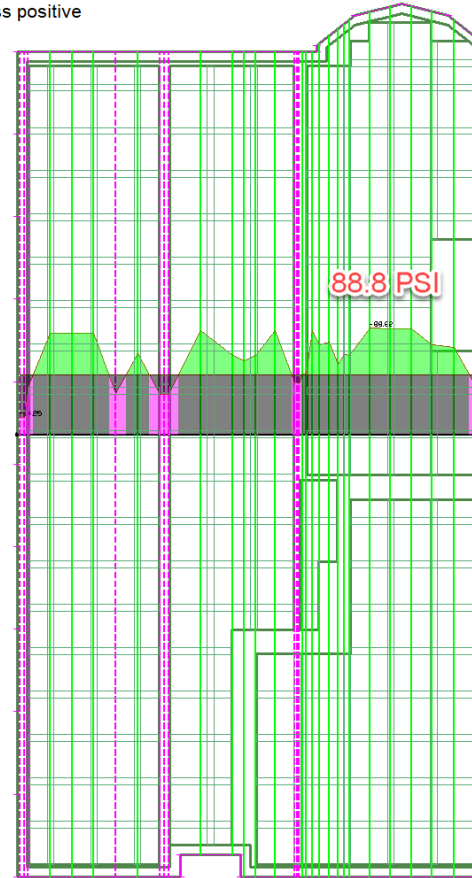


Slab, Stress (contour map), Mid-depth along YY (Psi)
 Load Combination: PT Only (SERVICE_TOTAL_LOAD)
 Max 91.46@(11.07, 2.72, 10.00)
 Min -150.56@(38.67, 24.49, 10.00)

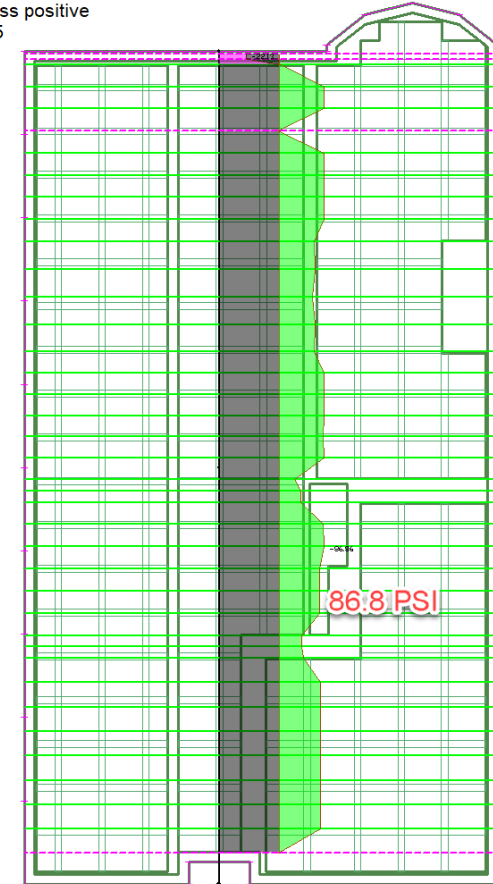


Effective prestress:
 Short = 88.8 psi
 Long = 86.8 psi **OK**

Design Sections, Stresses, P/A (Precompression FEM) (Psi)
 Load Combination: PT Only (SERVICE_TOTAL_LOAD)
 Minimum allowable 50.00
 Tensile stress positive
 Max: -14.25
 Min: -88.82



Design Sections, Stresses, P/A (Precompression FEM) (Psi)
 Load Combination: PT Only (SERVICE_TOTAL_LOAD)
 Minimum allowable 50.00
 Tensile stress positive
 Max: -14.25
 Min: -88.82



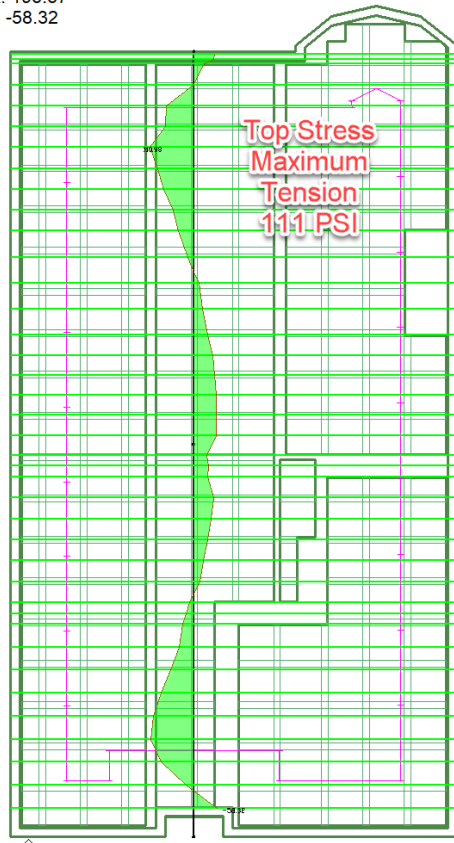
FEM – Moment Analysis – Center Lift Mode

All stresses are within limits – **OK**.

Design Sections, Stresses, Top (Psi)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Tensile stress positive
Max: 196.67
Min: -58.32



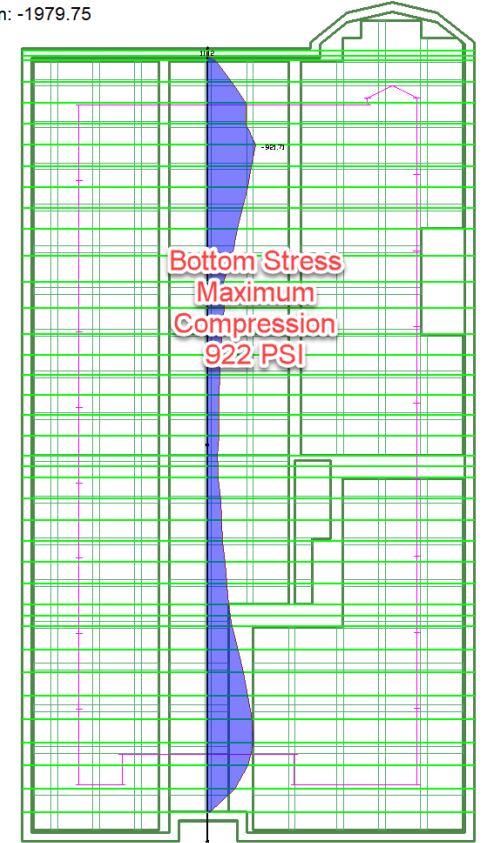
Design Sections, Stresses, Top (Psi)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Tensile stress positive
Max: 196.67
Min: -58.32



Design Sections, Stresses, Bottom (Psi)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Tensile stress positive
Max: 18.23
Min: -1979.75

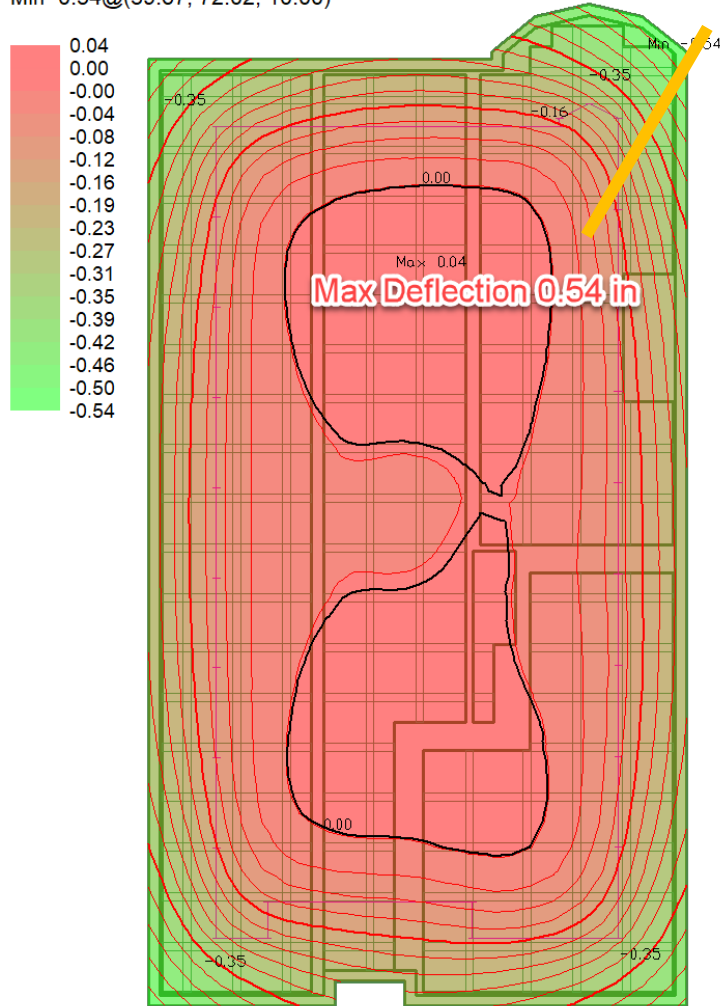


Design Sections, Stresses, Bottom (Psi)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Tensile stress positive
Max: 18.23
Min: -1979.75



FEM – Stiffness Analysis – Center Lift Mode

Slab, Deformation, Z-Translation (in)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Max 0.04@(21.02, 55.95, 10.00)
Min -0.54@(39.67, 72.02, 10.00)



Deflection check:

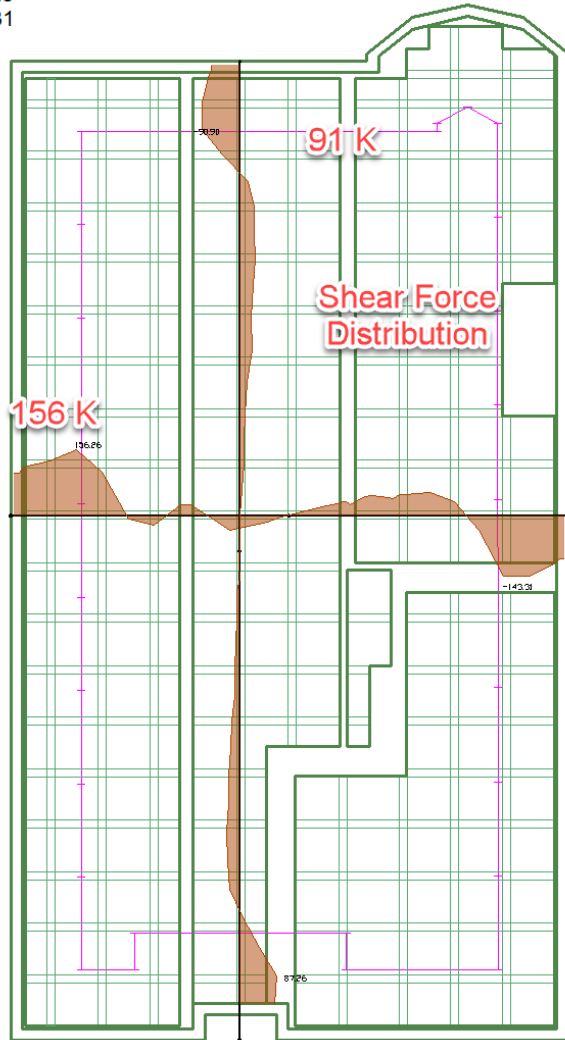
- Cantilever length at max deflection = 16 ft
- Max allowable deflection based on $L / 480 = 0.8$ in
- Max calculated deflection 0.54 in < 0.8 in **OK**

Stiffness comparison (moments of inertia Inch⁴):

- Short direction
 - Traditional ribbed slab 245,897
 - Wafflemat 258,000
- Long direction
 - Traditional ribbed slab 161,491
 - Wafflemat 226,000
- Wafflemat is stiffer in both directions compared to conforming ribbed slab **OK**

FEM – Shear Analysis – Center Lift Mode

Design Sections, Actions, Shear (Kip)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Max: 156.26
Min: -143.31



Allowable shear stress:

- Short direction 169 psi
- Long direction 169 psi

Max shear capacity:

- Short direction 391 K
- Long direction 335 K

Max shear demand

- Short direction 156 K **OK**
- Long direction 91 K **OK**

FEM – Cracked Section Analysis – Center Lift Mode

Short direction:

Design section moment capacity

Positive moment 171.04 k-ft

Negative moment -1063.56 k-ft

0.5 M Max -402 K-FT **OK**

Long direction:

Design section moment capacity

Positive moment 111.00 k-ft

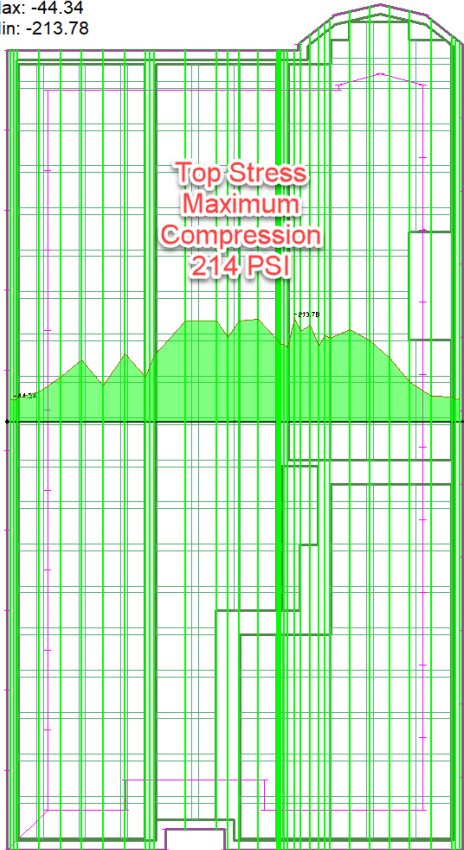
Negative moment -1020.78 k-ft

0.5 M Max -267 K-FT **OK**

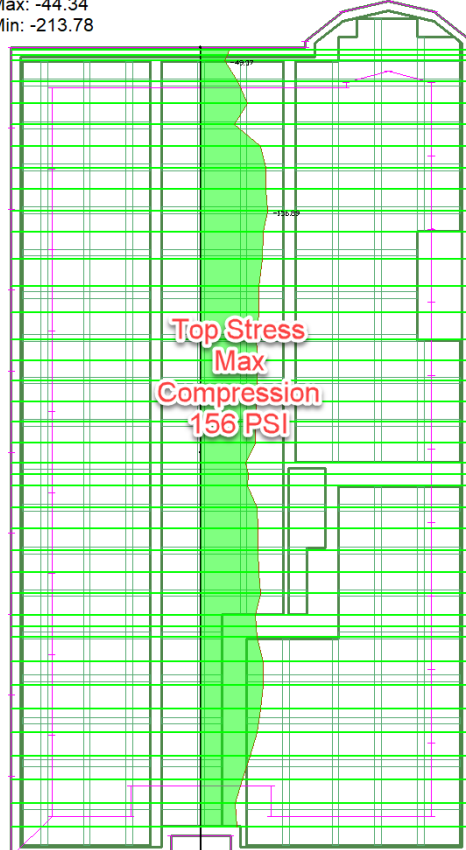
FEM – Moment Analysis – Edge Lift Mode

Bottom tension stresses in Short direction **exceed** allowable – same as traditional ribbed slab – **check cracked deflection.**

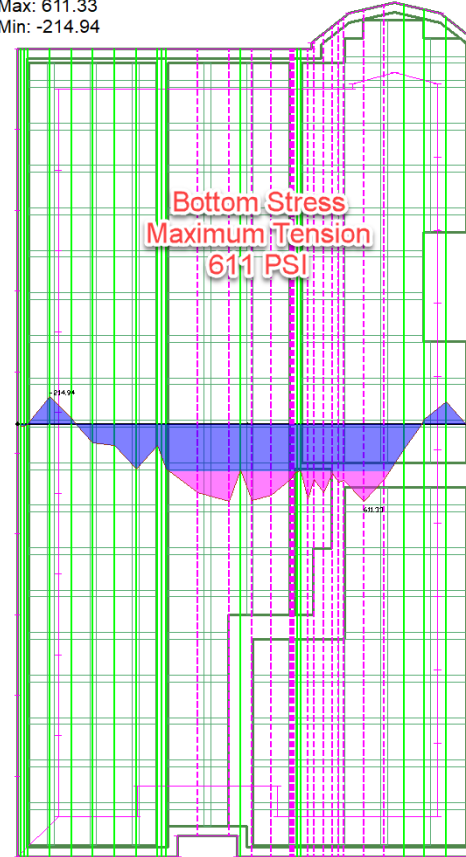
Design Sections, Stresses, Top (Psi)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Tensile stress positive
Max: -44.34
Min: -213.78



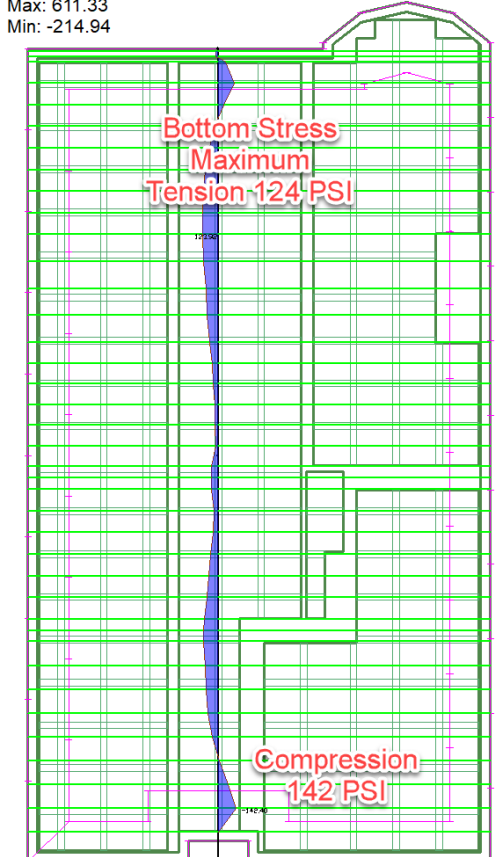
Design Sections, Stresses, Top (Psi)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Tensile stress positive
Max: -44.34
Min: -213.78



Design Sections, Stresses, Bottom (Psi)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Tensile stress positive
Max: 611.33
Min: -214.94

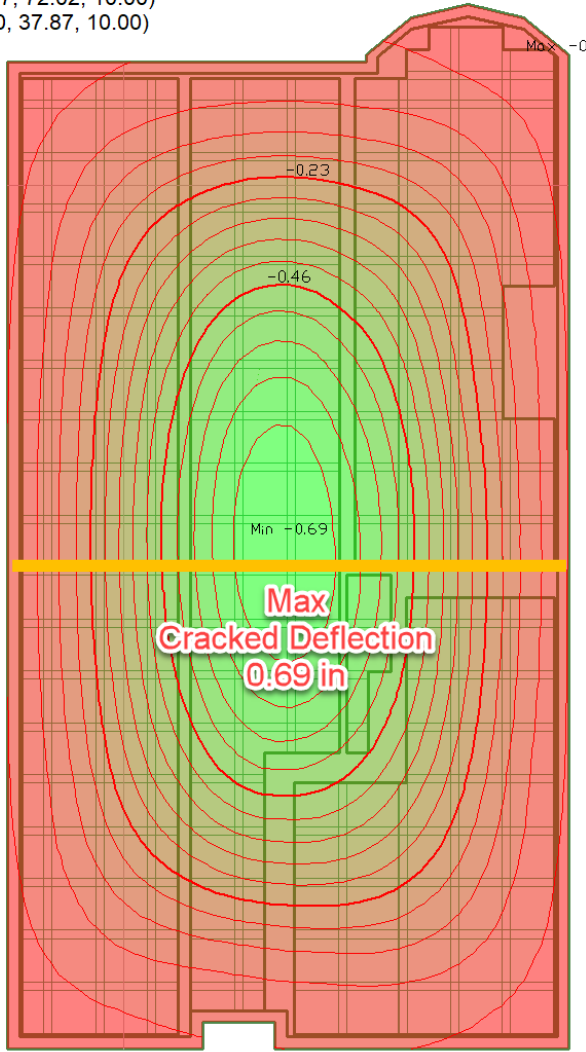
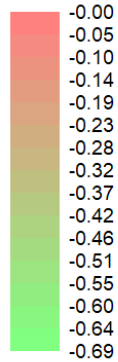


Design Sections, Stresses, Bottom (Psi)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Tensile stress positive
Max: 611.33
Min: -214.94



FEM – Stiffness Analysis – Edge Lift Mode

Slab, Deformation, Z-Translation (in)
Load Combination: cracked_Cracked_Def
Max -0.00@(39.67, 72.02, 10.00)
Min -0.69@(20.00, 37.87, 10.00)



Deflection check:

- Span = 40 ft
- Max allowable deflection based on $L / 480 = 1.0$ in
- Max calculated deflection 0.69 in < 1.0 in **OK**

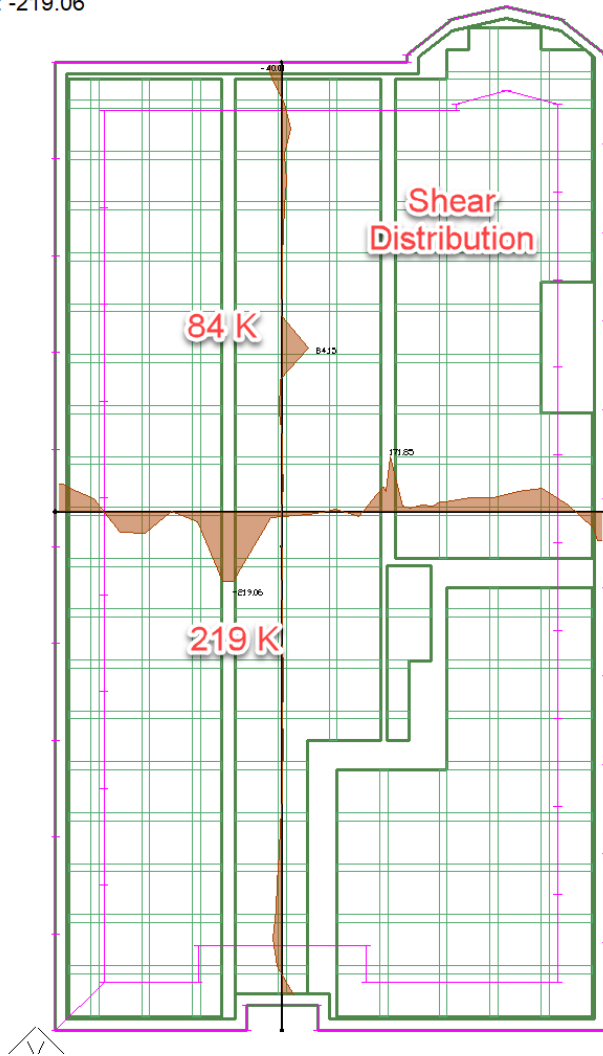
Stiffness comparison (moments of inertia Inch⁴):

- Short direction
 - Traditional ribbed slab 245,897
 - Wafflemat 258,000 **OK**
- Long direction
 - Traditional ribbed slab 161,491
 - Wafflemat 226,000 **OK**
- Wafflemat is stiffer in both directions compared to conforming ribbed slab



FEM – Shear Analysis – Edge Lift Mode

Design Sections, Actions, Shear (Kip)
Load Combination: Service(Total Load) (SERVICE_TOTAL_LOAD)
Max: 171.85
Min: -219.06



Allowable shear stress:

- Short direction 169 psi
- Long direction 169 psi

Max shear capacity:

- Short direction 391 K
- Long direction 335 K

Max shear demand

- Short direction 219 K **OK**
- Long direction 84 K **OK**

FEM – Cracked Section Analysis – Edge Lift Mode

Short direction:

Design section moment capacity	
Positive moment	298.93 k-ft
Negative moment	-958.83 k-ft

0.5 M Max 271 K-FT **OK**

Long direction:

Design section moment capacity	
Positive moment	136.37 k-ft
Negative moment	-993.49 k-ft

0.5 M Max 60 K-FT **OK**

Concluding Remarks

- The FEM method of analysis and design is a valid option for slab-on-ground designs
- We benchmarked the PTISlab method against the FEM method for a 40x70 ribbed slab
- A best practices design methodology based on FEM was presented
- Using the FEM method, we successfully analyzed and validated a wafflemat design

This concludes the Educational Content of this activity.

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