



*Practical Learning Series*

# Quantitative Aptitude

**For CA Foundation New Syllabus 2023**

Applicable for May 2024 Examination and onwards

with around 3600 Objective Q & A

**Complete Coverage of  
CA Foundation Syllabus**

Students' preferred Books for Self Study of CA Course



**CA G. Sekar**

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HEAD OFFICE: 4239/1, SHAKAHAR BHAWAN,  
ANSARI ROAD, DARYA GANJ, NEW DELHI- 110002

Phones: 43502007, 43502008, 43011562, 43452009

e-mail: commercialhouse@yahoo.co.in

naveen.commercialhouse@gmail.com

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Contact Address of Author CA G Sekar

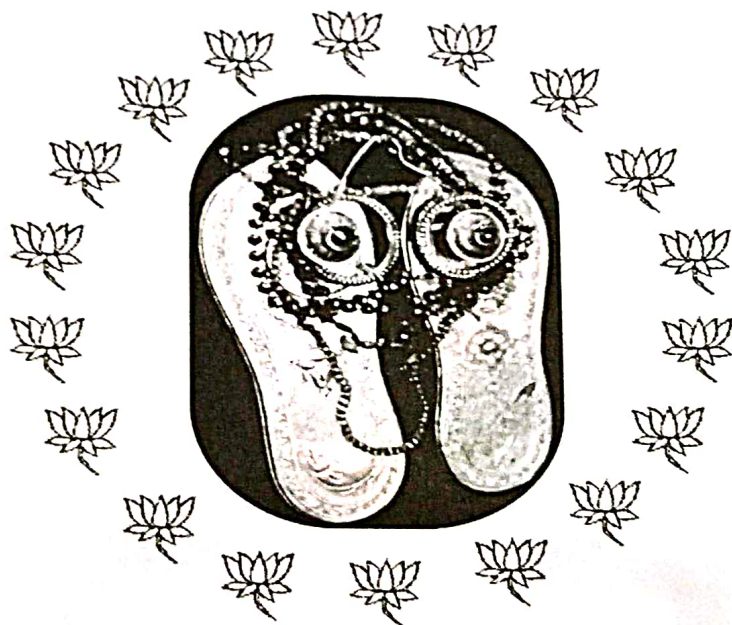
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Phone: 2483 7667; 2484 7667

Email: caclasses@shrigurukripa.com, Website: www.shrigurukripa.com

*PRANAMS*  
*TO*  
*THE ACHARYAS OF KANCHI*



## Preface

In CA Foundation Level, "Padhuka's Practical Learning Series – Quantitative Aptitude" subject covers a important topics from Mathematics, Logical Reasoning and Statistics. The Student is expected to gain control in handling mathematical concepts, formulae and making calculations as required in each topic.

In the CA Foundation Examination, the Student is required to give answers to questions which are on Multiple Choice / Objective Type basis. Hence, the focus of learning is –

- (a) know and remember the principles, concepts, formulae and procedures in Subject.
- (b) read the question quickly in the exam and comprehend the same.
- (c) make calculations as required, and
- (d) arrive at the correct choice as the answer.

The key issue is to handle the exam questions in a **rapid, efficient and effective manner**. It is to be noted that Students are preparing for the Professional Exams and hence, **all topics / subjects** should be given equal importance.

This revised edition of the book has been prepared with a view to communicate the formulae, principles, concepts and procedures in Mathematics, Logical Reasoning ability and Statistics, and to help the Student to meet the professional examination requirements.

**Special features of this updated book include –**

- **Full Coverage** of Examination Syllabus.
- A Lucid presentation of all relevant concepts, with Supportive Derivations, Graphs and Diagrams wherever required.
- About 400 Illustrations, illustrating the working procedures for various problem types.
- **About 3600 Objective Type Questions and Answers**, to help the student test his knowledge in the various segments, in examination simulated conditions.
- **"Additional Questions"** which is a mixture of the various question types has been provided at the end of the Chapter. The same may be attempted by the students as a revision, after attempting the MCQ segment.

With an exhaustive coverage of all that is relevant and required for the examination, any sincere follower of this Book will be able to comfortably clear the exams with distinction.

Many Thanks to the Users of the Padhuka's Publications, for their positive feedback, which reflects the benefits they have reaped from this Book, and also their keen interest to reciprocate with constructive suggestions.

We also thank the efforts and co-operation of the various service providers in bringing out this edition including the support of the Publishers, in quickly getting this book in the current form.

Constructive Suggestions and Feedback from Users would be highly appreciated, gratefully acknowledged and suitably incorporated.

With Best Wishes

**G Sekar**

Chennai  
July 2023

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## Students' Note:

Past Exam Questions based on memory and Important Revisionary Questions are marked with a Star, in the Relevant MCQs section of all the topics.

## **SPECIAL FEATURES / ADVANTAGES OF Padhuka's PUBLICATIONS**

**Padhuka's Publications / Textbooks** come with the following special advantages which will provide a "cutting edge" to students, in scoring high marks in the exams.

1. Comprehensive, Detailed Complete and **Full Coverage of entire syllabus** prescribed by ICAI,
2. Neat and **orderly arrangement** of all the topics given in the syllabus, into identifiable Chapters,
3. Systematic **arrangement** of all concepts in a Chapter,
4. "**Chapter Overview**" at the beginning of every Chapter, to help navigate the contents better,
5. Use of Flowcharts, Diagrams, Charts, Tables, etc. for **effective communication** of concepts,
6. Presentation of all concepts in a neat **Student Friendly format**, in the same manner as the **Student is expected to give his answer in the Main Examinations**,
7. **Detailed Step-by-Step Explanation of Illustrations**, in the same manner as the student is expected to present his answer in the Main Exams,
8. Full Coverage of all questions / illustration / problem types in a Chapter,
9. Use of simple language and effective presentation style, to meet the needs of all **categories of students** – (a) CBSE / Matric / State Board background, (b) English Medium / Regional Language Medium background, (c) Commerce / Non-Commerce background, etc.
10. **Complete Answers to about All Past Main Exams Questions**,
11. Inclusion of Questions & Answers from all the "**Revision Test Papers**" provided by the ICAI,
12. Additional **Exercises, Case Studies**, etc. with final answers thereto, to strengthen the students' hold / command over the subject,
13. **Query Facility** – for getting doubts clarified through e-mail **cabooks@shrigurukripa.com**,
14. **Update Facility** – for getting recent announcements, latest amendments to law, latest updates, etc. through **www.shrigurukripa.com**
15. In short, a **single window for sure success in the CA Exams under Self-Study Method**.

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Financial Tables

Present Value Interest Factor (R,n) =  $\frac{1}{(1+R)^n}$  (Discounting Factor of a Single Cash Flow)

Years	1%	2%	3%	4%	5%	6%	7%	8%	9%	10%
0	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
1	0.990	0.980	0.971	0.962	0.952	0.943	0.935	0.926	0.917	0.909
2	0.980	0.961	0.943	0.925	0.907	0.890	0.873	0.857	0.842	0.826
3	0.971	0.942	0.915	0.889	0.864	0.840	0.816	0.794	0.772	0.751
4	0.961	0.924	0.888	0.855	0.823	0.792	0.763	0.735	0.708	0.683
5	0.951	0.906	0.863	0.822	0.784	0.747	0.713	0.681	0.650	0.621
6	0.942	0.888	0.837	0.790	0.746	0.705	0.666	0.630	0.596	0.564
7	0.933	0.871	0.813	0.760	0.711	0.665	0.623	0.583	0.547	0.513
8	0.923	0.853	0.789	0.731	0.677	0.627	0.582	0.540	0.502	0.467
9	0.914	0.837	0.766	0.703	0.645	0.592	0.544	0.500	0.460	0.424
10	0.905	0.820	0.744	0.676	0.614	0.558	0.508	0.463	0.422	0.386
11	0.896	0.804	0.722	0.650	0.585	0.527	0.475	0.429	0.388	0.350
12	0.887	0.788	0.701	0.625	0.557	0.497	0.444	0.397	0.356	0.319
13	0.879	0.773	0.681	0.601	0.530	0.469	0.415	0.368	0.326	0.290
14	0.870	0.758	0.661	0.577	0.505	0.442	0.388	0.340	0.299	0.263
15	0.861	0.743	0.642	0.555	0.481	0.417	0.362	0.315	0.275	0.239
16	0.853	0.728	0.623	0.534	0.458	0.394	0.339	0.292	0.252	0.218
17	0.844	0.714	0.605	0.513	0.436	0.371	0.317	0.270	0.231	0.198
18	0.836	0.700	0.587	0.494	0.416	0.350	0.296	0.250	0.212	0.180
19	0.828	0.686	0.570	0.475	0.396	0.331	0.277	0.232	0.194	0.164
20	0.820	0.673	0.554	0.456	0.377	0.312	0.258	0.215	0.178	0.149
21	0.811	0.660	0.538	0.439	0.359	0.294	0.242	0.199	0.164	0.135
22	0.803	0.647	0.522	0.422	0.342	0.278	0.226	0.184	0.150	0.123
23	0.795	0.634	0.507	0.406	0.326	0.262	0.211	0.170	0.138	0.112
24	0.788	0.622	0.492	0.390	0.310	0.247	0.197	0.158	0.126	0.102
25	0.780	0.610	0.478	0.375	0.295	0.233	0.184	0.146	0.116	0.092

Years	11%	12%	13%	14%	15%	16%	17%	18%	19%	20%
0	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
1	0.901	0.893	0.885	0.877	0.870	0.862	0.855	0.847	0.840	0.833
2	0.812	0.797	0.783	0.769	0.756	0.743	0.731	0.718	0.706	0.694
3	0.731	0.712	0.693	0.675	0.658	0.641	0.624	0.609	0.593	0.579
4	0.659	0.636	0.613	0.592	0.572	0.552	0.534	0.516	0.499	0.482
5	0.593	0.567	0.543	0.519	0.497	0.476	0.456	0.437	0.419	0.402
6	0.535	0.507	0.480	0.456	0.432	0.410	0.390	0.370	0.352	0.335
7	0.482	0.452	0.425	0.400	0.376	0.354	0.333	0.314	0.296	0.279
8	0.434	0.404	0.376	0.351	0.327	0.305	0.285	0.266	0.249	0.233
9	0.391	0.361	0.333	0.308	0.284	0.263	0.243	0.225	0.209	0.194
10	0.352	0.322	0.295	0.270	0.247	0.227	0.208	0.191	0.176	0.162
11	0.317	0.287	0.261	0.237	0.215	0.195	0.178	0.162	0.148	0.135
12	0.286	0.257	0.231	0.208	0.187	0.168	0.152	0.137	0.124	0.112
13	0.258	0.229	0.204	0.182	0.163	0.145	0.130	0.116	0.104	0.093
14	0.232	0.205	0.181	0.160	0.141	0.125	0.111	0.099	0.088	0.078
15	0.209	0.183	0.160	0.140	0.123	0.108	0.095	0.084	0.074	0.065
16	0.188	0.163	0.141	0.123	0.107	0.093	0.081	0.071	0.062	0.054
17	0.170	0.146	0.125	0.108	0.093	0.080	0.069	0.060	0.052	0.045
18	0.153	0.130	0.111	0.095	0.081	0.069	0.059	0.051	0.044	0.038
19	0.138	0.116	0.098	0.083	0.070	0.060	0.051	0.043	0.037	0.031
20	0.124	0.104	0.087	0.073	0.061	0.051	0.043	0.037	0.031	0.026
21	0.112	0.093	0.077	0.064	0.053	0.044	0.037	0.031	0.026	0.022
22	0.101	0.083	0.068	0.056	0.046	0.038	0.032	0.026	0.022	0.018
23	0.091	0.074	0.060	0.049	0.040	0.033	0.027	0.022	0.018	0.015
24	0.082	0.066	0.053	0.043	0.035	0.028	0.023	0.019	0.015	0.013
25	0.074	0.059	0.047	0.038	0.030	0.024	0.020	0.016	0.013	0.010

Financial Tables

Present Value Interest Factor (R,n) =  $\frac{1}{(1+R)^n}$  (Discounting Factor of a Single Cash Flow)

Years	21%	22%	23%	24%	25%	26%	27%	28%	29%	30%
0	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
1	0.826	0.820	0.813	0.806	0.800	0.794	0.787	0.781	0.775	0.769
2	0.683	0.672	0.661	0.650	0.640	0.630	0.620	0.610	0.601	0.592
3	0.564	0.551	0.537	0.524	0.512	0.500	0.488	0.477	0.466	0.455
4	0.467	0.451	0.437	0.423	0.410	0.397	0.384	0.373	0.361	0.350
5	0.386	0.370	0.355	0.341	0.328	0.315	0.303	0.291	0.280	0.269
6	0.319	0.303	0.289	0.275	0.262	0.250	0.238	0.227	0.217	0.207
7	0.263	0.249	0.235	0.222	0.210	0.198	0.188	0.178	0.168	0.159
8	0.218	0.204	0.191	0.179	0.168	0.157	0.148	0.139	0.130	0.123
9	0.180	0.167	0.155	0.144	0.134	0.125	0.116	0.108	0.101	0.094
10	0.149	0.137	0.126	0.116	0.107	0.099	0.092	0.085	0.078	0.073
11	0.123	0.112	0.103	0.094	0.086	0.079	0.072	0.066	0.061	0.056
12	0.102	0.092	0.083	0.076	0.069	0.062	0.057	0.052	0.047	0.043
13	0.084	0.075	0.068	0.061	0.055	0.050	0.045	0.040	0.037	0.033
14	0.069	0.062	0.055	0.049	0.044	0.039	0.035	0.032	0.028	0.025
15	0.057	0.051	0.045	0.040	0.035	0.031	0.028	0.025	0.022	0.020
16	0.047	0.042	0.036	0.032	0.028	0.025	0.022	0.019	0.017	0.015
17	0.039	0.034	0.030	0.026	0.023	0.020	0.017	0.015	0.013	0.012
18	0.032	0.028	0.024	0.021	0.018	0.016	0.014	0.012	0.010	0.009
19	0.027	0.023	0.020	0.017	0.014	0.012	0.011	0.009	0.008	0.007
20	0.022	0.019	0.016	0.014	0.012	0.010	0.008	0.007	0.006	0.005
21	0.018	0.015	0.013	0.011	0.009	0.008	0.007	0.006	0.005	0.004
22	0.015	0.013	0.011	0.009	0.007	0.006	0.005	0.004	0.004	0.003
23	0.012	0.010	0.009	0.007	0.006	0.005	0.004	0.003	0.003	0.002
24	0.010	0.008	0.007	0.006	0.005	0.004	0.003	0.003	0.002	0.002
25	0.009	0.007	0.006	0.005	0.004	0.003	0.003	0.002	0.002	0.001

Years	31%	32%	33%	34%	35%	36%	37%	38%	39%	40%
0	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
1	0.763	0.758	0.752	0.746	0.741	0.735	0.730	0.725	0.719	0.714
2	0.583	0.574	0.565	0.557	0.549	0.541	0.533	0.525	0.518	0.510
3	0.445	0.435	0.425	0.416	0.406	0.398	0.389	0.381	0.372	0.364
4	0.340	0.329	0.320	0.310	0.301	0.292	0.284	0.276	0.268	0.260
5	0.259	0.250	0.240	0.231	0.223	0.215	0.207	0.200	0.193	0.186
6	0.198	0.189	0.181	0.173	0.165	0.158	0.151	0.145	0.139	0.133
7	0.151	0.143	0.136	0.129	0.122	0.116	0.110	0.105	0.100	0.095
8	0.115	0.108	0.102	0.096	0.091	0.085	0.081	0.076	0.072	0.068
9	0.088	0.082	0.077	0.072	0.067	0.063	0.059	0.055	0.052	0.048
10	0.067	0.062	0.058	0.054	0.050	0.046	0.043	0.040	0.037	0.035
11	0.051	0.047	0.043	0.040	0.037	0.034	0.031	0.029	0.027	0.025
12	0.039	0.036	0.033	0.030	0.027	0.025	0.023	0.021	0.019	0.018
13	0.030	0.027	0.025	0.022	0.020	0.018	0.017	0.015	0.014	0.013
14	0.023	0.021	0.018	0.017	0.015	0.014	0.012	0.011	0.010	0.009
15	0.017	0.016	0.014	0.012	0.011	0.010	0.009	0.008	0.007	0.006
16	0.013	0.012	0.010	0.009	0.008	0.007	0.006	0.006	0.005	0.005
17	0.010	0.009	0.008	0.007	0.006	0.005	0.005	0.004	0.004	0.003
18	0.008	0.007	0.006	0.005	0.005	0.004	0.003	0.003	0.003	0.002
19	0.006	0.005	0.004	0.004	0.003	0.003	0.003	0.002	0.002	0.002
20	0.005	0.004	0.003	0.003	0.002	0.002	0.002	0.002	0.001	0.001
21	0.003	0.003	0.003	0.002	0.002	0.002	0.001	0.001	0.001	0.001
22	0.003	0.002	0.002	0.002	0.001	0.001	0.001	0.001	0.001	0.001
23	0.002	0.002	0.001	0.001	0.001	0.001	0.001	0.001	0.001	0.000
24	0.002	0.001	0.001	0.001	0.001	0.001	0.001	0.000	0.000	0.000
25	0.001	0.001	0.001	0.001	0.001	0.000	0.000	0.000	0.000	0.000

$$\text{Present Value Annuity Factor (R,m)} = \frac{1 - \frac{1}{(1+R)^m}}{R} \quad (\text{Discounting Factor of an Annuity})$$

Years	1%	2%	3%	4%	5%	6%	7%	8%	9%	10%
1	0.990	0.980	0.971	0.962	0.952	0.943	0.935	0.926	0.917	0.909
2	1.970	1.942	1.913	1.886	1.859	1.833	1.808	1.783	1.759	1.736
3	2.941	2.884	2.829	2.775	2.723	2.673	2.624	2.577	2.531	2.487
4	3.902	3.808	3.717	3.630	3.546	3.465	3.387	3.312	3.240	3.170
5	4.853	4.713	4.580	4.452	4.329	4.212	4.100	3.993	3.890	3.791
6	5.795	5.601	5.417	5.242	5.076	4.917	4.767	4.623	4.486	4.355
7	6.728	6.472	6.230	6.002	5.786	5.582	5.389	5.206	5.033	4.868
8	7.652	7.325	7.020	6.733	6.463	6.210	5.971	5.747	5.535	5.335
9	8.566	8.162	7.786	7.435	7.108	6.802	6.515	6.247	5.995	5.759
10	9.471	8.983	8.530	8.111	7.722	7.360	7.024	6.710	6.418	6.145
11	10.368	9.787	9.253	8.760	8.306	7.887	7.499	7.139	6.805	6.495
12	11.255	10.575	9.954	9.385	8.863	8.384	7.943	7.536	7.161	6.814
13	12.134	11.348	10.635	9.986	9.394	8.853	8.358	7.904	7.487	7.103
14	13.004	12.106	11.296	10.563	9.899	9.295	8.745	8.244	7.786	7.367
15	13.865	12.849	11.938	11.118	10.380	9.712	9.108	8.559	8.061	7.606
16	14.718	13.578	12.561	11.652	10.838	10.106	9.447	8.851	8.313	7.824
17	15.562	14.292	13.166	12.166	11.274	10.477	9.763	9.122	8.544	8.022
18	16.398	14.992	13.754	12.659	11.690	10.828	10.059	9.372	8.756	8.201
19	17.226	15.678	14.324	13.134	12.085	11.158	10.336	9.604	8.950	8.365
20	18.046	16.351	14.877	13.590	12.462	11.470	10.594	9.818	9.129	8.514
21	18.857	17.011	15.415	14.029	12.821	11.764	10.836	10.017	9.292	8.649
22	19.660	17.658	15.937	14.451	13.163	12.042	11.061	10.201	9.442	8.772
23	20.456	18.292	16.444	14.857	13.489	12.303	11.272	10.371	9.580	8.883
24	21.243	18.914	16.936	15.247	13.799	12.550	11.469	10.529	9.707	8.985
25	22.023	19.523	17.413	15.622	14.094	12.783	11.654	10.675	9.823	9.077

Years	11%	12%	13%	14%	15%	16%	17%	18%	19%	20%
1	0.901	0.893	0.885	0.877	0.870	0.862	0.855	0.847	0.840	0.833
2	1.713	1.690	1.668	1.647	1.626	1.605	1.585	1.566	1.547	1.528
3	2.444	2.402	2.361	2.322	2.283	2.246	2.210	2.174	2.140	2.106
4	3.102	3.037	2.974	2.914	2.855	2.798	2.743	2.690	2.639	2.589
5	3.696	3.605	3.517	3.433	3.352	3.274	3.199	3.127	3.058	2.991
6	4.231	4.111	3.998	3.889	3.784	3.685	3.589	3.498	3.410	3.326
7	4.712	4.564	4.423	4.288	4.160	4.039	3.922	3.812	3.706	3.605
8	5.146	4.968	4.799	4.639	4.487	4.344	4.207	4.078	3.954	3.837
9	5.537	5.328	5.132	4.946	4.772	4.607	4.451	4.303	4.163	4.031
10	5.889	5.650	5.426	5.216	5.019	4.833	4.659	4.494	4.339	4.192
11	6.207	5.938	5.687	5.453	5.234	5.029	4.836	4.656	4.486	4.327
12	6.492	6.194	5.918	5.660	5.421	5.197	4.988	4.793	4.611	4.439
13	6.750	6.424	6.122	5.842	5.583	5.342	5.118	4.910	4.715	4.533
14	6.982	6.628	6.302	6.002	5.724	5.468	5.229	5.008	4.802	4.611
15	7.191	6.811	6.462	6.142	5.847	5.575	5.324	5.092	4.876	4.675
16	7.379	6.974	6.604	6.265	5.954	5.668	5.405	5.162	4.938	4.730
17	7.549	7.120	6.729	6.373	6.047	5.749	5.475	5.222	4.990	4.775
18	7.702	7.250	6.840	6.467	6.128	5.818	5.534	5.273	5.033	4.812
19	7.839	7.366	6.938	6.550	6.198	5.877	5.584	5.316	5.070	4.843
20	7.963	7.469	7.025	6.623	6.259	5.929	5.628	5.353	5.101	4.870
21	8.075	7.562	7.102	6.687	6.312	5.973	5.665	5.384	5.127	4.891
22	8.176	7.645	7.170	6.743	6.359	6.011	5.696	5.410	5.149	4.909
23	8.266	7.718	7.230	6.792	6.399	6.044	5.723	5.432	5.167	4.925
24	8.348	7.784	7.283	6.835	6.434	6.073	5.746	5.451	5.182	4.937
25	8.422	7.843	7.330	6.873	6.464	6.097	5.766	5.467	5.195	4.948

Financial Tables

Present Value Annuity Factor (R,m) =  $\frac{1 - \frac{1}{(1+R)^m}}{R}$  (Discounting Factor of an Annuity)

Years	21%	22%	23%	24%	25%	26%	27%	28%	29%	30%
1	0.826	0.820	0.813	0.806	0.800	0.794	0.787	0.781	0.775	0.769
2	1.509	1.492	1.474	1.457	1.440	1.424	1.407	1.392	1.376	1.361
3	2.074	2.042	2.011	1.981	1.952	1.923	1.896	1.868	1.842	1.816
4	2.540	2.494	2.448	2.404	2.362	2.320	2.280	2.241	2.203	2.166
5	2.926	2.864	2.803	2.745	2.689	2.635	2.583	2.532	2.483	2.436
6	3.245	3.167	3.092	3.020	2.951	2.885	2.821	2.759	2.700	2.643
7	3.508	3.416	3.327	3.242	3.161	3.083	3.009	2.937	2.868	2.802
8	3.726	3.619	3.518	3.421	3.329	3.241	3.156	3.076	2.999	2.925
9	3.905	3.786	3.673	3.566	3.463	3.366	3.273	3.184	3.100	3.019
10	4.054	3.923	3.799	3.682	3.571	3.465	3.364	3.269	3.178	3.092
11	4.177	4.035	3.902	3.776	3.656	3.543	3.437	3.335	3.239	3.147
12	4.278	4.127	3.985	3.851	3.725	3.606	3.493	3.387	3.286	3.190
13	4.362	4.203	4.053	3.912	3.780	3.656	3.538	3.427	3.322	3.223
14	4.432	4.265	4.108	3.962	3.824	3.695	3.573	3.459	3.351	3.249
15	4.489	4.315	4.153	4.001	3.859	3.726	3.601	3.483	3.373	3.268
16	4.536	4.357	4.189	4.033	3.887	3.751	3.623	3.503	3.390	3.283
17	4.576	4.391	4.219	4.059	3.910	3.771	3.640	3.518	3.403	3.295
18	4.608	4.419	4.243	4.080	3.928	3.786	3.654	3.529	3.413	3.304
19	4.635	4.442	4.263	4.097	3.942	3.799	3.664	3.539	3.421	3.311
20	4.657	4.460	4.279	4.110	3.954	3.808	3.673	3.546	3.427	3.316
21	4.675	4.476	4.292	4.121	3.963	3.816	3.679	3.551	3.432	3.320
22	4.690	4.488	4.302	4.130	3.970	3.822	3.684	3.556	3.436	3.323
23	4.703	4.499	4.311	4.137	3.976	3.827	3.689	3.559	3.438	3.325
24	4.713	4.507	4.318	4.143	3.981	3.831	3.692	3.562	3.441	3.327
25	4.721	4.514	4.323	4.147	3.985	3.834	3.694	3.564	3.442	3.329
Years	31%	32%	33%	34%	35%	36%	37%	38%	39%	40%
1	0.763	0.758	0.752	0.746	0.741	0.735	0.730	0.725	0.719	0.714
2	1.346	1.331	1.317	1.303	1.289	1.276	1.263	1.250	1.237	1.224
3	1.791	1.766	1.742	1.719	1.696	1.673	1.652	1.630	1.609	1.589
4	2.130	2.096	2.062	2.029	1.997	1.966	1.935	1.906	1.877	1.849
5	2.390	2.345	2.302	2.260	2.220	2.181	2.143	2.106	2.070	2.035
6	2.588	2.534	2.483	2.433	2.385	2.339	2.294	2.251	2.209	2.168
7	2.739	2.677	2.619	2.562	2.508	2.455	2.404	2.355	2.308	2.263
8	2.854	2.786	2.721	2.658	2.598	2.540	2.485	2.432	2.380	2.331
9	2.942	2.868	2.798	2.730	2.665	2.603	2.544	2.487	2.432	2.379
10	3.009	2.930	2.855	2.784	2.715	2.649	2.587	2.527	2.469	2.414
11	3.060	2.978	2.899	2.824	2.752	2.683	2.618	2.555	2.496	2.438
12	3.100	3.013	2.931	2.853	2.779	2.708	2.641	2.576	2.515	2.456
13	3.129	3.040	2.956	2.876	2.799	2.727	2.658	2.592	2.529	2.469
14	3.152	3.061	2.974	2.892	2.814	2.740	2.670	2.603	2.539	2.478
15	3.170	3.076	2.988	2.905	2.825	2.750	2.679	2.611	2.546	2.484
16	3.183	3.088	2.999	2.914	2.834	2.757	2.685	2.616	2.551	2.489
17	3.193	3.097	3.007	2.921	2.840	2.763	2.690	2.621	2.555	2.492
18	3.201	3.104	3.012	2.926	2.844	2.767	2.693	2.624	2.557	2.494
19	3.207	3.109	3.017	2.930	2.848	2.770	2.696	2.626	2.559	2.496
20	3.211	3.113	3.020	2.933	2.850	2.772	2.698	2.627	2.561	2.497
21	3.215	3.116	3.023	2.935	2.852	2.773	2.699	2.629	2.562	2.498
22	3.217	3.118	3.025	2.936	2.853	2.775	2.700	2.629	2.562	2.498
23	3.219	3.120	3.026	2.938	2.854	2.775	2.701	2.630	2.563	2.499
24	3.221	3.121	3.027	2.939	2.855	2.776	2.701	2.630	2.563	2.499
25	3.222	3.122	3.028	2.939	2.856	2.777	2.702	2.631	2.563	2.499

Financial Tables

Future Value Interest Factor (R, n) = (1 + R)<sup>n</sup> (Compounding Factor of a Single Cash Flow)

Years	1%	2%	3%	4%	5%	6%	7%	8%	9%	10%
1	1.010	1.020	1.030	1.040	1.050	1.060	1.070	1.080	1.090	1.100
2	1.020	1.040	1.061	1.082	1.103	1.124	1.145	1.166	1.188	1.210
3	1.030	1.061	1.093	1.125	1.158	1.191	1.225	1.260	1.295	1.331
4	1.041	1.082	1.126	1.170	1.216	1.262	1.311	1.360	1.412	1.464
5	1.051	1.104	1.159	1.217	1.276	1.338	1.403	1.469	1.539	1.611
6	1.062	1.126	1.194	1.265	1.340	1.419	1.501	1.587	1.677	1.772
7	1.072	1.149	1.230	1.316	1.407	1.504	1.606	1.714	1.828	1.949
8	1.083	1.172	1.267	1.369	1.477	1.594	1.718	1.851	1.993	2.144
9	1.094	1.195	1.305	1.423	1.551	1.689	1.838	1.999	2.172	2.358
10	1.105	1.219	1.344	1.480	1.629	1.791	1.967	2.159	2.367	2.594
11	1.116	1.243	1.384	1.539	1.710	1.898	2.105	2.332	2.580	2.853
12	1.127	1.268	1.426	1.601	1.796	2.012	2.252	2.518	2.813	3.138
13	1.138	1.294	1.469	1.665	1.886	2.133	2.410	2.720	3.066	3.452
14	1.149	1.319	1.513	1.732	1.980	2.261	2.579	2.937	3.342	3.797
15	1.161	1.346	1.558	1.801	2.079	2.397	2.759	3.172	3.642	4.177
16	1.173	1.373	1.605	1.873	2.183	2.540	2.952	3.426	3.970	4.595
17	1.184	1.400	1.653	1.948	2.292	2.693	3.159	3.700	4.328	5.054
18	1.196	1.428	1.702	2.026	2.407	2.854	3.380	3.996	4.717	5.560
19	1.208	1.457	1.754	2.107	2.527	3.026	3.617	4.316	5.142	6.116
20	1.220	1.486	1.806	2.191	2.653	3.207	3.870	4.661	5.604	6.727
21	1.232	1.516	1.860	2.279	2.786	3.400	4.141	5.034	6.109	7.400
22	1.245	1.546	1.916	2.370	2.925	3.604	4.430	5.437	6.659	8.140
23	1.257	1.577	1.974	2.465	3.072	3.820	4.741	5.871	7.258	8.954
24	1.270	1.608	2.033	2.563	3.225	4.049	5.072	6.341	7.911	9.850
25	1.282	1.641	2.094	2.666	3.386	4.292	5.427	6.848	8.623	10.835

Years	11%	12%	13%	14%	15%	16%	17%	18%	19%	20%
1	1.110	1.120	1.130	1.140	1.150	1.160	1.170	1.180	1.190	1.200
2	1.232	1.254	1.277	1.300	1.323	1.346	1.369	1.392	1.416	1.440
3	1.368	1.405	1.443	1.482	1.521	1.561	1.602	1.643	1.685	1.728
4	1.518	1.574	1.630	1.689	1.749	1.811	1.874	1.939	2.005	2.074
5	1.685	1.762	1.842	1.925	2.011	2.100	2.192	2.288	2.386	2.488
6	1.870	1.974	2.082	2.195	2.313	2.436	2.565	2.700	2.840	2.986
7	2.076	2.211	2.353	2.502	2.660	2.826	3.001	3.185	3.379	3.583
8	2.305	2.476	2.658	2.853	3.059	3.278	3.511	3.759	4.021	4.300
9	2.558	2.773	3.004	3.252	3.518	3.803	4.108	4.435	4.785	5.160
10	2.839	3.106	3.395	3.707	4.046	4.411	4.807	5.234	5.695	6.192
11	3.152	3.479	3.836	4.226	4.652	5.117	5.624	6.176	6.777	7.430
12	3.498	3.896	4.335	4.818	5.350	5.936	6.580	7.288	8.064	8.916
13	3.883	4.363	4.898	5.492	6.153	6.886	7.699	8.599	9.596	10.699
14	4.310	4.887	5.535	6.261	7.076	7.988	9.007	10.147	11.420	12.839
15	4.785	5.474	6.254	7.138	8.137	9.266	10.539	11.974	13.590	15.407
16	5.311	6.130	7.067	8.137	9.358	10.748	12.330	14.129	16.172	18.488
17	5.895	6.866	7.986	9.276	10.761	12.468	14.426	16.672	19.244	22.186
18	6.544	7.690	9.024	10.575	12.375	14.463	16.879	19.673	22.901	26.623
19	7.263	8.613	10.197	12.056	14.232	16.777	19.748	23.214	27.252	31.948
20	8.062	9.646	11.523	13.743	16.367	19.461	23.106	27.393	32.429	38.338
21	8.949	10.804	13.021	15.668	18.822	22.574	27.034	32.324	38.591	46.005
22	9.934	12.100	14.714	17.861	21.645	26.186	31.629	38.142	45.923	55.206
23	11.026	13.552	16.627	20.362	24.891	30.376	37.006	45.008	54.649	66.247
24	12.239	15.179	18.788	23.212	28.625	35.236	43.297	53.109	65.032	79.497
25	13.585	17.000	21.231	26.462	32.919	40.874	50.658	62.669	77.388	95.396

Financial Tables

Future Value Annuity Factor (R,n) =  $\frac{(1+R)^n - 1}{R}$  (Compounding Factor of an Annuity)

Years	1%	2%	3%	4%	5%	6%	7%	8%	9%	10%
1	1.000									
2	2.010	1.000								
3	3.030	2.020	1.000							
4	4.060	3.060	2.030	1.000						
5	5.101	4.122	3.091	2.040	1.000					
6	6.152	5.204	4.184	3.122	2.050	1.000				
7	7.214	6.308	5.309	4.246	3.153	2.060	1.000			
8	8.286	7.434	6.468	5.416	4.310	3.184	2.070	1.000		
9	9.369	8.583	7.662	6.633	5.526	4.375	3.215	2.080	1.000	
10	10.462	9.755	8.892	7.898	6.802	5.637	4.440	3.246	2.090	1.000
11	11.567	10.950	10.159	9.214	8.142	6.975	5.751	4.506	2.100	2.100
12	12.683	12.169	11.464	10.583	9.549	8.394	7.153	4.573	2.090	3.310
13	13.809	13.412	12.808	12.006	11.027	9.897	8.654	4.641	2.080	4.641
14	14.947	14.680	14.192	13.486	12.578	11.491	10.260	4.716	2.070	6.105
15	16.097	15.974	15.618	15.026	14.207	13.181	11.978	4.795	2.060	7.716
16	17.258	17.293	17.086	16.627	15.917	14.972	12.488	4.875	2.050	9.487
17	18.430	18.639	18.599	18.292	17.713	16.870	13.021	4.959	2.040	11.436
18	19.615	20.012	20.157	20.024	19.599	18.882	13.579	5.046	2.030	13.579
19	20.811	21.412	23.414	21.825	21.579	21.015	14.152	5.136	2.020	15.937
20	22.019	22.841	25.117	23.698	23.657	23.276	14.745	5.229	2.010	18.531
21	23.239	24.297	26.870	25.645	25.840	25.673	15.358	5.325	2.000	21.384
22	24.472	25.783	28.676	27.671	28.132	28.213	16.000	5.424	2.000	24.523
23	25.716	27.299	30.537	29.778	30.539	30.906	16.672	5.525	2.000	27.975
24	26.973	28.845	32.453	31.969	33.066	33.760	17.379	5.628	2.000	31.772
25	28.243	30.422	34.426	34.248	35.719	36.786	18.121	5.733	2.000	35.950
		32.030	36.459	36.618	38.505	39.993	18.900	5.840	2.000	40.545
				39.083	41.430	43.392	19.715	5.950	2.000	45.599
				41.646	44.502	46.996	20.565	6.062	2.000	51.159
					47.727	50.816	21.445	6.177	2.000	57.275
						54.865	22.358	6.295	2.000	64.002
							23.300	6.415	2.000	71.403
							24.275	6.536	2.000	79.543
							25.285	6.660	2.000	88.497
							26.328	6.786	2.000	98.347

Years	11%	12%	13%	14%	15%	16%	17%	18%	19%	20%
1	1.000									
2	2.110	1.000								
3	3.342	2.120	1.000							
4	4.710	3.374	2.130	1.000						
5	6.228	4.779	3.407	2.140	1.000					
6	7.913	6.353	4.850	3.440	2.150	1.000				
7	9.783	8.115	6.480	4.921	3.473	2.160	1.000			
8	11.859	10.089	8.323	6.610	4.993	3.506	2.170	1.000		
9	14.164	12.300	10.405	8.536	6.742	5.066	3.539	2.180	1.000	
10	16.722	14.776	12.757	10.730	8.754	5.141	3.572	2.190	2.190	1.000
11	19.561	17.549	15.416	13.233	11.067	5.215	3.606	2.200	2.190	2.200
12	22.713	20.655	18.420	16.085	13.727	5.291	3.640	2.210	2.190	3.640
13	26.212	24.133	21.814	19.337	16.786	5.366	3.688	2.220	2.190	5.368
14	30.095	28.029	25.650	23.045	20.304	5.441	3.742	2.230	2.190	7.442
15	34.405	32.393	29.985	27.271	24.349	5.516	3.800	2.240	2.190	9.930
16	39.190	37.280	34.883	32.089	29.002	5.591	3.862	2.250	2.190	12.916
17	44.501	42.753	40.417	37.581	34.352	5.666	3.928	2.260	2.190	16.499
18	50.396	48.884	46.672	43.842	40.505	5.741	4.000	2.270	2.190	20.799
19	56.939	55.750	53.739	50.980	47.580	5.816	4.076	2.280	2.190	25.959
20	64.203	63.440	61.725	59.118	55.717	5.891	4.156	2.290	2.190	32.150
21	72.265	72.052	70.749	68.394	65.075	5.966	4.240	2.300	2.190	39.581
22	81.214	81.699	80.947	78.969	75.836	6.041	4.328	2.310	2.190	48.497
23	91.148	92.503	92.470	91.025	88.212	6.116	4.420	2.320	2.190	59.196
24	102.174	104.603	105.491	104.768	102.444	6.191	4.516	2.330	2.190	72.035
25	114.413	118.155	120.205	120.436	118.810	6.266	4.616	2.340	2.190	87.442
		133.334	136.831	138.297	137.632	6.341	4.720	2.350	2.190	105.931
			155.620	158.659	159.276	6.416	4.828	2.360	2.190	128.117
				181.871	184.168	6.491	4.940	2.370	2.190	154.740
					212.793	6.566	5.056	2.380	2.190	186.688
						6.641	5.176	2.390	2.190	225.026
						6.716	5.300	2.400	2.190	271.031
						6.791	5.428	2.410	2.190	326.237
						6.866	5.560	2.420	2.190	392.484
						6.941	5.696	2.430	2.190	471.981

Present Value Interest Factor under Continuous Compounding

x	e <sup>-x</sup>	x	e <sup>-x</sup>	x	e <sup>-x</sup>	x	e <sup>-x</sup>	x	e <sup>-x</sup>	x	e <sup>-x</sup>
0.001	0.9990	0.051	0.9503	0.101	0.9039	0.151	0.8598	0.201	0.8179	0.251	0.7780
0.002	0.9980	0.052	0.9493	0.102	0.9030	0.152	0.8590	0.202	0.8171	0.252	0.7772
0.003	0.9970	0.053	0.9484	0.103	0.9021	0.153	0.8581	0.203	0.8163	0.253	0.7765
0.004	0.9960	0.054	0.9474	0.104	0.9012	0.154	0.8573	0.204	0.8155	0.254	0.7757
0.005	0.9950	0.055	0.9465	0.105	0.9003	0.155	0.8564	0.205	0.8146	0.255	0.7749
0.006	0.9940	0.056	0.9455	0.106	0.8994	0.156	0.8556	0.206	0.8138	0.256	0.7741
0.007	0.9930	0.057	0.9446	0.107	0.8985	0.157	0.8547	0.207	0.8130	0.257	0.7734
0.008	0.9920	0.058	0.9436	0.108	0.8976	0.158	0.8538	0.208	0.8122	0.258	0.7726
0.009	0.9910	0.059	0.9427	0.109	0.8967	0.159	0.8530	0.209	0.8114	0.259	0.7718
0.010	0.9900	0.060	0.9418	0.110	0.8958	0.160	0.8521	0.210	0.8106	0.260	0.7711
0.011	0.9891	0.061	0.9408	0.111	0.8949	0.161	0.8513	0.211	0.8098	0.261	0.7703
0.012	0.9881	0.062	0.9399	0.112	0.8940	0.162	0.8504	0.212	0.8090	0.262	0.7695
0.013	0.9871	0.063	0.9389	0.113	0.8932	0.163	0.8496	0.213	0.8082	0.263	0.7687
0.014	0.9861	0.064	0.9380	0.114	0.8923	0.164	0.8487	0.214	0.8073	0.264	0.7680
0.015	0.9851	0.065	0.9371	0.115	0.8914	0.165	0.8479	0.215	0.8065	0.265	0.7672
0.016	0.9841	0.066	0.9361	0.116	0.8905	0.166	0.8470	0.216	0.8057	0.266	0.7664
0.017	0.9831	0.067	0.9352	0.117	0.8896	0.167	0.8462	0.217	0.8049	0.267	0.7657
0.018	0.9822	0.068	0.9343	0.118	0.8887	0.168	0.8454	0.218	0.8041	0.268	0.7649
0.019	0.9812	0.069	0.9333	0.119	0.8878	0.169	0.8445	0.219	0.8033	0.269	0.7641
0.020	0.9802	0.070	0.9324	0.120	0.8869	0.170	0.8437	0.220	0.8025	0.270	0.7634
0.021	0.9792	0.071	0.9315	0.121	0.8860	0.171	0.8428	0.221	0.8017	0.271	0.7626
0.022	0.9782	0.072	0.9305	0.122	0.8851	0.172	0.8420	0.222	0.8009	0.272	0.7619
0.023	0.9773	0.073	0.9296	0.123	0.8843	0.173	0.8411	0.223	0.8001	0.273	0.7611
0.024	0.9763	0.074	0.9287	0.124	0.8834	0.174	0.8403	0.224	0.7993	0.274	0.7603
0.025	0.9753	0.075	0.9277	0.125	0.8825	0.175	0.8395	0.225	0.7985	0.275	0.7596
0.026	0.9743	0.076	0.9268	0.126	0.8816	0.176	0.8386	0.226	0.7977	0.276	0.7588
0.027	0.9734	0.077	0.9259	0.127	0.8807	0.177	0.8378	0.227	0.7969	0.277	0.7581
0.028	0.9724	0.078	0.9250	0.128	0.8799	0.178	0.8369	0.228	0.7961	0.278	0.7573
0.029	0.9714	0.079	0.9240	0.129	0.8790	0.179	0.8361	0.229	0.7953	0.279	0.7565
0.030	0.9704	0.080	0.9231	0.130	0.8781	0.180	0.8353	0.230	0.7945	0.280	0.7558
0.031	0.9695	0.081	0.9222	0.131	0.8772	0.181	0.8344	0.231	0.7937	0.281	0.7550
0.032	0.9685	0.082	0.9213	0.132	0.8763	0.182	0.8336	0.232	0.7929	0.282	0.7543
0.033	0.9675	0.083	0.9204	0.133	0.8755	0.183	0.8328	0.233	0.7922	0.283	0.7535
0.034	0.9666	0.084	0.9194	0.134	0.8746	0.184	0.8319	0.234	0.7914	0.284	0.7528
0.035	0.9656	0.085	0.9185	0.135	0.8737	0.185	0.8311	0.235	0.7906	0.285	0.7520
0.036	0.9646	0.086	0.9176	0.136	0.8728	0.186	0.8303	0.236	0.7898	0.286	0.7513
0.037	0.9637	0.087	0.9167	0.137	0.8720	0.187	0.8294	0.237	0.7890	0.287	0.7505
0.038	0.9627	0.088	0.9158	0.138	0.8711	0.188	0.8286	0.238	0.7882	0.288	0.7498
0.039	0.9618	0.089	0.9148	0.139	0.8702	0.189	0.8278	0.239	0.7874	0.289	0.7490
0.040	0.9608	0.090	0.9139	0.140	0.8694	0.190	0.8270	0.240	0.7866	0.290	0.7483
0.041	0.9598	0.091	0.9130	0.141	0.8685	0.191	0.8261	0.241	0.7858	0.291	0.7475
0.042	0.9589	0.092	0.9121	0.142	0.8676	0.192	0.8253	0.242	0.7851	0.292	0.7468
0.043	0.9579	0.093	0.9112	0.143	0.8668	0.193	0.8245	0.243	0.7843	0.293	0.7460
0.044	0.9570	0.094	0.9103	0.144	0.8659	0.194	0.8237	0.244	0.7835	0.294	0.7453
0.045	0.9560	0.095	0.9094	0.145	0.8650	0.195	0.8228	0.245	0.7827	0.295	0.7445
0.046	0.9550	0.096	0.9085	0.146	0.8642	0.196	0.8220	0.246	0.7819	0.296	0.7438
0.047	0.9541	0.097	0.9076	0.147	0.8633	0.197	0.8212	0.247	0.7811	0.297	0.7430
0.048	0.9531	0.098	0.9066	0.148	0.8624	0.198	0.8204	0.248	0.7804	0.298	0.7423
0.049	0.9522	0.099	0.9057	0.149	0.8616	0.199	0.8195	0.249	0.7796	0.299	0.7416
0.050	0.9512	0.100	0.9048	0.150	0.8607	0.200	0.8187	0.250	0.7788	0.300	0.7408
										0.301	0.7401
										0.302	0.7393
										0.303	0.7386
										0.304	0.7379
										0.305	0.7371
										0.306	0.7364
										0.307	0.7357
										0.308	0.7349
										0.309	0.7342
										0.310	0.7334
										0.311	0.7327
										0.312	0.7320
										0.313	0.7312
										0.314	0.7305
										0.315	0.7298
										0.316	0.7291
										0.317	0.7283
										0.318	0.7276
										0.319	0.7269
										0.320	0.7261
										0.321	0.7254
										0.322	0.7247
										0.323	0.7240
										0.324	0.7233
										0.325	0.7225
										0.326	0.7218
										0.327	0.7211
										0.328	0.7204
										0.329	0.7196
										0.330	0.7189
										0.331	0.7182
										0.332	0.7175
										0.333	0.7168
										0.334	0.7161
										0.335	0.7153
										0.336	0.7146
										0.337	0.7139
										0.338	0.7132
										0.339	0.7125
										0.340	0.7118
										0.341	0.7111
										0.342	0.7103
										0.343	0.7096
										0.344	0.7089
										0.345	0.7082
										0.346	0.7075
										0.347	0.7068
										0.348	0.7061
										0.349	0.7054
										0.350	0.7047

Financial Tables

Present Value Interest Factor under Continuous Compounding

x	e <sup>-x</sup>
0.351	0.7040
0.352	0.7033
0.353	0.7026
0.354	0.7019
0.355	0.7012
0.356	0.7005
0.357	0.6998
0.358	0.6991
0.359	0.6984
0.360	0.6977
0.361	0.6970
0.362	0.6963
0.363	0.6956
0.364	0.6949
0.365	0.6942
0.366	0.6935
0.367	0.6928
0.368	0.6921
0.369	0.6914
0.370	0.6907
0.371	0.6900
0.372	0.6894
0.373	0.6887
0.374	0.6880
0.375	0.6873
0.376	0.6866
0.377	0.6859
0.378	0.6852
0.379	0.6845
0.380	0.6839
0.381	0.6832
0.382	0.6825
0.383	0.6818
0.384	0.6811
0.385	0.6805
0.386	0.6798
0.387	0.6791
0.388	0.6784
0.389	0.6777
0.390	0.6771
0.391	0.6764
0.392	0.6757
0.393	0.6750
0.394	0.6744
0.395	0.6737
0.396	0.6730
0.397	0.6723
0.398	0.6717
0.399	0.6710
0.400	0.6703

x	e <sup>-x</sup>
0.401	0.6697
0.402	0.6690
0.403	0.6683
0.404	0.6676
0.405	0.6670
0.406	0.6663
0.407	0.6656
0.408	0.6650
0.409	0.6643
0.410	0.6637
0.411	0.6630
0.412	0.6623
0.413	0.6617
0.414	0.6610
0.415	0.6603
0.416	0.6597
0.417	0.6590
0.418	0.6584
0.419	0.6577
0.420	0.6570
0.421	0.6564
0.422	0.6557
0.423	0.6551
0.424	0.6544
0.425	0.6538
0.426	0.6531
0.427	0.6525
0.428	0.6518
0.429	0.6512
0.430	0.6505
0.431	0.6499
0.432	0.6492
0.433	0.6486
0.434	0.6479
0.435	0.6473
0.436	0.6466
0.437	0.6460
0.438	0.6453
0.439	0.6447
0.440	0.6440
0.441	0.6434
0.442	0.6427
0.443	0.6421
0.444	0.6415
0.445	0.6408
0.446	0.6402
0.447	0.6395
0.448	0.6389
0.449	0.6383
0.450	0.6376

x	e <sup>-x</sup>
0.451	0.6370
0.452	0.6364
0.453	0.6357
0.454	0.6351
0.455	0.6344
0.456	0.6338
0.457	0.6332
0.458	0.6325
0.459	0.6319
0.460	0.6313
0.461	0.6307
0.462	0.6300
0.463	0.6294
0.464	0.6288
0.465	0.6281
0.466	0.6275
0.467	0.6269
0.468	0.6263
0.469	0.6256
0.470	0.6250
0.471	0.6244
0.472	0.6238
0.473	0.6231
0.474	0.6225
0.475	0.6219
0.476	0.6213
0.477	0.6206
0.478	0.6200
0.479	0.6194
0.480	0.6188
0.481	0.6182
0.482	0.6175
0.483	0.6169
0.484	0.6163
0.485	0.6157
0.486	0.6151
0.487	0.6145
0.488	0.6139
0.489	0.6132
0.490	0.6126
0.491	0.6120
0.492	0.6114
0.493	0.6108
0.494	0.6102
0.495	0.6096
0.496	0.6090
0.497	0.6084
0.498	0.6077
0.499	0.6071
0.500	0.6065

x	e <sup>-x</sup>
0.501	0.6059
0.502	0.6053
0.503	0.6047
0.504	0.6041
0.505	0.6035
0.506	0.6029
0.507	0.6023
0.508	0.6017
0.509	0.6011
0.510	0.6005
0.511	0.5999
0.512	0.5993
0.513	0.5987
0.514	0.5981
0.515	0.5975
0.516	0.5969
0.517	0.5963
0.518	0.5957
0.519	0.5951
0.520	0.5945
0.521	0.5939
0.522	0.5933
0.523	0.5927
0.524	0.5921
0.525	0.5916
0.526	0.5910
0.527	0.5904
0.528	0.5898
0.529	0.5892
0.530	0.5886
0.531	0.5880
0.532	0.5874
0.533	0.5868
0.534	0.5863
0.535	0.5857
0.536	0.5851
0.537	0.5845
0.538	0.5839
0.539	0.5833
0.540	0.5827
0.541	0.5822
0.542	0.5816
0.543	0.5810
0.544	0.5804
0.545	0.5798
0.546	0.5793
0.547	0.5787
0.548	0.5781
0.549	0.5775
0.550	0.5769

x	e <sup>-x</sup>
0.551	0.5764
0.552	0.5758
0.553	0.5752
0.554	0.5746
0.555	0.5741
0.556	0.5735
0.557	0.5729
0.558	0.5724
0.559	0.5718
0.560	0.5712
0.561	0.5706
0.562	0.5701
0.563	0.5695
0.564	0.5689
0.565	0.5684
0.566	0.5678
0.567	0.5672
0.568	0.5667
0.569	0.5661
0.570	0.5655
0.571	0.5650
0.572	0.5644
0.573	0.5638
0.574	0.5633
0.575	0.5627
0.576	0.5621
0.577	0.5616
0.578	0.5610
0.579	0.5605
0.580	0.5599
0.581	0.5593
0.582	0.5588
0.583	0.5582
0.584	0.5577
0.585	0.5571
0.586	0.5565
0.587	0.5560
0.588	0.5554
0.589	0.5549
0.590	0.5543
0.591	0.5538
0.592	0.5532
0.593	0.5527
0.594	0.5521
0.595	0.5516
0.596	0.5510
0.597	0.5505
0.598	0.5499
0.599	0.5494
0.600	0.5488

x	e <sup>-x</sup>
0.601	0.5483
0.602	0.5477
0.603	0.5472
0.604	0.5466
0.605	0.5461
0.606	0.5455
0.607	0.5450
0.608	0.5444
0.609	0.5439
0.610	0.5434
0.611	0.5428
0.612	0.5423
0.613	0.5417
0.614	0.5412
0.615	0.5406
0.616	0.5401
0.617	0.5396
0.618	0.5390
0.619	0.5385
0.620	0.5379
0.621	0.5374
0.622	0.5369
0.623	0.5363
0.624	0.5358
0.625	0.5353
0.626	0.5347
0.627	0.5342
0.628	0.5337
0.629	0.5331
0.630	0.5326
0.631	0.5321
0.632	0.5315
0.633	0.5310
0.634	0.5305
0.635	0.5299
0.636	0.5294
0.637	0.5289
0.638	0.5283
0.639	0.5278
0.640	0.5273
0.641	0.5268
0.642	0.5262
0.643	0.5257
0.644	0.5252
0.645	0.5247
0.646	0.5241
0.647	0.5236
0.648	0.5231
0.649	0.5226
0.650	0.5220



Financial Tables

Present Value Interest Factor under Continuous Compounding

x	e <sup>-x</sup>	x	e <sup>-x</sup>	x	e <sup>-x</sup>	x	e <sup>-x</sup>	x	e <sup>-x</sup>	x	e <sup>-x</sup>	x	e <sup>-x</sup>
0.651	0.5215	0.701	0.4961	0.751	0.4719	0.801	0.4489	0.851	0.4270	0.901	0.4062	0.951	0.3864
0.652	0.5210	0.702	0.4956	0.752	0.4714	0.802	0.4484	0.852	0.4266	0.902	0.4058	0.952	0.3860
0.653	0.5205	0.703	0.4951	0.753	0.4710	0.803	0.4480	0.853	0.4261	0.903	0.4054	0.953	0.3856
0.654	0.5200	0.704	0.4946	0.754	0.4705	0.804	0.4475	0.854	0.4257	0.904	0.4049	0.954	0.3852
0.655	0.5194	0.705	0.4941	0.755	0.4700	0.805	0.4471	0.855	0.4253	0.905	0.4045	0.955	0.3848
0.656	0.5189	0.706	0.4936	0.756	0.4695	0.806	0.4466	0.856	0.4249	0.906	0.4041	0.956	0.3844
0.657	0.5184	0.707	0.4931	0.757	0.4691	0.807	0.4462	0.857	0.4244	0.907	0.4037	0.957	0.3840
0.658	0.5179	0.708	0.4926	0.758	0.4686	0.808	0.4457	0.858	0.4240	0.908	0.4033	0.958	0.3837
0.659	0.5174	0.709	0.4921	0.759	0.4681	0.809	0.4453	0.859	0.4236	0.909	0.4029	0.959	0.3833
0.660	0.5169	0.710	0.4916	0.760	0.4677	0.810	0.4449	0.860	0.4232	0.910	0.4025	0.960	0.3829
0.661	0.5163	0.711	0.4912	0.761	0.4672	0.811	0.4444	0.861	0.4227	0.911	0.4021	0.961	0.3825
0.662	0.5158	0.712	0.4907	0.762	0.4667	0.812	0.4440	0.862	0.4223	0.912	0.4017	0.962	0.3821
0.663	0.5153	0.713	0.4902	0.763	0.4663	0.813	0.4435	0.863	0.4219	0.913	0.4013	0.963	0.3817
0.664	0.5148	0.714	0.4897	0.764	0.4658	0.814	0.4431	0.864	0.4215	0.914	0.4009	0.964	0.3814
0.665	0.5143	0.715	0.4892	0.765	0.4653	0.815	0.4426	0.865	0.4211	0.915	0.4005	0.965	0.3810
0.666	0.5138	0.716	0.4887	0.766	0.4649	0.816	0.4422	0.866	0.4206	0.916	0.4001	0.966	0.3806
0.667	0.5132	0.717	0.4882	0.767	0.4644	0.817	0.4418	0.867	0.4202	0.917	0.3997	0.967	0.3802
0.668	0.5127	0.718	0.4877	0.768	0.4639	0.818	0.4413	0.868	0.4198	0.918	0.3993	0.968	0.3798
0.669	0.5122	0.719	0.4872	0.769	0.4635	0.819	0.4409	0.869	0.4194	0.919	0.3989	0.969	0.3795
0.670	0.5117	0.720	0.4868	0.770	0.4630	0.820	0.4404	0.870	0.4190	0.920	0.3985	0.970	0.3791
0.671	0.5112	0.721	0.4863	0.771	0.4626	0.821	0.4400	0.871	0.4185	0.921	0.3981	0.971	0.3787
0.672	0.5107	0.722	0.4858	0.772	0.4621	0.822	0.4396	0.872	0.4181	0.922	0.3977	0.972	0.3783
0.673	0.5102	0.723	0.4853	0.773	0.4616	0.823	0.4391	0.873	0.4177	0.923	0.3973	0.973	0.3779
0.674	0.5097	0.724	0.4848	0.774	0.4612	0.824	0.4387	0.874	0.4173	0.924	0.3969	0.974	0.3776
0.675	0.5092	0.725	0.4843	0.775	0.4607	0.825	0.4382	0.875	0.4169	0.925	0.3965	0.975	0.3772
0.676	0.5086	0.726	0.4838	0.776	0.4602	0.826	0.4378	0.876	0.4164	0.926	0.3961	0.976	0.3768
0.677	0.5081	0.727	0.4834	0.777	0.4598	0.827	0.4374	0.877	0.4160	0.927	0.3957	0.977	0.3764
0.678	0.5076	0.728	0.4829	0.778	0.4593	0.828	0.4369	0.878	0.4156	0.928	0.3953	0.978	0.3761
0.679	0.5071	0.729	0.4824	0.779	0.4589	0.829	0.4365	0.879	0.4152	0.929	0.3949	0.979	0.3757
0.680	0.5066	0.730	0.4819	0.780	0.4584	0.830	0.4360	0.880	0.4148	0.930	0.3946	0.980	0.3753
0.681	0.5061	0.731	0.4814	0.781	0.4579	0.831	0.4356	0.881	0.4144	0.931	0.3942	0.981	0.3749
0.682	0.5056	0.732	0.4809	0.782	0.4575	0.832	0.4352	0.882	0.4140	0.932	0.3938	0.982	0.3746
0.683	0.5051	0.733	0.4805	0.783	0.4570	0.833	0.4347	0.883	0.4135	0.933	0.3934	0.983	0.3742
0.684	0.5046	0.734	0.4800	0.784	0.4566	0.834	0.4343	0.884	0.4131	0.934	0.3930	0.984	0.3738
0.685	0.5041	0.735	0.4795	0.785	0.4561	0.835	0.4339	0.885	0.4127	0.935	0.3926	0.985	0.3734
0.686	0.5036	0.736	0.4790	0.786	0.4557	0.836	0.4334	0.886	0.4123	0.936	0.3922	0.986	0.3731
0.687	0.5031	0.737	0.4785	0.787	0.4552	0.837	0.4330	0.887	0.4119	0.937	0.3918	0.987	0.3727
0.688	0.5026	0.738	0.4781	0.788	0.4548	0.838	0.4326	0.888	0.4115	0.938	0.3914	0.988	0.3723
0.689	0.5021	0.739	0.4776	0.789	0.4543	0.839	0.4321	0.889	0.4111	0.939	0.3910	0.989	0.3719
0.690	0.5016	0.740	0.4771	0.790	0.4538	0.840	0.4317	0.890	0.4107	0.940	0.3906	0.990	0.3716
0.691	0.5011	0.741	0.4766	0.791	0.4534	0.841	0.4313	0.891	0.4102	0.941	0.3902	0.991	0.3712
0.692	0.5006	0.742	0.4762	0.792	0.4529	0.842	0.4308	0.892	0.4098	0.942	0.3898	0.992	0.3708
0.693	0.5001	0.743	0.4757	0.793	0.4525	0.843	0.4304	0.893	0.4094	0.943	0.3895	0.993	0.3705
0.694	0.4996	0.744	0.4752	0.794	0.4520	0.844	0.4300	0.894	0.4090	0.944	0.3891	0.994	0.3701
0.695	0.4991	0.745	0.4747	0.795	0.4516	0.845	0.4296	0.895	0.4086	0.945	0.3887	0.995	0.3697
0.696	0.4986	0.746	0.4743	0.796	0.4511	0.846	0.4291	0.896	0.4082	0.946	0.3883	0.996	0.3694
0.697	0.4981	0.747	0.4738	0.797	0.4507	0.847	0.4287	0.897	0.4078	0.947	0.3879	0.997	0.3690
0.698	0.4976	0.748	0.4733	0.798	0.4502	0.848	0.4283	0.898	0.4074	0.948	0.3875	0.998	0.3686
0.699	0.4971	0.749	0.4728	0.799	0.4498	0.849	0.4278	0.899	0.4070	0.949	0.3871	0.999	0.3682
0.700	0.4966	0.750	0.4724	0.800	0.4493	0.850	0.4274	0.900	0.4066	0.950	0.3867	1.000	0.3679

Financial Tables

Future Value Interest Factor under Continuous Compounding

x	e <sup>x</sup>	x	e <sup>x</sup>	x	e <sup>x</sup>	x	e <sup>x</sup>	x	e <sup>x</sup>	x	e <sup>x</sup>	x	e <sup>x</sup>	x	e <sup>x</sup>
0.001	1.0010	0.051	1.0523	0.101	1.1063	0.151	1.1630	0.201	1.2226	0.251	1.2853	0.301	1.3512		
0.002	1.0020	0.052	1.0534	0.102	1.1074	0.152	1.1642	0.202	1.2238	0.252	1.2866	0.302	1.3526		
0.003	1.0030	0.053	1.0544	0.103	1.1085	0.153	1.1653	0.203	1.2251	0.253	1.2879	0.303	1.3539		
0.004	1.0040	0.054	1.0555	0.104	1.1096	0.154	1.1665	0.204	1.2263	0.254	1.2892	0.304	1.3553		
0.005	1.0050	0.055	1.0565	0.105	1.1107	0.155	1.1677	0.205	1.2275	0.255	1.2905	0.305	1.3566		
0.006	1.0060	0.056	1.0576	0.106	1.1118	0.156	1.1688	0.206	1.2288	0.256	1.2918	0.306	1.3580		
0.007	1.0070	0.057	1.0587	0.107	1.1129	0.157	1.1700	0.207	1.2300	0.257	1.2930	0.307	1.3593		
0.008	1.0080	0.058	1.0597	0.108	1.1140	0.158	1.1712	0.208	1.2312	0.258	1.2943	0.308	1.3607		
0.009	1.0090	0.059	1.0608	0.109	1.1152	0.159	1.1723	0.209	1.2324	0.259	1.2956	0.309	1.3621		
0.010	1.0101	0.060	1.0618	0.110	1.1163	0.160	1.1735	0.210	1.2337	0.260	1.2969	0.310	1.3634		
0.011	1.0111	0.061	1.0629	0.111	1.1174	0.161	1.1747	0.211	1.2349	0.261	1.2982	0.311	1.3648		
0.012	1.0121	0.062	1.0640	0.112	1.1185	0.162	1.1759	0.212	1.2361	0.262	1.2995	0.312	1.3662		
0.013	1.0131	0.063	1.0650	0.113	1.1196	0.163	1.1770	0.213	1.2374	0.263	1.3008	0.313	1.3675		
0.014	1.0141	0.064	1.0661	0.114	1.1208	0.164	1.1782	0.214	1.2386	0.264	1.3021	0.314	1.3689		
0.015	1.0151	0.065	1.0672	0.115	1.1219	0.165	1.1794	0.215	1.2399	0.265	1.3034	0.315	1.3703		
0.016	1.0161	0.066	1.0682	0.116	1.1230	0.166	1.1806	0.216	1.2411	0.266	1.3047	0.316	1.3716		
0.017	1.0171	0.067	1.0693	0.117	1.1241	0.167	1.1818	0.217	1.2423	0.267	1.3060	0.317	1.3730		
0.018	1.0182	0.068	1.0704	0.118	1.1252	0.168	1.1829	0.218	1.2436	0.268	1.3073	0.318	1.3744		
0.019	1.0192	0.069	1.0714	0.119	1.1264	0.169	1.1841	0.219	1.2448	0.269	1.3087	0.319	1.3758		
0.020	1.0202	0.070	1.0725	0.120	1.1275	0.170	1.1853	0.220	1.2461	0.270	1.3100	0.320	1.3771		
0.021	1.0212	0.071	1.0736	0.121	1.1286	0.171	1.1865	0.221	1.2473	0.271	1.3113	0.321	1.3785		
0.022	1.0222	0.072	1.0747	0.122	1.1298	0.172	1.1877	0.222	1.2486	0.272	1.3126	0.322	1.3799		
0.023	1.0233	0.073	1.0757	0.123	1.1309	0.173	1.1889	0.223	1.2498	0.273	1.3139	0.323	1.3813		
0.024	1.0243	0.074	1.0768	0.124	1.1320	0.174	1.1901	0.224	1.2511	0.274	1.3152	0.324	1.3826		
0.025	1.0253	0.075	1.0779	0.125	1.1331	0.175	1.1912	0.225	1.2523	0.275	1.3165	0.325	1.3840		
0.026	1.0263	0.076	1.0790	0.126	1.1343	0.176	1.1924	0.226	1.2536	0.276	1.3178	0.326	1.3854		
0.027	1.0274	0.077	1.0800	0.127	1.1354	0.177	1.1936	0.227	1.2548	0.277	1.3192	0.327	1.3868		
0.028	1.0284	0.078	1.0811	0.128	1.1366	0.178	1.1948	0.228	1.2561	0.278	1.3205	0.328	1.3882		
0.029	1.0294	0.079	1.0822	0.129	1.1377	0.179	1.1960	0.229	1.2573	0.279	1.3218	0.329	1.3896		
0.030	1.0305	0.080	1.0833	0.130	1.1388	0.180	1.1972	0.230	1.2586	0.280	1.3231	0.330	1.3910		
0.031	1.0315	0.081	1.0844	0.131	1.1400	0.181	1.1984	0.231	1.2599	0.281	1.3245	0.331	1.3924		
0.032	1.0325	0.082	1.0855	0.132	1.1411	0.182	1.1996	0.232	1.2611	0.282	1.3258	0.332	1.3938		
0.033	1.0336	0.083	1.0865	0.133	1.1422	0.183	1.2008	0.233	1.2624	0.283	1.3271	0.333	1.3951		
0.034	1.0346	0.084	1.0876	0.134	1.1434	0.184	1.2020	0.234	1.2636	0.284	1.3284	0.334	1.3965		
0.035	1.0356	0.085	1.0887	0.135	1.1445	0.185	1.2032	0.235	1.2649	0.285	1.3298	0.335	1.3979		
0.036	1.0367	0.086	1.0898	0.136	1.1457	0.186	1.2044	0.236	1.2662	0.286	1.3311	0.336	1.3993		
0.037	1.0377	0.087	1.0909	0.137	1.1468	0.187	1.2056	0.237	1.2674	0.287	1.3324	0.337	1.4007		
0.038	1.0387	0.088	1.0920	0.138	1.1480	0.188	1.2068	0.238	1.2687	0.288	1.3338	0.338	1.4021		
0.039	1.0398	0.089	1.0931	0.139	1.1491	0.189	1.2080	0.239	1.2700	0.289	1.3351	0.339	1.4035		
0.040	1.0408	0.090	1.0942	0.140	1.1503	0.190	1.2092	0.240	1.2712	0.290	1.3364	0.340	1.4049		
0.041	1.0419	0.091	1.0953	0.141	1.1514	0.191	1.2105	0.241	1.2725	0.291	1.3378	0.341	1.4064		
0.042	1.0429	0.092	1.0964	0.142	1.1526	0.192	1.2117	0.242	1.2738	0.292	1.3391	0.342	1.4078		
0.043	1.0439	0.093	1.0975	0.143	1.1537	0.193	1.2129	0.243	1.2751	0.293	1.3404	0.343	1.4092		
0.044	1.0450	0.094	1.0986	0.144	1.1549	0.194	1.2141	0.244	1.2763	0.294	1.3418	0.344	1.4106		
0.045	1.0460	0.095	1.0997	0.145	1.1560	0.195	1.2153	0.245	1.2776	0.295	1.3431	0.345	1.4120		
0.046	1.0471	0.096	1.1008	0.146	1.1572	0.196	1.2165	0.246	1.2789	0.296	1.3445	0.346	1.4134		
0.047	1.0481	0.097	1.1019	0.147	1.1584	0.197	1.2177	0.247	1.2802	0.297	1.3458	0.347	1.4148		
0.048	1.0492	0.098	1.1030	0.148	1.1595	0.198	1.2190	0.248	1.2815	0.298	1.3472	0.348	1.4162		
0.049	1.0502	0.099	1.1041	0.149	1.1607	0.199	1.2202	0.249	1.2827	0.299	1.3485	0.349	1.4176		
0.050	1.0513	0.100	1.1052	0.150	1.1618	0.200	1.2214	0.250	1.2840	0.300	1.3499	0.350	1.4191		

Future Value Interest Factor under Continuous Compounding

x	e <sup>x</sup>	x	e <sup>x</sup>	x	e <sup>x</sup>	x	e <sup>x</sup>	x	e <sup>x</sup>	x	e <sup>x</sup>
0.351	1.4205	0.401	1.4933	0.451	1.5699	0.501	1.6504	0.551	1.7350	0.601	1.8233
0.352	1.4219	0.402	1.4948	0.452	1.5715	0.502	1.6520	0.552	1.7367	0.602	1.8259
0.353	1.4233	0.403	1.4963	0.453	1.5730	0.503	1.6537	0.553	1.7385	0.603	1.8285
0.354	1.4248	0.404	1.4978	0.454	1.5746	0.504	1.6553	0.554	1.7402	0.604	1.8311
0.355	1.4262	0.405	1.4993	0.455	1.5762	0.505	1.6570	0.555	1.7419	0.605	1.8337
0.356	1.4276	0.406	1.5008	0.456	1.5778	0.506	1.6586	0.556	1.7437	0.606	1.8363
0.357	1.4290	0.407	1.5023	0.457	1.5793	0.507	1.6603	0.557	1.7454	0.607	1.8389
0.358	1.4305	0.408	1.5038	0.458	1.5809	0.508	1.6620	0.558	1.7472	0.608	1.8415
0.359	1.4319	0.409	1.5053	0.459	1.5825	0.509	1.6636	0.559	1.7489	0.609	1.8441
0.360	1.4333	0.410	1.5068	0.460	1.5841	0.510	1.6653	0.560	1.7507	0.610	1.8467
0.361	1.4348	0.411	1.5083	0.461	1.5857	0.511	1.6670	0.561	1.7524	0.611	1.8493
0.362	1.4362	0.412	1.5098	0.462	1.5872	0.512	1.6686	0.562	1.7542	0.612	1.8519
0.363	1.4376	0.413	1.5113	0.463	1.5888	0.513	1.6703	0.563	1.7559	0.613	1.8545
0.364	1.4391	0.414	1.5129	0.464	1.5904	0.514	1.6720	0.564	1.7577	0.614	1.8571
0.365	1.4405	0.415	1.5144	0.465	1.5920	0.515	1.6736	0.565	1.7594	0.615	1.8597
0.366	1.4420	0.416	1.5159	0.466	1.5936	0.516	1.6753	0.566	1.7612	0.616	1.8623
0.367	1.4434	0.417	1.5174	0.467	1.5952	0.517	1.6770	0.567	1.7630	0.617	1.8649
0.368	1.4448	0.418	1.5189	0.468	1.5968	0.518	1.6787	0.568	1.7647	0.618	1.8675
0.369	1.4463	0.419	1.5204	0.469	1.5984	0.519	1.6803	0.569	1.7665	0.619	1.8701
0.370	1.4477	0.420	1.5220	0.470	1.6000	0.520	1.6820	0.570	1.7683	0.620	1.8727
0.371	1.4492	0.421	1.5235	0.471	1.6016	0.521	1.6837	0.571	1.7700	0.621	1.8753
0.372	1.4506	0.422	1.5250	0.472	1.6032	0.522	1.6854	0.572	1.7718	0.622	1.8779
0.373	1.4521	0.423	1.5265	0.473	1.6048	0.523	1.6871	0.573	1.7736	0.623	1.8805
0.374	1.4535	0.424	1.5281	0.474	1.6064	0.524	1.6888	0.574	1.7754	0.624	1.8831
0.375	1.4550	0.425	1.5296	0.475	1.6080	0.525	1.6905	0.575	1.7771	0.625	1.8857
0.376	1.4564	0.426	1.5311	0.476	1.6096	0.526	1.6922	0.576	1.7789	0.626	1.8883
0.377	1.4579	0.427	1.5327	0.477	1.6112	0.527	1.6938	0.577	1.7807	0.627	1.8909
0.378	1.4594	0.428	1.5342	0.478	1.6128	0.528	1.6955	0.578	1.7825	0.628	1.8935
0.379	1.4608	0.429	1.5357	0.479	1.6145	0.529	1.6972	0.579	1.7843	0.629	1.8961
0.380	1.4623	0.430	1.5373	0.480	1.6161	0.530	1.6989	0.580	1.7860	0.630	1.8987
0.381	1.4637	0.431	1.5388	0.481	1.6177	0.531	1.7006	0.581	1.7878	0.631	1.9013
0.382	1.4652	0.432	1.5403	0.482	1.6193	0.532	1.7023	0.582	1.7896	0.632	1.9039
0.383	1.4667	0.433	1.5419	0.483	1.6209	0.533	1.7040	0.583	1.7914	0.633	1.9065
0.384	1.4681	0.434	1.5434	0.484	1.6226	0.534	1.7057	0.584	1.7932	0.634	1.9091
0.385	1.4696	0.435	1.5450	0.485	1.6242	0.535	1.7074	0.585	1.7950	0.635	1.9117
0.386	1.4711	0.436	1.5465	0.486	1.6258	0.536	1.7092	0.586	1.7968	0.636	1.9143
0.387	1.4726	0.437	1.5481	0.487	1.6274	0.537	1.7109	0.587	1.7986	0.637	1.9169
0.388	1.4740	0.438	1.5496	0.488	1.6291	0.538	1.7126	0.588	1.8004	0.638	1.9195
0.389	1.4755	0.439	1.5512	0.489	1.6307	0.539	1.7143	0.589	1.8022	0.639	1.9221
0.390	1.4770	0.440	1.5527	0.490	1.6323	0.540	1.7160	0.590	1.8040	0.640	1.9247
0.391	1.4785	0.441	1.5543	0.491	1.6339	0.541	1.7177	0.591	1.8058	0.641	1.9273
0.392	1.4799	0.442	1.5558	0.492	1.6356	0.542	1.7194	0.592	1.8076	0.642	1.9299
0.393	1.4814	0.443	1.5574	0.493	1.6372	0.543	1.7212	0.593	1.8094	0.643	1.9325
0.394	1.4829	0.444	1.5589	0.494	1.6389	0.544	1.7229	0.594	1.8112	0.644	1.9351
0.395	1.4844	0.445	1.5605	0.495	1.6405	0.545	1.7246	0.595	1.8130	0.645	1.9377
0.396	1.4859	0.446	1.5621	0.496	1.6421	0.546	1.7263	0.596	1.8148	0.646	1.9403
0.397	1.4874	0.447	1.5636	0.497	1.6438	0.547	1.7281	0.597	1.8167	0.647	1.9429
0.398	1.4888	0.448	1.5652	0.498	1.6454	0.548	1.7298	0.598	1.8185	0.648	1.9455
0.399	1.4903	0.449	1.5667	0.499	1.6471	0.549	1.7315	0.599	1.8203	0.649	1.9481
0.400	1.4918	0.450	1.5683	0.500	1.6487	0.550	1.7333	0.600	1.8221	0.650	1.9507

Financial Tables

Future Value Interest Factor under Continuous Compounding

x	e <sup>x</sup>	x	e <sup>x</sup>	x	e <sup>x</sup>	x	e <sup>x</sup>	x	e <sup>x</sup>	x	e <sup>x</sup>	x	e <sup>x</sup>	x	e <sup>x</sup>
0.651	1.9175	0.701	2.0158	0.751	2.1191	0.801	2.2278	0.851	2.3420	0.901	2.4621	0.951	2.5883	1.000	2.7183
0.652	1.9194	0.702	2.0178	0.752	2.1212	0.802	2.2300	0.852	2.3443	0.902	2.4645	0.952	2.5909		
0.653	1.9213	0.703	2.0198	0.753	2.1234	0.803	2.2322	0.853	2.3467	0.903	2.4670	0.953	2.5935		
0.654	1.9232	0.704	2.0218	0.754	2.1255	0.804	2.2345	0.854	2.3490	0.904	2.4695	0.954	2.5961		
0.655	1.9251	0.705	2.0238	0.755	2.1276	0.805	2.2367	0.855	2.3514	0.905	2.4719	0.955	2.5987		
0.656	1.9271	0.706	2.0259	0.756	2.1297	0.806	2.2389	0.856	2.3537	0.906	2.4744	0.956	2.6013		
0.657	1.9290	0.707	2.0279	0.757	2.1319	0.807	2.2412	0.857	2.3561	0.907	2.4769	0.957	2.6039		
0.658	1.9309	0.708	2.0299	0.758	2.1340	0.808	2.2434	0.858	2.3584	0.908	2.4794	0.958	2.6065		
0.659	1.9329	0.709	2.0320	0.759	2.1361	0.809	2.2457	0.859	2.3608	0.909	2.4818	0.959	2.6091		
0.660	1.9348	0.710	2.0340	0.760	2.1383	0.810	2.2479	0.860	2.3632	0.910	2.4843	0.960	2.6117		
0.661	1.9367	0.711	2.0360	0.761	2.1404	0.811	2.2502	0.861	2.3655	0.911	2.4868	0.961	2.6143		
0.662	1.9387	0.712	2.0381	0.762	2.1426	0.812	2.2524	0.862	2.3679	0.912	2.4893	0.962	2.6169		
0.663	1.9406	0.713	2.0401	0.763	2.1447	0.813	2.2547	0.863	2.3703	0.913	2.4918	0.963	2.6195		
0.664	1.9425	0.714	2.0421	0.764	2.1468	0.814	2.2569	0.864	2.3726	0.914	2.4943	0.964	2.6222		
0.665	1.9445	0.715	2.0442	0.765	2.1490	0.815	2.2592	0.865	2.3750	0.915	2.4968	0.965	2.6248		
0.666	1.9464	0.716	2.0462	0.766	2.1511	0.816	2.2614	0.866	2.3774	0.916	2.4993	0.966	2.6274		
0.667	1.9484	0.717	2.0483	0.767	2.1533	0.817	2.2637	0.867	2.3798	0.917	2.5018	0.967	2.6300		
0.668	1.9503	0.718	2.0503	0.768	2.1555	0.818	2.2660	0.868	2.3821	0.918	2.5043	0.968	2.6327		
0.669	1.9523	0.719	2.0524	0.769	2.1576	0.819	2.2682	0.869	2.3845	0.919	2.5068	0.969	2.6353		
0.670	1.9542	0.720	2.0544	0.770	2.1598	0.820	2.2705	0.870	2.3869	0.920	2.5093	0.970	2.6379		
0.671	1.9562	0.721	2.0565	0.771	2.1619	0.821	2.2728	0.871	2.3893	0.921	2.5118	0.971	2.6406		
0.672	1.9581	0.722	2.0585	0.772	2.1641	0.822	2.2750	0.872	2.3917	0.922	2.5143	0.972	2.6432		
0.673	1.9601	0.723	2.0606	0.773	2.1663	0.823	2.2773	0.873	2.3941	0.923	2.5168	0.973	2.6459		
0.674	1.9621	0.724	2.0627	0.774	2.1684	0.824	2.2796	0.874	2.3965	0.924	2.5193	0.974	2.6485		
0.675	1.9640	0.725	2.0647	0.775	2.1706	0.825	2.2819	0.875	2.3989	0.925	2.5219	0.975	2.6512		
0.676	1.9660	0.726	2.0668	0.776	2.1728	0.826	2.2842	0.876	2.4013	0.926	2.5244	0.976	2.6538		
0.677	1.9680	0.727	2.0689	0.777	2.1749	0.827	2.2864	0.877	2.4037	0.927	2.5269	0.977	2.6565		
0.678	1.9699	0.728	2.0709	0.778	2.1771	0.828	2.2887	0.878	2.4061	0.928	2.5294	0.978	2.6591		
0.679	1.9719	0.729	2.0730	0.779	2.1793	0.829	2.2910	0.879	2.4085	0.929	2.5320	0.979	2.6618		
0.680	1.9739	0.730	2.0751	0.780	2.1815	0.830	2.2933	0.880	2.4109	0.930	2.5345	0.980	2.6645		
0.681	1.9759	0.731	2.0772	0.781	2.1837	0.831	2.2956	0.881	2.4133	0.931	2.5370	0.981	2.6671		
0.682	1.9778	0.732	2.0792	0.782	2.1858	0.832	2.2979	0.882	2.4157	0.932	2.5396	0.982	2.6698		
0.683	1.9798	0.733	2.0813	0.783	2.1880	0.833	2.3002	0.883	2.4181	0.933	2.5421	0.983	2.6725		
0.684	1.9818	0.734	2.0834	0.784	2.1902	0.834	2.3025	0.884	2.4206	0.934	2.5447	0.984	2.6751		
0.685	1.9838	0.735	2.0855	0.785	2.1924	0.835	2.3048	0.885	2.4230	0.935	2.5472	0.985	2.6778		
0.686	1.9858	0.736	2.0876	0.786	2.1946	0.836	2.3071	0.886	2.4254	0.936	2.5498	0.986	2.6805		
0.687	1.9877	0.737	2.0897	0.787	2.1968	0.837	2.3094	0.887	2.4278	0.937	2.5523	0.987	2.6832		
0.688	1.9897	0.738	2.0917	0.788	2.1990	0.838	2.3117	0.888	2.4303	0.938	2.5549	0.988	2.6859		
0.689	1.9917	0.739	2.0938	0.789	2.2012	0.839	2.3141	0.889	2.4327	0.939	2.5574	0.989	2.6885		
0.690	1.9937	0.740	2.0959	0.790	2.2034	0.840	2.3164	0.890	2.4351	0.940	2.5600	0.990	2.6912		
0.691	1.9957	0.741	2.0980	0.791	2.2056	0.841	2.3187	0.891	2.4376	0.941	2.5625	0.991	2.6939		
0.692	1.9977	0.742	2.1001	0.792	2.2078	0.842	2.3210	0.892	2.4400	0.942	2.5651	0.992	2.6966		
0.693	1.9997	0.743	2.1022	0.793	2.2100	0.843	2.3233	0.893	2.4424	0.943	2.5677	0.993	2.6993		
0.694	2.0017	0.744	2.1043	0.794	2.2122	0.844	2.3257	0.894	2.4449	0.944	2.5702	0.994	2.7020		
0.695	2.0037	0.745	2.1064	0.795	2.2144	0.845	2.3280	0.895	2.4473	0.945	2.5728	0.995	2.7047		
0.696	2.0057	0.746	2.1085	0.796	2.2167	0.846	2.3303	0.896	2.4498	0.946	2.5754	0.996	2.7074		
0.697	2.0077	0.747	2.1107	0.797	2.2189	0.847	2.3326	0.897	2.4522	0.947	2.5780	0.997	2.7101		
0.698	2.0097	0.748	2.1128	0.798	2.2211	0.848	2.3350	0.898	2.4547	0.948	2.5805	0.998	2.7129		
0.699	2.0117	0.749	2.1149	0.799	2.2233	0.849	2.3373	0.899	2.4571	0.949	2.5831	0.999	2.7156		
0.700	2.0138	0.750	2.1170	0.800	2.2255	0.850	2.3396	0.900	2.4596	0.950	2.5857				

Natural Logarithms

x	Ln(x)
0.01	-4.6052
0.02	-3.9120
0.03	-3.5066
0.04	-3.2189
0.05	-2.9957
0.06	-2.8134
0.07	-2.6593
0.08	-2.5257
0.09	-2.4079
0.10	-2.3026
0.11	-2.2073
0.12	-2.1203
0.13	-2.0402
0.14	-1.9661
0.15	-1.8971
0.16	-1.8326
0.17	-1.7720
0.18	-1.7148
0.19	-1.6607
0.20	-1.6094
0.21	-1.5606
0.22	-1.5141
0.23	-1.4697
0.24	-1.4271
0.25	-1.3863
0.26	-1.3471
0.27	-1.3093
0.28	-1.2730
0.29	-1.2379
0.30	-1.2040
0.31	-1.1712
0.32	-1.1394
0.33	-1.1087
0.34	-1.0788
0.35	-1.0498
0.36	-1.0217
0.37	-0.9943
0.38	-0.9676
0.39	-0.9416
0.40	-0.9163
0.41	-0.8916
0.42	-0.8675
0.43	-0.8440
0.44	-0.8210
0.45	-0.7985
0.46	-0.7765
0.47	-0.7550
0.48	-0.7340
0.49	-0.7133
0.50	-0.6931

x	Ln(x)
0.51	-0.6733
0.52	-0.6539
0.53	-0.6349
0.54	-0.6162
0.55	-0.5978
0.56	-0.5798
0.57	-0.5621
0.58	-0.5447
0.59	-0.5276
0.60	-0.5108
0.61	-0.4943
0.62	-0.4780
0.63	-0.4620
0.64	-0.4463
0.65	-0.4308
0.66	-0.4155
0.67	-0.4005
0.68	-0.3857
0.69	-0.3711
0.70	-0.3567
0.71	-0.3425
0.72	-0.3285
0.73	-0.3147
0.74	-0.3011
0.75	-0.2877
0.76	-0.2744
0.77	-0.2614
0.78	-0.2485
0.79	-0.2357
0.80	-0.2231
0.81	-0.2107
0.82	-0.1985
0.83	-0.1863
0.84	-0.1744
0.85	-0.1625
0.86	-0.1508
0.87	-0.1393
0.88	-0.1278
0.89	-0.1165
0.90	-0.1054
0.91	-0.0943
0.92	-0.0834
0.93	-0.0726
0.94	-0.0619
0.95	-0.0513
0.96	-0.0408
0.97	-0.0305
0.98	-0.0202
0.99	-0.0101
1.00	0.0000

x	Ln(x)
1.01	0.0100
1.02	0.0198
1.03	0.0296
1.04	0.0392
1.05	0.0488
1.06	0.0583
1.07	0.0677
1.08	0.0770
1.09	0.0862
1.10	0.0953
1.11	0.1044
1.12	0.1133
1.13	0.1222
1.14	0.1310
1.15	0.1398
1.16	0.1484
1.17	0.1570
1.18	0.1655
1.19	0.1740
1.20	0.1823
1.21	0.1906
1.22	0.1989
1.23	0.2070
1.24	0.2151
1.25	0.2231
1.26	0.2311
1.27	0.2390
1.28	0.2469
1.29	0.2546
1.30	0.2624
1.31	0.2700
1.32	0.2776
1.33	0.2852
1.34	0.2927
1.35	0.3001
1.36	0.3075
1.37	0.3148
1.38	0.3221
1.39	0.3293
1.40	0.3365
1.41	0.3436
1.42	0.3507
1.43	0.3577
1.44	0.3646
1.45	0.3716
1.46	0.3784
1.47	0.3853
1.48	0.3920
1.49	0.3988
1.50	0.4055

x	Ln(x)
1.51	0.4121
1.52	0.4187
1.53	0.4253
1.54	0.4318
1.55	0.4383
1.56	0.4447
1.57	0.4511
1.58	0.4574
1.59	0.4637
1.60	0.4700
1.61	0.4762
1.62	0.4824
1.63	0.4886
1.64	0.4947
1.65	0.5008
1.66	0.5068
1.67	0.5128
1.68	0.5188
1.69	0.5247
1.70	0.5306
1.71	0.5365
1.72	0.5423
1.73	0.5481
1.74	0.5539
1.75	0.5596
1.76	0.5653
1.77	0.5710
1.78	0.5766
1.79	0.5822
1.80	0.5878
1.81	0.5933
1.82	0.5988
1.83	0.6043
1.84	0.6098
1.85	0.6152
1.86	0.6206
1.87	0.6259
1.88	0.6313
1.89	0.6366
1.90	0.6419
1.91	0.6471
1.92	0.6523
1.93	0.6575
1.94	0.6627
1.95	0.6678
1.96	0.6729
1.97	0.6780
1.98	0.6831
1.99	0.6881
2.00	0.6931

x	Ln(x)
2.10	0.7410
2.20	0.7850
2.30	0.8320
2.40	0.8750
2.50	0.9160
2.60	0.9550
2.70	0.9930
2.80	1.0290
2.90	1.0640
3.00	1.0980
3.10	1.1310
3.20	1.1630
3.30	1.1930
3.40	1.2230
3.50	1.2520
3.60	1.2800
3.70	1.3080
3.80	1.3350
3.90	1.3610
4.00	1.3860
4.10	1.4110
4.20	1.4350
4.30	1.4580
4.40	1.4810
4.50	1.5040
4.60	1.5260
4.70	1.5470
4.80	1.5680
4.90	1.5890
5.00	1.6090
6.00	1.7910
6.50	1.8710
7.00	1.9450
7.50	2.0140
8.00	2.0790
8.50	2.1400
9.00	2.1970
9.50	2.2510
10.00	2.3020
11.00	2.3970
12.00	2.4840
13.00	2.5640
14.00	2.6390
15.00	2.7080
16.00	2.7720
17.00	2.8330
18.00	2.8900
19.00	2.9440
20.00	2.9950

Area under the Normal Curve

Z Value	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.0000									
0.1	0.0398									
0.2	0.0793	0.0438								
0.3	0.1179	0.0832	0.0478							0.0753
0.4	0.1554	0.1217	0.0871	0.0517	0.0557	0.0596	0.0636	0.0675	0.0714	0.1141
0.5	0.1915	0.1591	0.1255	0.0910	0.0948	0.0987	0.1026	0.1064	0.1103	0.1517
0.6	0.2257	0.1950	0.1628	0.1293	0.1331	0.1368	0.1406	0.1443	0.1480	0.1879
0.7	0.2580	0.2291	0.1985	0.1664	0.1700	0.1736	0.1772	0.1808	0.1844	0.2224
0.8	0.2881	0.2611	0.2324	0.2019	0.2054	0.2088	0.2123	0.2157	0.2190	0.2549
0.9	0.3159	0.2910	0.2642	0.2357	0.2389	0.2422	0.2454	0.2486	0.2517	0.2852
1.0	0.3413	0.3186	0.2939	0.2673	0.2704	0.2734	0.2764	0.2794	0.2823	0.3133
1.1	0.3643	0.3438	0.3212	0.2967	0.2995	0.3023	0.3051	0.3078	0.3106	0.3389
1.2	0.3849	0.3665	0.3461	0.3238	0.3264	0.3289	0.3315	0.3340	0.3365	0.3621
1.3	0.4032	0.3869	0.3686	0.3485	0.3508	0.3531	0.3554	0.3577	0.3599	0.3830
1.4	0.4192	0.4049	0.3888	0.3708	0.3729	0.3749	0.3770	0.3790	0.3810	0.4015
1.5	0.4332	0.4207	0.4066	0.3907	0.3925	0.3944	0.3962	0.3980	0.3997	0.4177
1.6	0.4452	0.4345	0.4222	0.4082	0.4099	0.4115	0.4131	0.4147	0.4162	0.4319
1.7	0.4554	0.4463	0.4357	0.4236	0.4251	0.4265	0.4279	0.4292	0.4306	0.4441
1.8	0.4641	0.4564	0.4474	0.4370	0.4382	0.4394	0.4406	0.4418	0.4429	0.4545
1.9	0.4713	0.4649	0.4573	0.4484	0.4495	0.4505	0.4515	0.4525	0.4535	0.4633
2.0	0.4772	0.4719	0.4656	0.4582	0.4591	0.4599	0.4608	0.4616	0.4625	0.4706
2.1	0.4821	0.4778	0.4726	0.4664	0.4671	0.4678	0.4686	0.4693	0.4699	0.4767
2.2	0.4861	0.4826	0.4783	0.4732	0.4738	0.4744	0.4750	0.4756	0.4761	0.4817
2.3	0.4893	0.4864	0.4830	0.4788	0.4793	0.4798	0.4803	0.4808	0.4812	0.4857
2.4	0.4918	0.4896	0.4868	0.4834	0.4838	0.4842	0.4846	0.4850	0.4854	0.4890
2.5	0.4938	0.4920	0.4898	0.4871	0.4875	0.4878	0.4881	0.4884	0.4887	0.4916
2.6	0.4953	0.4940	0.4922	0.4901	0.4904	0.4906	0.4909	0.4911	0.4913	0.4936
2.7	0.4965	0.4955	0.4941	0.4925	0.4927	0.4929	0.4931	0.4932	0.4934	0.4952
2.8	0.4974	0.4966	0.4956	0.4943	0.4945	0.4946	0.4948	0.4949	0.4951	0.4964
2.9	0.4981	0.4975	0.4967	0.4957	0.4959	0.4960	0.4961	0.4962	0.4963	0.4974
3.0	0.4987	0.4977	0.4976	0.4968	0.4969	0.4970	0.4971	0.4972	0.4973	0.4981
3.1	0.4990	0.4982	0.4982	0.4977	0.4977	0.4978	0.4979	0.4979	0.4980	0.4981
3.2	0.4993	0.4987	0.4987	0.4983	0.4983	0.4984	0.4984	0.4985	0.4985	0.4986
3.3	0.4995	0.4987	0.4987	0.4988	0.4988	0.4988	0.4989	0.4989	0.4989	0.4986
3.4	0.4997	0.4987	0.4987	0.4988	0.4988	0.4989	0.4989	0.4989	0.4990	0.4990
3.5	0.4998	0.4987	0.4987	0.4988	0.4988	0.4989	0.4989	0.4989	0.4990	0.4990
3.6	0.4998	0.4987	0.4987	0.4988	0.4988	0.4989	0.4989	0.4989	0.4990	0.4990
3.7	0.4999	0.4987	0.4987	0.4988	0.4988	0.4989	0.4989	0.4989	0.4990	0.4990
3.8	0.4999	0.4987	0.4987	0.4988	0.4988	0.4989	0.4989	0.4989	0.4990	0.4990
3.9	0.5000	0.4987	0.4987	0.4988	0.4988	0.4989	0.4989	0.4989	0.4990	0.4990
4.0	0.5000	0.4987	0.4987	0.4988	0.4988	0.4989	0.4989	0.4989	0.4990	0.4990

Note: For computation, use 0.50 ± Above Values, depending upon whether Z is positive or negative.

## Fast Track Referencer

### Ratios, Proportions, Indices & Logarithms

#### A. Proportions

- Equality of two ratios is called a proportion. If the terms  $a, b, c, d$  are in proportion, then  $a:b = c:d$ , or  $ad = bc$ .
- Mean Proportional of three terms:** If  $a, b, c$  are in continued proportion then,  $\frac{a}{b} = \frac{b}{c}$ . Therefore,  $b^2 = ac$ .

$b = \sqrt{ab} \Rightarrow b = \sqrt{ac}$ . Hence  $b$  is itself the Mean Proportional between  $a$  and  $c$ .

Result	Property
1. $b : a = d : c$	Invertendo
2. $a : c = b : d$	Alternendo
3. $(a + b) : b = (c + d) : d$	Componendo
4. $(a - b) : b = (c - d) : d$	Dividendo
5. $(a + b) : (a - b) = (c + d) : (c - d)$	Componendo and Dividendo
6. $a:b = c:d = (a+c) : (b+d)$	Addendo
7. $a:b = c:d = (a-c) : (b-d)$	Subtrahendo

#### B. Indices

1. $a^m \times a^n = a^{m+n}$	4. $(ab)^m = a^m b^m$	7. $a^x = a^y \Rightarrow x = y$
2. $\frac{a^m}{a^n} = a^{m-n}$	5. $a^0 = 1$	8. $x^a = y^a \Rightarrow x = y$
3. $(a^m)^n = a^{mn} = (a^n)^m$	6. $a^{-m} = \frac{1}{a^m}$	9. $\sqrt[m]{a} = a^{\frac{1}{m}}$

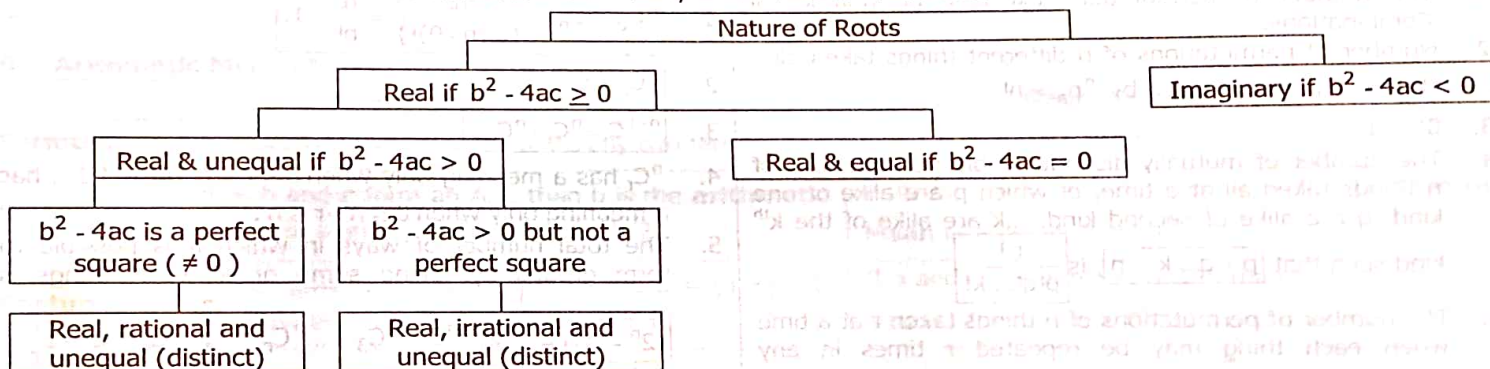
#### C. Logarithms:

1. If $a^x = n$ , then $\log_a n = x$	5. $\log_a m^n = n \log_a m$	9. $\log_b a = \frac{1}{\log_a b}$
2. $\log_a a = 1$	6. $\log_a m = \log_b m \times \log_a b$	10. $a^{\log_a x} = x$
3. $\log_a mn = \log_a m + \log_a n$	7. $\log_a 1 = 0$	11. $\log 10 = 1$
4. $\log_a \left(\frac{m}{n}\right) = \log_a m - \log_a n$	8. $\log_b a \times \log_a b = 1$	

**Note:** Log using base 10 is called Common Logarithm. Log using base  $e$  is called Natural Logarithm. [ $e = \text{Exponent} \approx 2.33$ ]

## Equations

- Roots of the quadratic equation shall be identified by:  $\alpha = \frac{-b + \sqrt{b^2 - 4ac}}{2a}$ ;  $\beta = \frac{-b - \sqrt{b^2 - 4ac}}{2a}$
- Discriminant =  $b^2 - 4ac$ . It is called as Discriminant, since it discriminates between the roots,  $\alpha, \beta$ .



1. Irrational roots occur in pairs, i.e. if  $(m + \sqrt{n})$  is a root then  $(m - \sqrt{n})$  is the other root of the same equation.
2. If one root is reciprocal to the other root then their product is 1 and so  $\frac{c}{a} = 1$ , i.e.  $c = a$
3. If one root is equal to other root but opposite in sign then, their sum = 0 and so  $\frac{b}{a} = 0$ , i.e.  $b = 0$ .

## Time Value of Money

### A. Simple Interest & Compound Interest

	Simple Interest	Compound Interest
<b>Interest</b>	$P \times N \times R$	$P(1+R)^n - P = P[(1+R)^n - 1]$
<b>Amount</b>	$A = P [1 + (N \times R)]$	$A = P(1 + I/K)^{NK}$
<b>Principal</b>	$P = A \div [1 + (N \times R)]$	$P = A \div (1 + I/K)^{NK}$

$$\text{Effective Interest Rate} = \frac{\text{Actual Interest Paid During the Year}}{\text{Opening Principal of the Year}} = \frac{\text{Closing Amount} - \text{Opening Principal}}{\text{Opening Principal of the Year}} = E = \left(1 + \frac{i}{k}\right)^k - 1$$

### B. Annuity

	Annuity Regular (Year end)	Annuity Immediate (Year beginning)
<b>Present Value (PV)</b>	$PV = CF \left[ \frac{(1+i)^n - 1}{i(1+i)^n} \right]$	$PV = CF \left[ \frac{(1+i)^n - 1}{i(1+i)^n} \right] \times (1+i)$
<b>Future Value (FV)</b>	$A = CF \left[ \frac{(1+i)^n - 1}{i} \right]$	$A = CF \left[ \frac{(1+i)^n - 1}{i} \right] \times (1+i)$
<b>PV using Factors</b>	$PV = CF \times \text{PVAF @ } r\% \text{ for } n \text{ periods}$	$PV = CF \times [\text{PVAF @ } r\% \text{ for } (n-1) \text{ periods} + 1]$
<b>FV using Factors</b>	$FV = CF \times [\text{FVAF @ } r\% \text{ for } (n-1) \text{ periods} + 1]$	$FV = CF \times \text{FVAF @ } r\% \text{ for } n \text{ periods}$

### C. Perpetuity

PV of a **Constant** Perpetuity =  $\frac{C}{R}$

Where **C** = Cash Flow, i.e. Interest, Dividend, etc. per period.  
**R** = Interest Rate per payment period.

PV of a **Growing** Perpetuity =  $\frac{C}{R - G}$

Where **C** = Cash Flow, i.e. Interest, Dividend, etc. for the first period  
**R** = Interest Rate per payment period.  
**G** = Rate of growth in Cash Flows.

## Permutations & Combinations

Permutations	Combinations
<ol style="list-style-type: none"> <li>1. The number of Permutations exceeds the number of Combinations.</li> <li>2. Number of permutations of <math>n</math> different things taken all <math>n</math> things at a time is given by <math>{}^n P_n = n!</math></li> <li>3. <math>0! = 1</math>.</li> <li>4. The number of mutually distinguishable permutations of <math>n</math> things taken all at a time, of which <math>p</math> are alike of one kind, <math>q</math> are alike of second kind, ...<math>k</math> are alike of the <math>k^{\text{th}}</math> kind such that <math>p + q + \dots + k = n</math>, is <math>\frac{n!}{p!q!\dots k!}</math></li> <li>5. The number of permutations of <math>n</math> things taken <math>r</math> at a time when each thing may be repeated <math>r</math> times in any arrangement is <math>[n^r]</math>.</li> </ol>	<ol style="list-style-type: none"> <li>1. <math>{}^n C_0 = {}^n C_n = \frac{n!}{\{0!(n-0)!\}} = \frac{n!}{n!} = 1</math>.</li> <li>2. <math>{}^n C_r = {}^n C_{n-r}</math></li> <li>3. <math>{}^{n+1} C_r = {}^n C_r + {}^n C_{r-1}</math></li> <li>4. <math>{}^n C_r</math> has a meaning only when <math>0 \leq r \leq n</math>. Also <math>{}^n C_{n-r}</math> has a meaning only when <math>0 \leq n-r \leq n</math>.</li> <li>5. The total number of ways in which it is possible to form groups by taking some or all of <math>n</math> things is <math>(2^n - 1)</math> i.e. <math>{}^n C_1 + {}^n C_2 + {}^n C_3 + \dots + {}^n C_n = \sum_{r=1}^n {}^n C_r = 2^n - 1</math>.</li> </ol>



6. Total number of Circular Permutations =  $(n-1)!$   
 7. Circular Permutations such that a person shall not have the same neighbor in any two arrangements =  $\frac{1}{2}(n-1)!$

8.  ${}^n P_r = n \cdot {}^{n-1} P_{r-1}$   
 9.  ${}^n P_r = (n-r+1) \times {}^n P_{r-1}$   
 10.  ${}^n P_r = {}^{n-1} P_{r+r} \cdot {}^{n-1} P_{r-1}$  [Note]

6. The total number of ways in which it is possible to make groups by taking some or all out of  $n = (n_1+n_2+n_3+\dots)$  things, where  $n_1, n_2, n_3$  are things each alike of one kind, is given by  $\{(n_1+1)(n_2+1)(n_3+1)\dots\}-1$ .  
 7.  ${}^n C_r$  and  ${}^n C_{n-r}$  are called complementary combinations, for if we form a group of  $r$  things out of  $n$  different things,  $(n-r)$  remaining things which are not included in this group form another group of rejected things.

**Note:**  ${}^{n-1} P_r$  is the No. of Permutations of  $n$  distinct objects when a particular object is not taken in any arrangement, and  $r \cdot {}^{n-1} P_{r-1}$  is the No. of permutations of  $n$  distinct objects when a particular object is always included in any arrangement.

## Arithmetic & Geometric Progression (AP & GP)

### A. Arithmetic Progressions (AP) vs. Geometric Progression (GP)

	Arithmetic Progressions (AP)	Geometric Progression (GP)
<b>3 Parts</b>	$a-d, a, a+d$	$a/r, a, ar$
<b>nth term</b>	$t_n = a + (n-1)d$ Where 'a' is the first term 'd' is the common difference	$t_n = ar^{n-1}$ Where 'a' is the first term 'r' is the common ratio
<b>Sum (<math>S_n</math>) of n terms</b>	$S_n = \frac{n}{2}\{2a + (n-1)d\}$ or $S_n = \frac{n}{2}\{a+l\}$ Where l is the last term = $a + (n-1)d$	$S_n = a\left(\frac{r^n-1}{r-1}\right)$ if $r > 1$ or $S_n = \frac{r^n a - a}{r-1}$ $S_n = a\left(\frac{1-r^n}{1-r}\right)$ , if $r < 1$ or $S_n = \frac{a-lr}{1-r}$   = Last term
<b>Infinite Progression</b>	Refer Table Below [Note]	$S_\infty = \frac{a}{1-r}$ , for $r < 1$

Situation	Formulae
1. Sum of 1 <sup>st</sup> n Natural Numbers	$\sum_{n=1}^n n = 1 + 2 + 3 + \dots + n = \frac{n(n+1)}{2}$
2. Sum of 1 <sup>st</sup> n Odd Numbers	$1 + 3 + 5 + \dots + (2n-1) = n^2$
3. Sum of the squares of 1 <sup>st</sup> n Natural Numbers	$\sum_{n=1}^n n^2 = 1^2 + 2^2 + 3^2 + \dots + n^2 = \frac{n(n+1)(2n+1)}{6}$
4. Sum of the cubes of 1 <sup>st</sup> n Natural Numbers	$\sum_{n=1}^n n^3 = 1^3 + 2^3 + 3^3 + \dots + n^3 = \left[\frac{n(n+1)}{2}\right]^2$

### B. Arithmetic Mean (AM) vs Geometric Mean (GM)

	Arithmetic Mean (AM)	Geometric Mean (GM)
<b>Formula</b>	$A = (a+b)/2$ , where a and b are any two terms.	$G = \sqrt{ab}$ , where a and b are any two terms.
<b>Meaning</b>	If a, b and c form an A.P. then b is the <b>arithmetic mean</b> of a and c, where $b = (a+c)/2$ .	If a, b, c are in G.P., then b is the <b>Geometric Mean</b> of a and c, then $b^2 = ac$ or $b = \sqrt{ac}$ .
<b>Features</b>	If the terms a and c are in A.P. and $b = (a+c)/2$ , then the terms a, b, c also form an A.P.	If a and c are terms of a G.P. then terms a, b, c are also in GP where $b = GM$ of a and $c = \sqrt{ac}$