## CA INTERMEDIATE

# FINANCIAL MANAGEMENT 

## VOLUME II

## By

## CA. Namit Arora Sir

## This book is dedicated to my Father

## 'MR. SURESK KUMAR ARORA'

## ABOUT THE AUTHOR

Mr. Namit Arora is a First class commerce graduate and member of The Institute of Chartered Accountants of India (ICAI). He has cleared both groups of PCC examination and final examination in his first attempt.

He has vast experience of teaching even at such young age. He has taught large number of students of various professional courses such as CA, CS, CMA and also of undergraduate and post graduate course for university examinations. He is also author of Taxmann.

His specialized knowledge helps the students to understand the topic easily and his expert advice makes the revision very easy and fast.

He gives practical examples that help students to visualize the concepts and his teaching style is very famous among the students.

## PREFACE TO THIS EDITION

This is a comprehensive book having thoroughly explained concepts with lucid and systematic presentation of the subject matter. All attempts are made in this book to keep concept easier to understand and remember.

A special attention is given to presentation keeping in mind the examination needs to the student. The book is primarily written for CA - INTERMEDIATE exams.

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## A word to the students

My dear student, hard work is the key to success. Though smart work is publicized in today's world but to be smart, you have to work hard. So always be attentive in class and have thorough revision after the class. It is also important to be motivated and inspired for working hard. The key for success is:
"Work hard in class, be attentive and grab the concepts
\&
Work smart during revision, select important questions for next revision."

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## CHAPTER 7

## TRADITIONAL TECHNIQUES

## BQ 1

A project requiring an investment of $₹ 10,00,000$ and it yields profit after tax and depreciation which is as follows:

| Year | Profit after tax and depreciation (₹) |
| :---: | :---: |
| 1 | 50,000 |
| 2 | 75,000 |
| 3 | $1,25,000$ |
| 4 | $1,30,000$ |
| 5 | 80,000 |

At the end of the $5^{\text {th }}$ year, the plant and machinery of the project can be sold for ₹ 80,000 .
Determine Accounting (Book) Rate of Return.

## Answer

Alternative 1 (Average Investment Basis):
$\begin{array}{rll}\text { Accounting Rate of Return } & =\frac{\text { Average Profit After Tax }}{\text { Average Investment }} \times 100 \\ & =\frac{92,000}{5,40,000} \times 100 & =17.04 \%\end{array}$
Alternative 2 (Total Investment Basis):
Accounting Rate of Return $=\quad \frac{\text { Average Profit After Tax }}{\text { Initial Investment }} \times 100$
$=\frac{92,000}{10,00,000} \times 100 \quad=\quad 9.20 \%$

Alternative 3 (Annual Basis):
Accounting Rate of Return
$=\quad \frac{\text { Pr ofit After Tax }}{\text { Investment at the beginning of the year }} \times 100$
Year 1
$=\frac{50,000}{10,00,000} \times 100 \quad=\quad 5.00 \%$

Year 2
$=\frac{75,000}{8,16,000} \times 100$

Year 3
$=\quad \frac{1,25,000}{6,32,000} \times 100$
$=19.78 \%$

Year 4
$=\frac{1,30,000}{4,48,000} \times 100$
$=\quad 29.02 \%$

Year 5

$$
=\frac{80,000}{2,64,000} \times 100
$$

$$
=30.30 \%
$$

$$
\begin{array}{rll}
\text { Average } A R R \quad & = & (5 \%+9.19 \%+19.78 \%+29.02 \%+30.30 \%) \div 5 \text { years } \\
& =18.66 \%
\end{array}
$$

## Working Notes:

| Average Profit After Tax | $=$ | $(50,000+75,000+1,25,000+1,30,000+80,000) \div 5$ |
| :--- | :--- | :--- |
|  | $=92,000$ per annum |  |
| Average Investment | $=(10,00,000+80,000) \div 2=5,40,000$ |  |
| Depreciation per annum | $=(10,00,000-80,000) \div 5$ years $=1,84,000$ |  |

## BQ 2

Times Ltd. is going to invest in a project a sum of $₹ 3,00,000$ having a life span of 3 years. Salvage value of machine is $₹ 90,000$. The profit before depreciation for each year is $₹ 1,50,000$.

Determine Accounting (Book) Rate of Return.

## Answer

Alternative 1 (Average Investment Basis):
Accounting Rate of Return $=\quad \frac{\text { Average Profit After Tax }}{\text { Average Investment }} \times 100$
$=\frac{80,000}{1,95,000} \times 100=41.03 \%$
Alternative 2 (Total Investment Basis):
Accounting Rate of Return
$=\quad \frac{\text { Average Profit After Tax }}{\text { Initial Investment }} \times 100$
$=\frac{80,000}{3,00,000} \times 100=26.67 \%$

## Alternative 3 (Annual Basis):

Accounting Rate of Return
$=\quad \frac{\text { Profit After Tax }}{\text { Investment at the beginning of the year }} \times 100$

Year 1
$=\frac{80,000}{3,00,000} \times 100=26.67 \%$

Year 2
$=\frac{80,000}{2,30,000} \times 100=34.78 \%$

Year 3
$=\frac{80,000}{1,60,000} \times 100=\mathbf{5 0 . 0 0} \%$
Average ARR $\quad=\quad(26.67 \%+34.78 \%+50.00 \%) \div 3=37.15 \%$

## Working Notes:

| Average Profit After Tax | $=$ | Profit before depreciation - depreciation |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  | $=$ | $1,50,000-70,000$ | $=$ | 80,000 |
| Average Investment | $=$ | $(3,00,000+90,000) \div 2$ | $=$ | $1,95,000$ |

Depreciation per annum $=(3,00,000-90,000) \div 3$ years $=70,000$

## BQ 3

Times Ltd. is going to invest in a project a sum of $₹ 3,00,000$ having a life span of 3 years. Salvage value of machine is ₹ 90,000 . The profit after depreciation for each year is ₹ 80,000 . Additional working capital requirement is $₹ 45,000$

## Determine Accounting (Book) Rate of Return on the basis of average investment.

## Answer

| Accounting Rate of Return | $=\frac{\text { Average Profit After Tax }}{\text { Average Investment }} \times 100$ |
| ---: | :--- |
|  | $=\frac{80,000}{2,40,000} \times 100 \quad 33.33 \%$ |
| Average Investment | $=[(3,00,000+45,000)+(45,000+90,000)] \div 2$ |
|  | $=2,40,000$ |

BQ 4
Project A costs ₹ $2,00,000$ and Project B costs ₹ $3,00,000$ both have a ten year life. Uniform cash receipts expected are $A$ ₹ 40,000 p.a. and $B$ ₹ 80,000 p.a.

Calculate traditional payback period.

## Answer

| Payback Period | $=\frac{\text { Total Initial Capital Investment }}{\text { Annual Expected CFAT }}$ |  |
| :--- | :--- | :--- | :--- |
| Project A | $=\frac{2,00,000}{40,000}$ | $=5$ Years |
| Project B | $=\frac{3,00,000}{80,000}$ | $=3.75$ Years |

## BQ 5

The project involves a total initial expenditure of $₹ 2,00,000$ and it is estimated to generate future cash inflow of ₹ 30,000 , ₹ 38,000 , ₹ 25,000 , ₹ 22,000 , ₹ 36,000 , ₹ 40,000 , ₹ 40,000 , ₹ 28,000 , ₹ 24,000 and ₹ 24,000 in its last year.

## Calculate traditional payback period.

## Answer

Payback Period $=6$ year $+9,000 / 40,000=6.225$ Years

## Working Notes:

Calculation of Cumulative Cash Inflows:

| Year | Annual Cash Inflows | Cumulative Cash Inflows |
| :---: | :---: | :---: |
| 1 | $₹ 30,000$ | $₹ 30,000$ |


| 2 | $₹ 38,000$ | $₹ 68,000$ |
| :---: | :---: | :---: |
| 3 | $₹ 25,000$ | $₹ 93,000$ |
| 4 | $₹ 22,000$ | $₹ 1,15,000$ |
| 5 | $₹ 36,000$ | $₹ 1,51,000$ |
| 6 | $₹ 40,000$ | $₹ 1,91,000$ |
| 7 | $₹ 40,000$ | $₹ 2,31,000$ |
| 8 | $₹ 28,000$ | $₹ 2,59,000$ |
| 9 | $₹ 24,000$ | $₹ 2,83,000$ |
| 10 | $₹ 24,000$ | $₹ 3,07,000$ |

## DISCOUNTED PAYBACK, NPV \& PI TECHNIQUES (DCF)

## BQ 6

Geeta Ltd. is implementing a project with capital outlay of ₹7,600. Its cash inflows are as follows:

| Year | $\mathcal{F}$ |
| :---: | :---: |
| 1 | 6,000 |
| 2 | 2,000 |
| 3 | 1,000 |
| 4 | 5,000 |

The expected rate of return on the capital invested is $12 \%$ p.a.
Calculate the discounted payback period of the project.

## Answer

Calculation of Cumulative Discounted Cash Flow

| Year | Cash Inflow | DF @ 12\% p.a. | Discounted CF | Cumulative DCF |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 6,000 | 0.8929 | 5,357 | 5,357 |
| 2 | 2,000 | 0.7972 | 1,594 | 6,951 |
| 3 | 1,000 | 0.7118 | 712 | 7,663 |
| 4 | 5,000 | 0.6355 | 3,178 | 10,841 |

Discounted Payback period $=2$ years $+\frac{7,600-6,951}{712}=2.91$ years

## BQ 7

Compute the net present value for a project with a net investment of ₹ $1,00,000$ and net cash flows year one is ₹ 55,000 ; for year two is ₹ 80,000 and for year three is $₹ 15,000$. Further, the company's cost of capital is $10 \%$ ? [PVIF @ $10 \%$ for three years are $0.909,0.826$ and 0.751 ]

## Answer

Statement of NPV

| Pears | Particulars | ₹ | DF @ 10\% | PV |
| :---: | :--- | :---: | :---: | :---: |
| 0 | Investment (outflow) | $(1,00,000)$ | 1.000 | $(1,00,000)$ |
| 1 | Cash inflow | 55,000 | 0.909 | 49,995 |
| 2 | Cash inflow | 80,000 | 0.826 | 66,080 |
| 3 | Cash inflow | 15,000 | 0.751 | 11,265 |
| NPV |  |  |  | $\mathbf{2 7 , 3 4 0}$ |

Since the net present value is positive, investment in the project should be made.

## BQ 8

ABC Ltd. is a small company that is currently analyzing capital expenditure proposals for the purchase of equipment; the company uses the net present value technique to evaluate projects. The capital budget is limited to ₹500,000 which ABC Ltd believes is the maximum capital it can raise. The initial investment and projected net cash flows for each project are shown below. The cost of capital of ABC Ltd is $12 \%$.

You are required to compute the NPV of the different projects.

| Particulars | Project $\boldsymbol{A}$ | Project B | Project C | Project D |
| :---: | ---: | :---: | :---: | :---: |
| Initial Investment (outflow) | $2,00,000$ | $1,90,000$ | $2,50,000$ | $2,10,000$ |
| Projected Cash Inflows: |  |  |  |  |
| Year 1 | 50,000 | 40,000 | 75,000 | 75,000 |
| Year 2 | 50,000 | 50,000 | 75,000 | 75,000 |
| Year 3 | 50,000 | 70,000 | 60,000 | 60,000 |
| Year 4 | 50,000 | 75,000 | 80,000 | 40,000 |
| Year 5 | 50,000 | 75,000 | $1,00,000$ | 20,000 |

## Answer

## Statement of NPV

| Period | PV factor | Project $\boldsymbol{A}$ | Project B | Project $\boldsymbol{C}$ | Project $\boldsymbol{D}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 1.000 | $(2,00,000)$ | $(1,90,000)$ | $(2,50,000)$ | $(2,10,000)$ |
| 1 | 0.893 | 44,650 | 35,720 | 66,975 | 66,975 |
| 2 | 0.797 | 39,850 | 39,850 | 59,775 | 59,775 |
| 3 | 0.712 | 35,600 | 49,840 | 42,720 | 42,720 |
| 4 | 0.636 | 31,800 | 47,700 | 50,880 | 25,440 |
| 5 | 0.567 | 28,350 | 42,525 | 56,700 | 11,340 |
| Net Present Value |  | $(19,750)$ | 25,635 | 27,050 | $(3,750)$ |

## BQ 9

Suppose we have three projects involving discounted cash outflow of ₹5,50,000, ₹75,000 and ₹ $1,00,20,000$ respectively. Suppose further that the sum of discounted cash inflows for these projects are ₹ $6,50,000$, ₹ 95,000 and $₹ 1,00,30,000$ respectively.

## Calculate the desirability factors for the three projects.

## Answer

| Desirability factor | $=$ | $\frac{\mathrm{PV} \text { of Inflows }}{\mathrm{PV} \text { of Outflows }}$ |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Project 1 | $=$ | $\frac{6,50,000}{5,50,000}$ | $=$ | 1.18 |
| Project 2 | $=$ | $\frac{95,000}{75,000}$ | $=$ | 1.27 |
| Project 3 | $=$ | $\frac{1,00,30,000}{1,00,20,000}$ | $=$ | 1.001 |

## BQ 10

A Company is considering whether it should spend ₹ $4,00,000$ on a project to manufacture and sell a new product. The unit variable cost of the product is ₹ 6 . It is expected that the new product can be sold at ₹ 10 per unit. The annual fixed costs (only cash) will be ₹ 20,000 . The project will have a life of six years
with a scrap value of ₹ 20,000 . The cost of capital of the company is $15 \%$. The only uncertain factor is the volume of sales. To start with the company expects to sell at least 40,000 units during the first year.

## Required:

(1) Net present value of the project based on the sales expected during the first year and on the assumption that it will continue at the same level during the remaining years.
(2) The minimum volume of sales required to justify the project.

Note: Annuity of ₹1 at $15 \%$ for six years has a present value of ₹ 3.7845 and present value of ₹ 1 received at the end of sixth year at $15 \%$ is ₹ 0.4323 .
[(1) NPV 1,38,476; (2) 30,853 units]

## BQ 11

Cello Limited is considering buying a new machine which would have a useful economic life of five years, a cost of $₹ 1,25,000$ and a scrap value of $₹ 30,000$, with 80 per cent of the cost being payable at the start of the project and 20 per cent at the end of the first year. The machine would produce 50,000 units per annum of a new project with an estimated selling price of ₹ 3 per unit. Direct costs would be ₹ 1.75 per unit and annual fixed costs, including depreciation calculated on a straight line basis, would be ₹40,000 per annum. In the first year and the second year, special sales promotion expenditure, not included in the above costs, would be incurred, amounting to ₹ 10,000 and ₹ 15,000 respectively.

Evaluate the project using the NPV method of investment appraisal, assuming the company's cost of capital to be 10 percent.

## Answer

Statement of NPV

| Year | Particulars | ₹ | DF @ 10\% | PV |
| :---: | :--- | :---: | :---: | :---: |
| 0 | Initial outflows (80\% of 1,25,000) | $(1,00,000)$ | 1.000 | $(1,00,000)$ |
| 1 | Cash inflow - Outflow | 6,500 | 0.909 | 5,909 |
|  | (31,500 - 20\% of 1,25,000) |  |  |  |
| 2 | Cash inflow | 26,500 | 0.826 | 21,889 |
| $3-5$ | Cash inflow | 41,500 | 2.055 | 85,283 |
| 5 | Salvage | 30000 | 0.621 | 18,630 |
| NPV |  |  |  | $\mathbf{3 1 , 7 1 0}$ |

## Working Note:

(a) Calculation of Annual Cash Inflow

| Particulars | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3 - 5}$ |
| :--- | :---: | :---: | :---: |
| Sales value @ ₹3 per unit of 50,000 units | $1,50,000$ | $1,50,000$ | $1,50,000$ |
| Less: Direct costs @ ₹1.75 per unit | 87,500 | 87,500 | 87,500 |
| Less: Annual cash fixed cost (40,000-19,000) | 21,000 | 21,000 | 21,000 |
| Less: Special sales promotion expenses | 10,000 | 15,000 | - |
| Cash Inflow | $\mathbf{3 1 , 5 0 0}$ | $\mathbf{2 6 , 5 0 0}$ | $\mathbf{4 1 , 5 0 0}$ |

(b) Depreciation |  | $=($ Cost of machine - Scrap value $) \div$ Life |
| ---: | :--- |
|  | $=(1,25,000-30,000) \div 5$ years |
|  | $=19,000$ per annum |

Advise: Cello limited should buy machine having positive NPV.

## BQ 12

XYZ Ltd is planning to introduce a new product with a projected life of 8 years. The project to be set up in a backward region, qualifies for a one time (as its starting) tax free subsidy from the government of ₹ $20,00,000$ equipment cost will be ₹ 140 lakhs and additional equipment costing ₹ $10,00,000$ will be needed at the beginning of the third year. At the end of 8 years the original equipment will have no resale value but the supplementary equipment can be sold for ₹ $1,00,000$. A working capital of ₹ $15,00,000$ will be needed.

The sales volume over the eight years period has been forecasted as follows:

| Year | Units |
| :---: | ---: |
| 1 | 80,000 |
| 2 | $1,20,000$ |
| $3-5$ | $3,00,000$ |
| $6-8$ | $2,00,000$ |

A sale price of $₹ 100$ per unit is expected and variable expenses will amount to $40 \%$ of sales revenue. Fixed cash operating costs will amount to ₹ $16,00,000$ per year. In addition an extensive advertising campaign will be implemented requiring annual outlays as follows:

| Year | (₹in lakhs) |
| :---: | :---: |
| 1 | 30 |
| 2 | 15 |
| $3-5$ | 10 |
| $6-8$ | 4 |

The company is subject to $50 \%$ tax rate and considers $12 \%$ to be an appropriate after tax cost of capital for this project. The company follows the straight line method of depreciation.

## Should the project be accepted?

## Answer

Net Present Value

| Year | Particulars | ₹ | DF @ 12\% | PV |
| :---: | :--- | :---: | :---: | :---: |
| 0 | Initial outflows | $(1,35,00,000)$ | 1.000 | $(1,35,00,000)$ |
|  | $(140-20+15)$ Lakhs |  |  |  |
| 1 | CFAT | $2,00,000$ | 0.893 | $1,78,600$ |
| 2 | CFAT less Additional Equipment | $24,50,000$ | 0.797 | $19,52,650$ |
|  | $(34,50,000-10,00,000)$ |  |  |  |
| $3-5$ | CFAT | $85,25,000$ | 1.915 | $1,63,25,375$ |
| $6-8$ | CFAT | $58,25,000$ | 1.363 | $79,39,475$ |
| 8 | Working Capital and Salvage | $16,00,000$ | 0.404 | $6,46,400$ |
|  | $(15,00,000+1,00,000)$ |  |  |  |
| $\mathbf{N P V}$ |  |  |  |  |

## Company should accept the proposal having positive NPV of the project.

## Working Notes:

1. Statement of CFAT

| Particulars | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3 - 5}$ | $\mathbf{6 - 8}$ |
| :--- | :---: | :---: | :---: | :---: |
| Units sold | 80,000 | $1,20,000$ | $3,00,000$ | $2,00,000$ |


| Sales @ ₹100 p.u. | $80,00,000$ | $1,20,00,000$ | $3,00,00,000$ | $2,00,00,000$ |
| :--- | :---: | :---: | :---: | :---: |
| Less: VC @ 40\% | $32,00,000$ | $48,00,000$ | $1,20,00,000$ | $80,00,000$ |
| Contribution | $48,00,000$ | $72,00,000$ | $1,80,00,000$ | $1,20,00,000$ |
| Less: Advertisement expenses | $(30,00,000)$ | $15,00,000)$ | $(10,00,000)$ | $(4,00,000)$ |
| Less: Cash fixed cost | $(16,00,000)$ | $(16,00,000)$ | $(16,00,000)$ | $(16,00,000)$ |
| Less: Depreciation | $(15,00,000)$ | $(15,00,000)$ | $(16,50,000)$ | $(16,50,000)$ |
| PBT | $(13,00,000)$ | $26,00,000$ | $1,37,50,000$ | $83,50,000$ |
| Less: Tax @ 50\% | - | $16,50,000)$ | $(68,75,000)$ | $(41,75,000)$ |
| PAT | $(13,00,000)$ | $19,50,000$ | $68,75,000$ | $41,75,000$ |
| Add: Depreciation | $\mathbf{1 5 , 0 0 , 0 0 0}$ | $15,00,000$ | $16,50,000$ | $16,50,000$ |
| $\boldsymbol{C F A T}$ | $\mathbf{2 , 0 0 , 0 0 0}$ | $\mathbf{3 4 , 5 0 , 0 0 0}$ | $\mathbf{8 5 , 2 5 , 0 0 0}$ | $\mathbf{5 8 , 2 5 , 0 0 0}$ |

## 2. Depreciation:

| Main equipment $\left(\boldsymbol{t}_{\boldsymbol{0}}-\boldsymbol{t}_{\boldsymbol{8}}\right)$ | $=\frac{\text { Original Cost-Subsidy-Salvage }}{\text { Life of Equipment }}=\frac{1,20,00,000}{8 \text { Years }}$ |
| ---: | :--- |
|  | $=\mathbf{1 5 , 0 0 , 0 0 0}$ |
| Additional equipment $\left(\boldsymbol{t}_{3}-\boldsymbol{t}_{\boldsymbol{8}}\right)$ | $=\frac{\text { Original Cost -Salvage }}{\text { Life of Equipment }}=\frac{9,00,000}{6 \text { Years }}$ |
|  | $=\mathbf{1 , 5 0 , 0 0 0}$ |
| Tax for year 2 | $=50 \%$ of $(26,00,000-13,00,000)=\mathbf{6 , 5 0 , 0 0 0}$ |

Note: As per section 32 of Income Tax Act "Depreciation is not allowed on subsidized part of asset"

## BQ 13

XYZ Ltd. is planning to introduce a new product with a project life of 8 years. Initial equipment cost will be ₹ 3.5 crores. Additional equipment costing ₹ $25,00,000$ will be purchased at the end of the third year from the cash inflow of this year. At the end of 8 years, the original equipment will have no resale value, but additional equipment can be sold for $₹ 2,50,000$. A working capital of $₹ 40,00,000$ will be needed and it will be released at the end of eighth year. The project will be financed with sufficient amount of equity capital. The sales volumes over eight years have been estimated as follows:

| Year | 1 | 2 | 3 | $4-5$ | $6-8$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Units | 72,000 | $1,08,000$ | $2,60,000$ | $2,70,000$ | $1,80,000$ |

A sales price of ₹ 240 per unit is expected and variable expenses will amount to $60 \%$ of sales revenue. Fixed cash operating costs will amount $₹ 36,00,000$ per year. The loss of any year will be set off from the profits of subsequent two years. The company is subject to 30 per cent tax rate and considers 12 per cent to be an appropriate after tax cost of capital for this project. The company follows straight line method of depreciation.

## Calculate the net present value of the project and advise the management to take appropriate decision.

## The PV factors at 12\% are

| Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 | Year 7 | Year 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.893 | 0.797 | 0.712 | 0.636 | 0.567 | 0.507 | 0.452 | 0.404 |

## Answer

Net Present Value

| Year | Particulars | $₹$ | DF @ 12\% | PV |
| :---: | :--- | :---: | :---: | :---: |
| 0 | Initial Equipment cost plus working capital | $(3,90,00,000)$ | 1.000 | $(3,90,00,000)$ |
|  | $(350+40)$ Lakhs |  |  |  |
| 1 | CFAT | $33,12,000$ | 0.893 | $29,57,616$ |
| 2 | CFAT | $63,69,000$ | 0.797 | $50,76,093$ |
| 3 | CFAT less Additional Equipment | $1,37,64,500$ | 0.712 | $98,00,324$ |
|  | $(1,62,64,500-25,00,000)$ |  |  |  |
| $4-5$ | CFAT | $1,70,71,500$ | 1.203 | $2,05,37,015$ |
| $6-8$ | CFAT | $1,10,23,500$ | 1.363 | $1,50,25,031$ |
| 8 | Working Capital and Salvage | $42,50,000$ | 0.404 | $17,17,000$ |
|  | $(40,00,000+2,50,000)$ | $\mathbf{N P V}$ |  | $\mathbf{1 , 6 1 , 1 3 , 0 7 9}$ |

## Company should accept the proposal having positive NPV of the project.

Working Notes:

## 1. Statement of CFAT

| Particulars | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4 - 5}$ | $\mathbf{6 - 8}$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Units sold | 72,000 | $1,08,000$ | $2,60,000$ | $2,70,000$ | $1,80,000$ |
| Sales @ ₹240 p.u. | $1,72,80,000$ | $2,59,20,000$ | $6,24,00,000$ | $6,48,00,000$ | $4,32,00,000$ |
| Less: VC @ 60\% | $1,03,68,000$ | $1,55,52,000$ | $3,74,40,000$ | $3,88,80,000$ | $2,59,20,000$ |
| Contribution | $69,12,000$ | $1,03,68,000$ | $2,49,60,000$ | $2,59,20,000$ | $1,72,80,000$ |
| Less: Cash fixed cost | $36,00,000$ | $36,00,000$ | $36,00,000$ | $36,00,000$ | $36,00,000$ |
| Less: Depreciation | $43,75,000$ | $43,75,000$ | $43,75,000$ | $48,25,000$ | $48,25,000$ |
| PBT | $10,63,000)$ | $23,93,000$ | $1,69,85,000$ | $1,74,95,000$ | $88,55,000$ |
| Less: Tax @ 30\% | - | $3,99,000)$ | $150,95,500)$ | $152,48,500)$ | $(26,56,500)$ |
| PAT | $10,63,000$ | $19,94,000$ | $1,18,89,500$ | $1,22,46,500$ | $61,98,500$ |
| Add: Depreciation | $43,75,000$ | $43,75,000$ | $43,75,000$ | $48,25,000$ | $48,25,000$ |
| $\boldsymbol{C F A T}$ | $\mathbf{3 3 , 1 2 , 0 0 0}$ | $\mathbf{6 3 , 6 9 , 0 0 0}$ | $\mathbf{1 , 6 2 , 6 4 , 5 0 0}$ | $\mathbf{1 , 7 0 , 7 1 , 5 0 0}$ | $\mathbf{1 , 1 0 , 2 3 , 5 0 0}$ |

## 2. Depreciation:

| Main equipment $\left(\boldsymbol{t}_{\boldsymbol{0}}-\boldsymbol{t}_{\boldsymbol{B}}\right)$ | $=\frac{\text { Original Cost }}{\text { Life of Equipment }}=\frac{3,50,00,000}{8 \text { Years }}=\mathbf{4 3 , 7 5 , 0 0 0}$ |  |
| :--- | :--- | :--- |
| Additional equipment $\left(\boldsymbol{t}_{\boldsymbol{4}}-\boldsymbol{t}_{\boldsymbol{8}}\right)$ | $=\frac{\text { Original Cost -Salvage }}{\text { Life of Equipment }}=\frac{22,50,000}{5 \text { Years }}=\mathbf{4 , 5 0 , 0 0 0}$ |  |
| Tax for year 2 | $=30 \%$ of $(23,93,000-10,63,000)$ | $=3,99,000$ |

## BQ 14

A chemical company is presently paying an outside firm ₹ 1 per gallon to dispose off the waste resulting from its manufacturing operations. At normal operating capacity, the waste is about 50,000 gallons per year.

After spending ₹ 60,000 on research, the company discovered that the waste could be sold for ₹ 10 per gallon if it was processed further. Additional processing would, however, require an investment of ₹ $6,00,000$ in new equipment, which would have an estimated life of 10 years with no salvage value. Depreciation would be calculated by straight line method.

Except for the costs incurred in advertising ₹ 20,000 per year, no change in the present selling
and administrative expenses is expected, if the new product is sold. The details of additional processing costs are as follows:

| Variable | $:$ | ₹5 per gallon of waste put into process. |
| :--- | :--- | :--- |
| Fixed | $:$ | ₹ 30,000 per year (Excluding Depreciation). |

There will be no losses in processing, and it is assumed that the total waste processed in a given year will be sold in the same year. Estimates indicate that 50,000 gallons of the product could be sold each year.
The management when confronted with the choice of disposing off the waste or processing it further and selling it, seeks your advice. You should consider Present value of Annuity of ₹ 1 per year @ 15\% p.a. for 10 years as 5.019.

Which alternative would you recommend? Assume that the firm's cost of capital is 15\% and it pays on an average 50\% Tax on its income.

## Answer

Statement of NPV

| Year | Particulars | ₹ | DF @ 15\% | PV |
| :---: | :--- | :---: | :---: | :---: |
| 0 | Initial outflows | $(6,00,000)$ | 1.000 | $(6,00,000)$ |
| $1-10$ | Annual CFAT | $1,55,000$ | 5.019 | $7,77,945$ |
| NPV |  |  | $\mathbf{1 , 7 7 , 9 4 5}$ |  |

## Working Note:

## Calculation of CFAT

| Particulars | ₹ |
| :---: | :---: |
| Sales value of waste ( 50,000 gallon $\times$ ₹ 10 ) | 5,00,000 |
| Add: Saving in Disposal cost ( 50,000 gallon $\times$ ₹ 1 ) | 50,000 |
| Less: Variable processing cost (50,000 gallon $\times$ ₹ 5 ) | $(2,50,000)$ |
| Less: Fixed processing cost (excluding depreciation) | $(30,000)$ |
| Less: Advertisement cost | $(20,000)$ |
| Less: Depreciation ( $6,00,000 \div 10$ years) | $(60,000)$ |
| PBT | 1,90,000 |
| Less: Tax @ 50\% | $(95,000)$ |
| PAT | 95,000 |
| Add: Depreciation | 60,000 |
| Annual CFAT | 1,55,000 |

Recommendation: Processing of waste is a better option as it gives a positive NPV.
Note: Research cost of 60,000 is not relevant for decision making as it is sunk cost.

## BQ 15

Manoranjan Ltd is a News broadcasting channel having its broadcasting Centre in Mumbai. There are total 200 employees in the organisation including top management. As a part of employee benefit expenses, the company serves tea or coffee to its employees, which is outsourced from a third-party. The company offers tea or coffee three times a day to each of its employees. 120 employees prefer tea all three times, 40 employees prefer coffee all three times and remaining prefer tea only once in a day. The third-party charges ₹10 for each cup of tea and ₹ 15 for each cup of coffee. The company works for 200 days in a year.

Looking at the substantial amount of expenditure on tea and coffee, the finance department has proposed to the management an installation of a master tea and coffee vending machine which will cost $₹ 10,00,000$ with a useful life of five years. Upon purchasing the machine, the company will have to enter into an annual maintenance contract with the vendor, which will require a payment of ₹ 75,000 every year. The machine would require electricity consumption of 500 units p.m. and current incremental cost of electricity for the company is ₹ 12 per unit. Apart from these running costs, the company will have to incur the following consumables expenditure also:

1. Packets of Coffee beans at a cost of $₹ 90$ per packet.
2. Packet of tea powder at a cost of ₹ 70 per packet.
3. Sugar at a cost of $₹ 50$ per Kg.
4. Milk at a cost of ₹ 50 per litre.
5. Paper cup at a cost of 20 paise per cup.

Each packet of coffee beans would produce 200 cups of coffee and same goes for tea powder packet. Each cup of tea or coffee would consist of 10 g of sugar on an average and 100 ml of milk. The company anticipate that due to ready availability of tea and coffee through vending machines its employees would end up consuming more tea and coffee.

It estimates that the consumption will increase by on an average $20 \%$ for all class of employees. Also, the paper cups consumption will be $10 \%$ more than the actual cups served due to leakages in them.

The company is in the $25 \%$ tax bracket and has a current cost of capital at $12 \%$ per annum. Straight line method of depreciation is allowed for the purpose of taxation.

You as a financial consultant is required to ADVISE on the feasibility of acquiring the vending machine.

## PV factors @ 12\%:

| Year | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{P V F}$ | 0.8929 | 0.7972 | 0.7118 | 0.6355 | 0.5674 |

## Answer

Statement of NPV

| Year | Particulars | ₹ | DF @ 12\% | PV |
| :---: | :---: | :---: | :---: | :---: |
| 0 | Initial outflows | $(10,00,000)$ | 1.000 | (10,00,000) |
| 1-5 | Annual CFAT | 2,39,438 | 3.6048 | 8,63,126 |
| NPV |  |  |  | (1,36,874) |

Since NPV of the machine is negative, it should not be purchased.

## Working Note:

Calculation of CFAT

| Particulars | $₹$ |
| :--- | :---: |
| Saving in Existing Tea \& Coffee Charges | $11,60,000$ |
| $(120 \times 10 \times 3 \times 200)+(40 \times 15 \times 3 \times 200)+(40 \times 10 \times 1 \times 200)$ |  |
| Less: AMC of Machine | $(75,000)$ |
| Less: Electricity Charges $(500 \times 12 \times 12)$ | $(72,000)$ |
| Less: Coffee beans $(144 \times 90)$ | $(12,960)$ |
| Less: Tea powder $(480 \times 70)$ | $(33,600)$ |
| Less: Sugar $(1,248 \times 50)$ | $(62,400)$ |
| Less: Milk $(12,480 \times 50)$ | $(6,24,000)$ |


| Less: Paper cup $(1,37,280 \times 0.20)$ | $(27,456)$ |  |
| :--- | :--- | :---: |
| Less: Depreciation $(10,00,000 \div 5$ years $)$ | $(2,00,000)$ |  |
| Less: Tax @ 25\% | PBT | 52,584 |
|  | PAT | $(13,146)$ |
|  |  | 39,438 |
| Add: Depreciation | Annual CFAT | $2,00,000$ |

## Computation of Qty of consumable:

| No. of Tea Cups | = | $[(120 \times 3 \times 200$ days $)+(40 \times 1 \times 200$ days $) \times 1.2$ |  |  | 96,000 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of Coffee cups | = | $40 \times 3 \times 200$ days $\times 1.2$ |  |  | 28,800 |
| No. of coffee beans packet | = | 28,800/200 | = | 144 |  |
| No. of Tea Powder Packets | = | 96,000/200 | = | 480 |  |
| Qty of Sugar | = | $(96,000+28,800) \times 6,0$ | $=$ | 1,248 |  |
| Qty of Milk | = | $(96,000+28,800) \times 6,0$ |  | 12,48 |  |
| No. of paper cups | $=$ | $(96,000+28,800) \times 1.1$ | = | 1,37, |  |

## UNEQUAL LIFE OF PROJECTS

BQ 16
APZ limited is considering selecting a machine between two machines ' A ' and ' B '. The two machines have identical capacity, do exactly the same job, but designed differently.

Machine A costs ₹ $8,00,000$, having useful life of three years. It costs ₹ $1,30,000$ per year to run. Machine $B$ is an economic model costing ₹ $6,00,000$, having useful life of two years. It costs ₹ $2,50,000$ per year to run.

The cash flows of machine ' A ' and ' B ' are real cash flows. The costs are forecasted in rupees of constant purchasing power. Ignore taxes. The opportunity cost of capital is $10 \%$.

The present value factors at 10\% are:

| Years | $\boldsymbol{t}_{\mathbf{1}}$ | $\boldsymbol{t}_{\boldsymbol{2}}$ | $\boldsymbol{t}_{\mathbf{3}}$ |
| :--- | :---: | :---: | :---: |
| PVIF $_{0.10 \mathrm{t}}$ | 0.9091 | 0.8264 | 0.7513 |
| PVIFA $_{0.10 .2}=1.7355$ |  |  |  |
| PVIFA $_{0.10 .3}=2.4868$ |  |  |  |

Which machine would you recommend the company to buy?

## Answer

Statement Showing Evaluation of Two Machines

| Particulars | Machine ' $\boldsymbol{A}$ ' | Machine ' $\boldsymbol{B}^{\prime}$ |
| :---: | :---: | :---: |
| Initial outflow/ Purchase cost of machines | $8,00,000$ | $6,00,000$ |


| Annual running cost | $1,30,000$ | $2,50,000$ |
| :--- | :---: | :---: |
| Life of machines | 3 years | 2 years |
| PV of annual running cost |  |  |
| (Annual running cost $\times$ PVIFA) | $3,23,284$ | $4,33,875$ |
| Present value of total outflow <br> (Initial outflow + PV of annual running cost) <br> $\div$ PVIFA | $(1,30,000 \times 2.4868)$ | $(2,50,000 \times 1.7355)$ |
| $\quad$ | $\div 2,23,284$ | $10,33,875$ |
| Equivalent Annual outflow | $\mathbf{4 , 5 1 , 6 9 9}$ | $\div 1.7355$ |
|  |  | $\mathbf{5 , 9 5 , 7 2 2}$ |

Select the Machine A having lower equivalent annualized outflow.

## BQ 17

Ae Bee Cee Ltd. is planning to invest in machinery, for which it has to make a choice between the two identical machines, in terms of Capacity, ' X ' and ' Y '. Despite being designed differently, both machines do the same job. Further, details regarding both the machines are given below:

| Particulars | Machine ${ }^{\prime} X^{\prime}$ | Machine $^{\prime}$ ' $\mathrm{Y}^{\prime}$ |
| :--- | :---: | :---: |
| Purchase Cost of the Machine $(₹)$ | $15,00,000$ | $10,00,000$ |
| Life (years) | 3 | 2 |
| Running cost per year $(₹)$ | $4,00,000$ | $6,00,000$ |

The opportunity cost of capital is $9 \%$.
You are required to identify the machine the company should buy?
The present value (PV) factors at 9\% are:

| Year | $\boldsymbol{t}_{\mathbf{1}}$ | $\boldsymbol{t}_{\mathbf{2}}$ | $\boldsymbol{t}_{\mathbf{3}}$ |
| :---: | :---: | :---: | :---: |
| PVIF0.09.t | 0.917 | 0.842 | 0.772 |

## Answer

## Statement Showing Evaluation of Two Machines

| Particulars | Machine ' $\mathrm{X}^{\prime}$ | Machine ' $Y$ ' |
| :---: | :---: | :---: |
| Initial outflow/ Purchase cost of machines | 15,00,000 | 10,00,000 |
| Annual running cost | 4,00,000 | 6,00,000 |
| Life of machines | 3 years | 2 years |
| PV of annual running cost (Annual running cost $\times$ PVIFA) | $\begin{gathered} 10,12,400 \\ (4,00,000 \times 2.531) \end{gathered}$ | $\begin{gathered} 10,55,400 \\ (6,00,000 \times 1.759) \end{gathered}$ |
| Present value of total outflow <br> (Initial outflow + PV of annual running cost) <br> $\div$ PVIFA | $25,12,400$ $\div 2.531$ | $20,55,400$ $\div 1.759$ |
| Equivalent Annual outflow | 9,92,651 | 11,68,505 |

## Select the Machine X having lower equivalent annualized outflow.

## CAPITAL RATIONING

## BQ 18

Shiva Limited is planning its capital investment programme for next year. It has five projects all of which give a positive NPV at the company cut-off rate of 15 percent, the investment outflows and present values being as follows:

| Project Name | Initial Investment | NPV @ 15\% |
| :---: | :---: | :---: |
| A | $₹ 50,000$ | $₹ 15,400$ |
| B | $₹ 40,000$ | $₹ 18,700$ |
| C | $₹ 25,000$ | $₹ 10,100$ |
| D | $₹ 30,000$ | $₹ 11,200$ |
| E | $₹ 35,000$ | $₹ 19,300$ |

The company is limited to a capital spending of $₹ 1,20,000$.
You are required to optimise the returns from a package of projects within the capital spending limit. The projects are independent of each other and are (a) divisible, (b) indivisible.

Answer
(a) Statement of Rank and Selection of Projects
(Divisible Situation)

| Projects | PI (1+ NPV/Investment) | Rank | Project Cost | Project (\%) | Investment |
| :---: | :---: | :---: | :---: | :---: | :---: |
| A | $1+15,400 / 50,000=1.31$ | 5 | $₹ 50,000$ | - | - |
| B | $1+18,700 / 40,000=1.47$ | 2 | $₹ 40,000$ | $100 \%$ | $₹ 40,000$ |
| C | $1+10,100 / 25,000=1.40$ | 3 | $₹ 25,000$ | $100 \%$ | $₹ 25,000$ |
| D | $1+11,200 / 30,000=1.37$ | 4 | $₹ 30,000$ | $66.67 \%$ | $₹ 20,000(\mathrm{~b} . \mathrm{f})$ |
| E | $1+19,300 / 35,000=1.55$ | 1 | $₹ 35,000$ | $100 \%$ | $₹ 35,000$ |
| Total Investment |  |  |  |  |  |

Optimum investment: 100\% of B, C, E and 2/3 D.
(b) Statement of Possible Combinations and Combined NPV (Indivisible Situation)

| Possible Combinations | Combined Investment | Combined NPV |
| :---: | :---: | :---: |
| A + B + C | $₹ 1,15,000$ | $₹ 44,200$ |
| A + B + | $₹ 1,20,000$ | $₹ 45,300$ |
| A C + D | $₹ 1,05,000$ | $₹ 36,700$ |
| A C + E | $₹ 1,10,000$ | $₹ 44,800$ |
| A D E | $₹ 1,15,000$ | $₹ 40,900$ |
| B C + D | $₹ 95,000$ | $₹ 48,100$ |
| B + + E | $₹ 1,00,000$ | $₹ 49,200$ |
| B + D + E | $₹ 1,05,000$ | $₹ 40,600$ |

Invest in combination of B, D and E having highest combined NPV and invest remaining ₹15,000 elsewhere.

## BQ 19

P Ltd. has a machine having an additional life of 5 years which costs $₹ 10,00,000$ and has a book value of ₹ $4,00,000$.

A new machine costing ₹ $20,00,000$ is available. Though its capacity is the same as that of the old machine, it will mean a saving in variable costs to the extent of $₹ 7,00,000$ per annum. The life of the machine will be 5 years at the end of which it will have a scrap value of ₹ $2,00,000$.

The rate of income tax is $46 \%$ and $P$ Ltd's policy is not to make an investment if the yield is less than $12 \%$ per annum.

The old machine, if sold today will realise ₹ $1,00,000$; it will have no salvage value if sold at the end of 5th year. Advise P Ltd. whether or not the old machine should be replaced.

Present value of ₹ 1 receivable annually for 5 years at $12 \%$ is 3.605 , present value of ₹ 1 receivable at the end of 5 year at $12 \%$ per annum is 0.567 . Capital gain is tax free. Ignore income tax savings on depreciation as well as on loss due to sale of existing machine.

## Answer

## Statement of NPV

| Years | Particulars | ₹ | PVF @ 12\% | PV |
| :---: | :--- | :---: | :---: | :---: |
| 0 | Initial outflow | $(19,00,000)$ | 1.000 | $(19,00,000)$ |
| $1-5$ | CFAT | $3,78,000$ | 3.605 | $13,62,690$ |
| 5 | Scrap value of new assets | $2,00,000$ | 0.567 | $1,13,400$ |
| NPV |  |  | $(4,23,910)$ |  |

## Working notes:

## 1. Calculation of initial outflow:

Cost of new machine
Less: Sale proceeds of old machine
Initial outflow
₹ $20,00,000$
₹1,00,000
₹19,00,000
2. Calculation of incremental CFAT:

Annual savings
₹7,00,000
Less: Tax @ 46\% ₹3,22,000
Profit after tax/ CFAT
₹3,78,000

Analysis: P Ltd should not replace the machine.

## BQ 20

ABC Ltd. is considering the replacement of one of its molding machines. The existing machine is in good operation condition but is smaller than required if the firm is to expand its operations. The old machine is 5 years old and has remaining depreciable life of 10 years. The machine was originally purchased for $₹ 1,50,000$ and is being depreciated at ₹ 10,000 per year for tax purposes.

The new machine will cost $₹ 2,20,000$ or $₹ 1,70,000$ if exchanged with the existing machine. It will be depreciated on a straight line basis for 10 years with no salvage value. The management anticipates that with the increased operations there will be need for an additional net working capital of ₹ 30,000 .

The new machine will allow the company to expand current operations thereby increasing
annual revenue by ₹ 60,000 and variable operating costs from ₹ $2,00,000$ to ₹ $2,20,000$. The company's tax rate is $35 \%$ and its cost of capital is $10 \%$.

Should the company replace its existing machine? Assume that the loss on exchange of existing machine can be claimed as short term capital loss in the current year itself.

Answer
Statement of NPV

| Years | Particulars | ₹ | PVF @ 10\% | PV |  |  |  |
| :---: | :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | Initial outflow | $(1,82,500)$ | 1.000 | $(1,82,500)$ |  |  |  |
| $1-10$ | CFAT | 30,200 | 6.145 | $1,85,579$ |  |  |  |
| 10 | Working capital | 30,000 | 0.386 | 11,580 |  |  |  |
| $\mathbf{N P V}$ |  |  |  |  |  |  | $\mathbf{1 4 , 6 5 9}$ |

## Working notes:

## a. Calculation of initial outflow:

Cost of new machine
Less: Exchange value of old machine
Less: Tax saving on loss on sale of old machine
$[50,000-1,00,000(1,50,000-10,000 \times 5$ years $)] \times 35 \%$
Add: Additional working capital
Initial outflow
b. Calculation of incremental CFAT:

| Increase in sales | $₹ 60,000$ |
| :--- | :--- |
| Less: Increase in operating cost | (₹20,000) |
| Less: Increase in depreciation $(22,000-10,000)$ | (₹12,000) |
| Profit before tax | $₹ 28,000$ |
| Less: Tax @ $35 \%$ | $(₹ 9,800)$ |
| Profit after tax | $₹ 18,200$ |
| Add: Depreciation | $₹ 12,000$ |
| CFAT | $₹ 30,200$ |

Decision: ABC Ltd should exchange the machine.
BQ 21
MNP Limited is thinking of replacing its existing machine by a new machine which would cost ₹ 60 lakhs. The company's current production is ₹ 80,000 units, and is expected to increase to $1,00,000$ units, if the new machine is bought. The selling price of the product would remain unchanged at ₹ 200 per unit. The following is the cost of producing one unit of product using both the existing and new machine:

| Particulars | Existing Machine <br> (80,000 units) | New Machine <br> $\mathbf{( 1 , 0 0 , 0 0 0}$ units) | Difference |
| :--- | :---: | :---: | :---: |
| Materials | 75.00 | 63.75 | $(11.25)$ |
| Wages and Salaries | 51.25 | 37.50 | $(13.75)$ |
| Supervision | 20.00 | 25.00 | 5.00 |
| Repairs and Maintenance | 11.25 | 7.50 | $(3.75)$ |
| Power and Fuel | 15.50 | 14.25 | $(1.25)$ |
| Depreciation | 0.25 | 5.00 | 4.75 |
| Allocated Corporate OH | 10.00 | 12.50 | 2.50 |
| Total |  | $\mathbf{1 8 3 . 2 5}$ | $\mathbf{1 6 5 . 5 0}$ |
| $\mathbf{n y y y}$ |  | $\mathbf{1 7 . 7 5 )}$ |  |

The existing machine has an accounting book value of ₹ $1,00,000$, and it has been fully depreciated for tax purpose. It is estimated that machine will be useful for 5 years. The supplier of the new machine has offered to accept the old machine for ₹ $2,50,000$. However, the market price of old machine today is $₹ 1,50,000$ and it is expected to be ₹ 35,000 after 5 years. The new machine has a life of 5 years and a salvage value of $₹ 2,50,000$ at the end of its economic life.

Assume corporate Income tax rate at 40\%, and depreciation is charged on straight line basis for Incometax purposes. Further assume that book profit is treated as ordinary income for tax purpose. The opportunity cost of capital of the Company is $15 \%$.

## Required:

(i) Estimate net present value of the replacement decision.
(ii) Should Company go ahead with the replacement decision? Suggest.

| Year $(\boldsymbol{t})$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| PVIF $_{0.15, \mathrm{t}}$ | 0.8696 | 0.7561 | 0.6575 | 0.5718 | 0.4972 |
| PVIF $_{0.20, \mathrm{t}}$ | 0.8333 | 0.6944 | 0.5787 | 0.4823 | 0.4019 |
| PVIF $_{0.25, \mathrm{t}}$ | 0.8000 | 0.6400 | 0.5120 | 0.4096 | 0.3277 |
| PVIF $_{0.30, \mathrm{t}}$ | 0.7692 | 0.5917 | 0.4552 | 0.3501 | 0.2693 |
| PVIF $_{0.35, \mathrm{t}}$ | 0.7407 | 0.5487 | 0.4064 | 0.3011 | 0.2230 |

## Answer

(i) Statement of NPV

| Year | Particulars | ₹ | DF @ 15\% | PV |
| :---: | :--- | :---: | :---: | :---: |
| 0 | Initial outflows | $(58,50,000)$ | 1.0000 | $(58,50,000)$ |
| $1-5$ | Cash Flow After Tax | $22,84,000$ | 3.3522 | $76,56,425$ |
| 5 | Net Salvage 2,50,000 - 35,000 $(1-0.40)$ | $2,29,000$ | 0.4972 | $1,13,859$ |
| NPV |  |  | $\mathbf{1 9 , 2 0 , 2 8 4}$ |  |

## Working Notes:

## 1. Calculation of initial outflow:

> Cost of new machine ₹60,00,000

Less: Exchange value of old machine
(₹2,50,000)
Add: Tax payment on profit on exchange of old machine ₹1,00,000 $(2,50,000-\mathrm{Nil}) \times 40 \%$
Initial outflow F58,50,000
2. Calculation of incremental CFAT:

Increase in sales ( $200 \times 20,000$ units)
Less: Increase in operating cost $(1,00,000 \times 148)-(80,000 \times 173)$
₹ $40,00,000$
(excluding Depreciation and Allocated overheads)
Less: Increase in depreciation [(60,00,00-2,50,000) $\div 5]$ - Nil ₹11,50,000
Profit before tax ₹18,90,000
Less: Tax @ 40\%
Profit after tax
₹7,56,000
Add: Depreciation
₹11,34,000
Incremental CFAT
₹11,50,000
₹22,84,000

## 3. Calculation of Incremental Salvage:

Salvage of new machine (Salvage = WDV; no gain or loss) ₹2,50,000

| Less: Salvage of old machine (Salvage > WDV) | ₹35,000 |  |
| :---: | :---: | :---: |
| Tax on gain 40\% of 35,000 $(35,000-\mathrm{Nil})$ | $\underline{₹} 14,000$ | $₹ 21,000$ |
| Incremental Salvage |  | $₹ 2,29,000$ |

## Notes:

(a) The old machine could be sold for ₹ $1,50,000$ in the market. Since exchange value is more than the market value, company will exchange it at $₹ 2,50,000$.
(b) Old machine has fully depreciated for tax purpose, therefore depreciation of old machine as well as WDV are NIL.
(c) Allocated overheads are allocations from corporate office therefore they are irrelevant for computation of CFAT.
(ii) Advise: The company should go ahead with replacement project, since it has positive NPV.

BQ 22
HMR Ltd. is considering replacing a manually operated old machine with a fully automatic new machine. The old machine had been fully depreciated for tax purpose but has a book value of ₹ $2,40,000$ on $31^{\text {st }}$ March. The machine has begun causing problems with breakdowns and it cannot fetch more than ₹ 30,000 if sold in the market at present.

It will have no realizable value after 10 years. The company has been offered ₹ $1,00,000$ for the old machine as a trade in on the new machine which has a price (before allowance for trade in) of ₹ $4,50,000$. The expected life of new machine is 10 years with salvage value of ₹ 35,000 .

Further, the company follows straight line depreciation method but for tax purpose, written down value method depreciation @ $7.5 \%$ is considering that this is the only machine in the block of assets.

Given below are the expected sales and costs from both old and new machine:

| Particulars | Old Machine $(\mathbb{\text { }}$ ) | New Machine ( $₹$ ) |
| :--- | :---: | :---: |
| Sales | $8,10,000$ | $8,10,000$ |
| Material cost | $1,80,000$ | $1,26,250$ |
| Labour cost | $1,35,000$ | $1,10,000$ |
| Variable overhead | 56,250 | 47,500 |
| Fixed overhead | 90,000 | 97,500 |
| Depreciation | 24,000 | 41,500 |
| PBT | $3,24,750$ | $3,87,250$ |
| Tax @30\% | 97,425 | $1,16,175$ |
| PAT | 2,27325 | $2,71,075$ |

From the above information, ANALYSE whether the old machine should be replaced or not if required rate of return is 10\%? Ignore capital gain tax.

## PV factors @ 10\%:

| Year | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\mathbf{8}$ | $\mathbf{9}$ | $\mathbf{1 0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{P V F}$ | 0.909 | 0.826 | 0.751 | 0.683 | 0.621 | 0.564 | 0.513 | 0.467 | 0.424 | 0.386 |

## Answer

## Calculation of Incremental CFAT \& NPV

| Year | PVF | PBDT | Dep @ 7.5\% | PBT | Tax @ 30\% | Cash Inflow | PV |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.909 | 80,000 | 26,250 | 53,750 | 16,125 | 63,875 | 58,062 |
| 2 | 0.826 | 80,000 | 24,281 | 55,719 | 16,716 | 63,284 | 52,273 |


| 3 | 0.751 | 80,000 | 22,460 | 57,540 | 17,262 | 62,738 | 47,116 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | 0.683 | 80,000 | 20,776 | 59,224 | 17,767 | 62,233 | 42,505 |
| 5 | 0.621 | 80,000 | 19,217 | 60,783 | 18,235 | 61,765 | 38,356 |
| 6 | 0.564 | 80,000 | 17,776 | 62,224 | 18,667 | 61,333 | 34,592 |
| 7 | 0.513 | 80,000 | 16,443 | 63,557 | 19,067 | 60,933 | 31,259 |
| 8 | 0.467 | 80,000 | 15,210 | 64,790 | 19,437 | 60,563 | 28,283 |
| 9 | 0.424 | 80,000 | 14,069 | 65,931 | 19,779 | 60,221 | 25,534 |
| 10 | 0.386 | 80,000 | 13,014 | 66,986 | 20,096 | 59,904 | 23,123 |
| Add: PV of salvage of new machine (35,000 $\times 0.386)$Less: Initial Outflow |  |  |  |  |  |  | $\begin{gathered} \hline 3,81,103 \\ 13,510 \end{gathered}$ |
|  |  |  |  |  |  |  | 3,94,613 |
|  |  |  |  |  |  |  | $(3,50,000)$ |
|  |  | Less: Initial Outflow |  |  |  |  | 44,613 |

Analysis: Since the Incremental NPV is positive, the old machine should be replaced.

## Working Notes:

## 1. Calculation of Base for Depreciation or Cost of New Machine:

| Cost of new machine | $₹ 4,50,000$ |
| :--- | :--- |
| Less: Sale value of old machine | $(₹ 1,00,000)$ |
|  | $₹ 3,50,000$ |

2. Calculation of Profit before tax and depreciation (PBTD) as per books:

| Particulars | Old Machine (₹) | New Machine (₹) | Difference (₹) |
| :--- | :---: | :---: | :---: |
| PBT as per books | $3,24,750$ | $3,87,250$ | 62,500 |
| Add: Depreciation as per books | 24,000 | 41,500 | 17,500 |
| PBTD |  | $3,48,750$ | $4,28,750$ |
| 80,000 |  |  |  |

## BQ 23

Xavly Ltd. has a machine which has been in operation for 3 years. The machine has a remaining estimated useful life of 5 years with no salvage value in the end. Its current market value is ₹ $2,00,000$. The company is considering a proposal to purchase a new model of machine to replace the existing machine. The relevant information is as follows:

| Particulars | Existing machine | New machine |
| :--- | :---: | :---: |
| Cost of machine | $₹ 3,30,000$ | $₹ 10,00,000$ |
| Estimated life | 8 years | 5 years |
| Salvage value | Nil | $₹ 40,000$ |
| Annual output | 30,000 units | 75,000 units |
| Selling price per unit | $₹ 15$ | $₹ 15$ |
| Annual operating hours | 3,000 | 3,000 |
| Material cost per unit | $₹ 4$ | $₹ 4$ |
| Labour cost per hour | $₹ 40$ | $₹ 70$ |
| Indirect cash cost per annum | $₹ 50,000$ | $₹ 65,000$ |

The company uses written down value of depreciation @ 20\% and it has several other machines in the block of assets. The Income tax rate is 30 per cent and Xavly Ltd. does not make any investment, if it yields less than 12 per cent.

| Year | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{P V F}$ | 0.893 | 0.797 | 0.712 | 0.636 | 0.567 |

Advise Xavly Ltd. whether the existing machine should be replaced or not.

## Answer

Statement of NPV

| Year | Particulars | ₹ | DF @ 12\% | PV |
| :---: | :--- | :---: | :---: | :---: |
| 0 | Initial outflows | $(8,00,000)$ | 1.000 | $(8,00,000)$ |
| 1 | Incremental CFAT | $3,21,000$ | 0.893 | $2,86,653$ |
| 2 | Incremental CFAT | $3,11,400$ | 0.797 | $2,48,186$ |
| 3 | Incremental CFAT | $3,03,720$ | 0.712 | $2,16,249$ |
| 4 | Incremental CFAT | $2,97,576$ | 0.636 | $1,89,258$ |
| 5 | Incremental CFAT + Incremental Salvage | $3,32,661$ | 0.567 | $1,88,619$ |
|  | $(2,92,661+40,000)$ |  |  | $\mathbf{3 , 2 8 , 9 6 5}$ |

Advise: The company should go ahead with replacement of machine, since it has positive NPV.

## Working Notes:

## 1. Calculation of initial outflow:

Cost of new machine ₹ $10,00,000$
Less: Sales value of old machine
(₹2,00,000)
Initial outflow
₹8,00,000
2. Increase in output $=75,000$ units $-30,000$ units $=45,000$ units
3. Base for incremental Depreciation:

| Particulars | ₹ |
| :---: | :---: |
| (A) WDV of Existing Machine: |  |
| Purchase price of existing machine | 3,30,000 |
| Less: Depreciation year $1 \quad(3,30,000 \times 20 \%)$ | $(66,000)$ |
| Less: Depreciation year $2 \quad(2,64,000 \times 20 \%)$ | $(52,800)$ |
| Less: Depreciation year $3 \quad(2,11,200 \times 20 \%)$ | $(42,240)$ |
| WDV of Existing Machine (A) | 1,68,960 |
| (B) Depreciation Base of New Machine: |  |
| Purchase price of new machine | 10,00,000 |
| Add: WDV of existing Machine | 1,68,960 |
| Less: Sale value of existing machine | $(2,00,000)$ |
| Depreciation Base of New Machine (B) | 9,68,960 |
| (C) Base for incremental Depreciation ( $B-A$ ) | 8,00,000 |

## 4. Calculation of incremental CFAT:

| Particulars | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Increase in Sales $(45,000 \times ₹ 15)$ <br> Less: Increase in Material cost <br> $(45,000$ units $\times$ ₹ 4$)$ | $6,75,000$ | $6,75,000$ | $6,75,000$ | $6,75,000$ | $6,75,000$ |
|  | $(1,80,000)$ | $(1,80,000)$ | $(1,80,000)$ | $(1,80,000)$ | $(1,80,000)$ |


| Less: Increase in Labour cost $\{3,000$ hours $\times(70-40)\}$ | (90,000) | $(90,000)$ | $(90,000)$ | $(90,000)$ | $(90,000)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Less: Increase in Indirect cash cost $(65,000-50,000)$ | $(15,000)$ | $(15,000)$ | $(15,000)$ | $(15,000)$ | $(15,000)$ |
| Less: Increase in Depreciation <br> (Base: 8,00,000) | $(1,60,000)$ | $(1,28,000)$ | $(1,02,400)$ | $(81,920)$ | $(65,536)$ |
| Incremental PBT | 2,30,000 | 2,62,000 | 2,87,600 | 3,08,080 | 3,24,464 |
| Less: Tax @ 30\% | $(69,000)$ | $(78,600)$ | $(86,280)$ | $(92,424)$ | $(97,339)$ |
| Incremental PAT | 1,61,000 | 1,83,400 | 2,01,320 | 2,15,656 | 2,27,125 |
| Add: Incremental Depreciation | 1,60,000 | 1,28,000 | 1,02,400 | 81,920 | 65,536 |
| Incremental CFAT | 3,21,000 | 3,11,400 | 3,03,720 | 2,97,576 | 2,92,661 |

Notes: Since company has several machines in $20 \%$ block of assets, there is no tax benefit or tax payment on loss or profit on sale of machine respectively because block will remain in existance.

## BQ 24

A \& Co. is contemplating whether to replace an existing machine or to spend money on overhauling it. A \& Co. currently pays no taxes. The replacement machine costs ₹ 90,000 now and requires maintenance of $₹ 10,000$ at the end of every year for eight years. At the end of eight years it would have a salvage value of ₹ 20,000 and would be sold. The existing machine requires increasing amounts of maintenance each year and its salvage value falls each year as follows:

| Year | Maintenance (₹) | Salvage ( $₹$ ) |
| :---: | :---: | :---: |
| Present | 0 | 40,000 |
| 1 | 10,000 | 25,000 |
| 2 | 20,000 | 15,000 |
| 3 | 30,000 | 10,000 |
| 4 | 40,000 | 0 |

The opportunity cost of capital for A \& Co. is $15 \%$. When should the company replace the machine?
Note: Present value of an annuity of Re. 1 per period for 8 years at interest rate of $15 \%: 4.4873$; present value of Re. 1 to be received after 8 years at interest rate of $15 \%: 0.3269$

## Answer

PV of Cost of Replacing the Old Machine in each 4 years with New Machine

| Scenario | Year | Cash Flow (\%) | PV @ 15\% | PV (₹) |
| :---: | :---: | :---: | :---: | :---: |
| Replace Immediately | 0 | $\begin{gathered} (28,600) \\ 40,000 \end{gathered}$ | $\begin{aligned} & 1.000 \\ & 1.000 \end{aligned}$ | $(28,600)$ |
|  |  |  |  | 40,000 |
|  |  |  |  | 11,400 |
| Replace in one year | 1 | $\begin{gathered} \hline(28,600) \\ (10,000) \\ 25,000 \end{gathered}$ | $\begin{aligned} & \hline 0.870 \\ & 0.870 \\ & 0.870 \end{aligned}$ | $(24,882)$ |
|  |  |  |  | $(8,700)$ |
|  |  |  |  | 21,750 |
|  |  |  |  | $(11,832)$ |
| Replace in 2 years | 1222 | $\begin{gathered} \hline(10,000) \\ (28,600) \\ (20,000) \\ 15,000 \end{gathered}$ | $\begin{aligned} & \hline 0.870 \\ & 0.756 \\ & 0.756 \\ & 0.756 \end{aligned}$ | $(8,700)$ |
|  |  |  |  | $(21,622)$ |
|  |  |  |  | $(15,120)$ |
|  |  |  |  | 11,340 |
|  |  |  |  | $(34,102)$ |
| Replace in 3 years | $\begin{aligned} & 1 \\ & 2 \end{aligned}$ | $(10,000)$ | $\begin{aligned} & \hline 0.870 \\ & 0.756 \end{aligned}$ | $\begin{gathered} (8,700) \\ (15,120) \\ \hline \end{gathered}$ |

$\left.\begin{array}{|l|l|c|c|c|}\hline & 3 & (20,000) & 0.658 & (18,819) \\ & 3 & (28,600) & 0.658 & (19,740) \\ & 3 & (30,000) & 0.658 \\ & & 10,000\end{array}\right)$

## Working Notes:

## Calculation of Equivalent Cost of New Machine:

| Particulars | $₹$ |
| :--- | :---: |
| Cost of new machine now | 90,000 |
| Add: PV of annual repairs @ 10,000 per annum for 8 years (10,000 $\times 4.4873)$ | 44,873 |
| Less: PV of salvage value at the end of 8 years $(20,000 \times 0.3269)$ | $(6,538)$ |
| Total PV of Outflows | $1,28,335$ |
| Equivalent annual cost $(\mathbf{1 , 2 8 , 3 3 5} \div \mathbf{4 . 4 8 7 3 )}$ | $\mathbf{2 8 , 6 0 0}$ |

Advice: The company should replace the old machine immediately because the PV of cost of replacing the old machine with new machine is least.

## ADJUSTED PV \& ADJUSTED DISCOUNT RATE

## BQ 25

XYZ Ltd. is presently all equity financed. The directors of the company have been evaluating investment in a project which will require ₹270 lakhs capital expenditure on new machinery. They expect the capital investment to provide annual cash flows of ₹ 42 lakhs indefinitely which is net of all tax adjustments. The discount rate which it applies to such investment decisions is $14 \%$ net.

The directors of the company believe that the current capital structure fails to take advantage of tax benefits of debt and propose to finance the new project with undated perpetual debt secured on the company's assets. The company intends to issue sufficient debt to cover the cost of capital expenditure and the after tax cost of issue.

The current annual gross rate of interest required by the market on corporate undated debt of similar risk is $10 \%$. The after tax costs of issue are expected to be ₹ 10 lakhs. Company's tax rate is $30 \%$.

## You are required to:

(a) Calculate the adjusted present value of the investment,
(b) Calculate the adjusted discount rate and
(c) Explain the circumstances under which this adjusted discount rate may be used to evaluate future investments.

## Answer

(a) Calculation of Adjusted Present Value of Investment (APV):

Adjusted PV = Base Case PV + PV of financing decisions associated with the project

Base Case NPV for the project:

| (-) ₹270 lakhs + (₹42 lakhs / 0.14) | = | (-) ₹270 lakhs + ₹ 300 lakhs | $=$ | ₹30 lakhs |
| :---: | :---: | :---: | :---: | :---: |
| Issue costs | = | ₹10 lakhs |  |  |
| Thus, the amount to be raised | = | ₹270 lakhs + ₹10 lakhs | = | ₹280 lakhs |
| Annual tax relief on interest | = | $₹ 280 \times 0.1 \times 0.3$ | = | ₹8.4 lakhs p.a. |
| The value of tax relief in perpetuity | $=$ | ₹8.4 lakhs / 0.1 | = | ₹84 lakhs |

Therefore, $A P V \quad=\quad$ Base case PV - Issue Costs + PV of Tax Relief on debt interest
$=$ ₹30 lakhs - ₹10 lakhs + ₹84 lakhs = ₹104 lakhs
(b) Calculation of Adjusted Discount Rate (ADR):

Annual Income or Savings required to allow an NPV to zero

| (-) ₹280 lakhs + (Annual Income / 0.14) | = | (-) ₹104 lakhs |  |
| :---: | :---: | :---: | :---: |
| Annual Income / 0.14 | = | (-) ₹104 lakhs + ₹ 280 lakhs |  |
| Therefore, Annual income | = | ₹ $176 \times 0.14$ | ₹ 24.64 lakhs |
| Adjusted discount rate | = | ( ₹ 24.64 lakhs / ₹ 280 lakhs) | $\times 100$ |
|  | = | 8.8\% |  |

(c) Useable circumstances:

This ADR may be used to evaluate future investments only if the business risk of the new venture is identical to the one being evaluated here and the project is to be financed by the same method on the same terms. The effect on the company's cost of capital of introducing debt into the capital structure cannot be ignored.

## INTERNAL RATE OF RETURN (IRR)

BQ 26
Using details given below, calculate IRR of an investment of ₹1,36,000:

| Year | Cash Inflows |
| :---: | :---: |
| 1 | $₹ 30,000$ |
| 2 | $₹ 40,000$ |
| 3 | $₹ 60,000$ |
| 4 | $₹ 30,000$ |
| 5 | $₹ 20,000$ |

## Answer

Let us calculate NPV by 10\% randomly:

| Years | ₹ | PVF @ 10\% | PV |
| :---: | :---: | :---: | :---: |
| 0 | $(1,36,000)$ | 1.000 | $(1,36,000)$ |
| 1 | 30,000 | 0.909 | 22,270 |
| 2 | 40,000 | 0.826 | 33,040 |


| 3 | 60,000 | 0.751 | 45,060 |
| :---: | :---: | :---: | :---: |
| 4 | 30,000 | 0.683 | 20,490 |
| 5 | 20,000 | 0.621 | 12,420 |
| $\boldsymbol{N P V}$ |  | $\mathbf{2 , 2 8 0}$ |  |

The net present value at $10 \%$ comes to ₹ 2,280 . Therefore, a higher discount rate is suggested, say, $12 \%$.

## NPV by 12\% randomly:

| Years | ₹ | PVF @ 12\% | PV |
| :---: | :---: | :---: | :---: |
| 0 | $(1,36,000)$ | 1.000 | $(1,36,000)$ |
| 1 | 30,000 | 0.893 | 26,790 |
| 2 | 40,000 | 0.797 | 31,880 |
| 3 | 60,000 | 0.712 | 42,720 |
| 4 | 30,000 | 0.636 | 19,080 |
| 5 | 20,000 | 0.567 | 11,340 |
| $\boldsymbol{N P V}$ |  |  | $\mathbf{( 4 , 1 9 0 )}$ |

The internal rate of return is, thus, more than $10 \%$ but less than $12 \%$. The exact rate can be obtained by interpolation:

$$
\begin{aligned}
\operatorname{IRR} & =\mathrm{L}+\frac{\mathrm{NPV}_{\mathrm{L}}}{\mathrm{NPV}_{\mathrm{L}}-\mathrm{NPV}_{\mathrm{H}}} \times(\mathrm{H}-\mathrm{L})=10 \%+\frac{2,280}{2,280-(-4,190)} \times(12 \%-10 \%) \\
& =\mathbf{1 0 . 7 0 \%}
\end{aligned}
$$

## BQ 27

A Ltd. is evaluating a project involving an outlay of ₹ $10,00,000$ resulting in an annual cash inflow of ₹2,50,000 for 6 years. Assuming salvage value of the project is zero determine the IRR of the project.

## Answer

First of all we shall find an approximation of the payback ( $\mathrm{PVIFA}_{\mathrm{IRR}}$ ) period:

$$
\text { PVIFA }_{\text {IRR }} \quad=10,00,000 \div 2,50,000 \quad=4
$$

Now we shall search this figure in the PVAF table corresponding to 6 years row. The value 4 lies between values 4.111 and 3.998 correspondingly discounting rates $12 \%$ and $13 \%$ respectively.

$$
\begin{array}{llll}
\mathrm{NPV}_{12 \%} & =(10,00,000)+4.111 \times 2,50,000 & =27,750 \\
\mathrm{NPV}_{13 \%} & =(10,00,000)+3.998 \times 2,50,000 & =(500)
\end{array}
$$

The internal rate of return is, thus, more than $12 \%$ but less than $13 \%$. The exact rate can be obtained by interpolation:

$$
\text { IRR } \quad=\quad 12 \%+\frac{2,775}{2,775-(-50)} \times(13 \%-12 \%) \quad=\quad 12.98 \%
$$

## BQ 28

A Company proposes to install a machine involving a capital cost of $₹ 3,60,000$. The life of the machine is 5 years and its salvage value at the end of the life is nil. The machine will produce the net operating income after depreciation of ₹ 68,000 per annum. The Company's tax rate is $45 \%$.

| Discounting Rate: | $14 \%$ | $15 \%$ | $16 \%$ | $17 \%$ | $18 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Cumulative factor: | 3.43 | 3.35 | 3.27 | 3.20 | 3.13 |

## You are required to calculate the internal rate of return of the proposal.

## Answer

$$
\text { Sum of DF @ IRR for } 4 \text { years }=\frac{\text { PV of outflow }}{\text { Annual CFAT }}=\frac{3,60,000}{1,09,400}=3.29
$$

The internal rate of return is, thus, more than $15 \%$ but less than $16 \%$. The exact rate can be obtained by interpolation:

$$
\operatorname{IRR}=\quad=\quad \mathrm{LR}+\frac{\mathrm{NPV}}{\mathrm{NPV} \mathrm{~V}_{\mathrm{LR}}-\mathrm{NPV}_{\mathrm{HR}}} \times(\mathrm{HR}-\mathrm{LR})=15 \%+\frac{6,490}{6,490+2,262} \times(16 \%-15 \%)
$$

$$
=\quad 15.74 \%
$$

## Calculation of NPV at 15\% and 16\%:

$$
\begin{aligned}
& \mathrm{NPV}_{15 \%}=(3,60,000)+3.35 \times 1,09,400=6,490 \\
& \mathrm{NPV}_{16 \%}=(3,60,000)+3.27 \times 1,09,400=(2,262)
\end{aligned}
$$

## Computation of cash inflow per annum:

| Net operating income per annum | ₹ 68,000 |
| :--- | ---: |
| Less: Tax @ 45\% | $₹ 30,600$ |
| Profit after tax | $₹ 37,400$ |
| Add: Depreciation (₹3,60,000 $\div 5$ years) | $₹ 72,000$ |
| Cash inflow (CFAT) | ₹1,09,400 |

## BQ 29

The cash of flows of projects X and Y are given below:
Cash Flow ( ${ }^{\text {( }}$ )

| Projects | Year 0 | Year 1 | Year 2 | Year 3 | NPV @ 10\% | IRR |
| :---: | ---: | ---: | :---: | ---: | :---: | :---: |
| X | $-10,000$ | $+2,000$ | $+4,000$ | $+12,000$ | $+4,134$ | $26.5 \%$ |
| Y | $-10,000$ | $+10,000$ | $+3,000$ | $+3,000$ | $+3,821$ | $37.6 \%$ |

(a) Why is there a conflict in ranking?
(b) Why should you recommend project X in spite of a lower rate of return?

## Answer

(a) Out of the two projects X and Y, the former is having higher NPV ( $10 \%$ rate) of ₹ 4,134 and is preferable. However, as per the IRR method the Project Y is preferable as it having IRR of $37.6 \%$. So, there is a conflict in ranking of projects.

The reason for this conflict may be traced in the pattern of cash inflows estimating from two projects. It may be noticed that inflows from project X are higher is later years while from Project Y the cash inflows are higher in earlier years. The reinvestment rate assumption implies that inflows are reinvested in the NPV method at the discount rate, while in case of IRR method the inflows are reinvested at IRR rate itself. The pattern of inflows and the reinvestment rate assumption make the ranking to differ from each other.
(b) Inspite of lower IRR of $26.5 \%$ the project X may be recommended as it is having the incremental NPV of ₹313 (₹4,134-₹3,821) and will lead to higher increase in the wealth of the shareholders.

MODIFIED INTERNAL RATE OF RETURN (MIRR)

BQ 30
Using details given below, calculate MIRR considering 8\% cost of Capital.

| Year | Cash Flow |
| :---: | :---: |
| 0 | $(₹ 1,36,000)$ |
| 1 | $₹ 30,000$ |
| 2 | $₹ 40,000$ |
| 3 | $₹ 60,000$ |
| 4 | $₹ 30,000$ |
| 5 | $₹ 20,000$ |

## Answer

Statement of Compounding Value

| Years | Particulars | ₹ | CVF @ 8\% | CV |
| :---: | :--- | :---: | :---: | :---: |
| 1 | Cash inflow | 30,000 | 1.3605 | 40,815 |
| 2 | Cash inflow | 40,000 | 1.2597 | 50,388 |
| 3 | Cash inflow | 60,000 | 1.1664 | 69,984 |
| 4 | Cash inflow | 30,000 | 1.0800 | 32,400 |
| 5 | Cash inflow | 20,000 | 1.0000 | 20,000 |
| Compound Value of Cash Inflow |  |  |  | $\mathbf{2 , 1 3 , 5 8 7}$ |

## Calculation of MIRR:

| Compound Factor | $=\frac{\text { Compound value of inflow }}{\text { Initial outflow }}=\frac{2,13,587}{1,36,000}=1.5705$ |
| ---: | :--- |
| MIRR | $=\sqrt[5]{1.5705}-1$ |

## MISCELLANEOUS

BQ 31
Navjeevani hospital is considering to purchase a machine for medical projectional radiography which is priced at $₹ 2,00,000$. The projected life of the machine is 8 years and has an expected salvage value of $₹ 18,000$ at the end of $8^{\text {th }}$ year. The annual operating cost of the machine is $₹ 22,500$. It is expected to generate revenues of $₹ 1,20,000$ per year for eight years. Presently, the hospital is outsourcing the radiography work to its neighbour Test Center and is earning commission income of ₹ 36,000 per annum, net of taxes. Consider tax @30\%.

Analyse whether it would be profitable for the hospital to purchase the machine? Give your recommendation under:
(i) Net Present Value method,
(ii) Profitability Index method.

PV factors at 10\% are given below:

| Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 | Year 7 | Year 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.909 | 0.826 | 0.751 | 0.683 | 0.621 | 0.564 | 0.513 | 0.467 |

## Answer

(i) Net Present Value

| Year | Particulars | ₹ | DF @ 10\% | PV |
| :---: | :--- | :---: | :---: | :---: |
| 0 | Initial outflows | $(2,00,000)$ | 1.000 | $(2,00,000)$ |
| $1-8$ | Cash Flow After Tax | 39,075 | 5.334 | $2,08,426$ |
| 8 | Salvage | 18,000 | 0.467 | 8,406 |
| $\mathbf{N P V}$ |  |  |  | $\mathbf{1 6 , 8 3 2}$ |

(ii) Profitability Index $=\frac{\mathrm{PV} \text { of Inflows }}{\mathrm{PV} \text { of Outflows }}=\frac{2,16,832}{2,00,000}=1.084$

## Working Notes:

Calculation of CFAT:

| Particulars | $₹$ |
| :--- | :---: |
| Sales | $1,20,000$ |
| Less: Operating cost | 22,500 |
| Less: Depreciation $(2,00,000-18,000) \div 8$ years | 22,750 |
| Net Income | 74,750 |
| Less: Tax @ 30\% | 22,425 |
| PAT | 52,325 |
| Add: Depreciation | 22,750 |
| Cash inflows after tax per annum | 75,075 |
| Less: Loss of commission income | 36,000 |
| Net CFAT | $\mathbf{3 9 , 0 7 5}$ |

Advise: Since the net present value (NPV) is positive and profitability index is also greater than 1, the hospital may purchase the machine.

## BQ 32

Lockwood Limited wants to replace its old machine with a new automatic machine. Two models A and $B$ are available at the same cost of ₹ 5 lakhs each. Salvage value of the old machine is ₹ 1 lakh. The utilities of the existing machine can be used if the company purchases A. Additional cost of utilities to be purchased in that case are ₹1 lakh. If the company purchases B then all the existing utilities will have to be replaced with new utilities costing ₹2 lakhs. The salvage value of the old utilities will be ₹ 0.20 lakhs. The cash flows after taxation are expected to be:

| Year | $\boldsymbol{A}$ | $\boldsymbol{B}$ |
| :---: | :---: | :---: |
| 1 | $₹ 1,00,000$ | $₹ 2,00,000$ |
| 2 | $₹ 1,50,000$ | $₹ 2,10,000$ |
| 3 | $₹ 1,80,000$ | $₹ 1,80,000$ |
| 4 | $₹ 2,00,000$ | $₹ 1,70,000$ |
| 5 | $₹ 1,70,000$ | $₹ 40,000$ |
| Salvage Value at the end of Year 5 | $₹ 50,000$ | $₹ 60,000$ |

The targeted return on capital is $15 \%$.

## You are required to:

(a) Compute, for the two machines separately, Net Present Value, Discounted Payback Period and Desirability Factor and
(b) Advice which of the machines is to be selected?

## Answer

(a) Net Present Value

| Year | NPV Factor @ | Machine A |  | Machine B |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{1 5 \%}$ | Cash Inflows | Discounted CF | Cash Inflows | Discounted CF |
| 0 | 1.0000 | $(5,00,000)$ | $(5,00,000)$ | $(5,80,000)$ | $(5,80,000)$ |
| 1 | 0.8696 | $1,00,000$ | 86,960 | $2,00,000$ | $1,73,920$ |
| 2 | 0.7561 | $1,50,000$ | $1,13,415$ | $2,10,000$ | $1,58,781$ |
| 3 | 0.6575 | $1,80,000$ | $1,18,350$ | $1,80,000$ | $1,18,350$ |
| 4 | 0.5718 | $2,00,000$ | $1,14,360$ | $1,70,000$ | 97,206 |
| 5 | 0.4972 | $1,70,000$ | 84,524 | 40,000 | 19,888 |
| Salvage | 0.4972 | 50,000 | 24,860 | 60,000 | 29,832 |
| NPV |  |  | $\mathbf{4 2 , 4 6 9}$ |  | $\mathbf{1 7 , 9 7 7}$ |

Discounted Payback Period

| Year | Machine A |  | Machine B |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Discounted CF | Cum Discounted CF | Discounted CF | Cum Discounted CF |
| 1 | 86,960 | 86,960 | $1,73,920$ | $1,73,920$ |
| 2 | $1,13,415$ | $2,00,375$ | $1,58,781$ | $3,32,701$ |
| 3 | $1,18,350$ | $3,18,725$ | $1,18,350$ | $4,51,051$ |
| 4 | $1,14,360$ | $4,33,085$ | 97,206 | $5,48,257$ |
| 5 | $1,09,384$ | $5,42,469$ | 49,720 | $5,97,977$ |


| Machine $A$ | $=$ | 4 years $+\frac{5,00,000-4,33,085}{1,09,384}$ | $=4.612 y$ |
| ---: | :--- | ---: | :--- |
| Machine $B$ | $=$ | 4 years $+\frac{5,80,000-5,48,257}{49,720}$ | $=4.638 y$ |
| Profitability Index (PI) | $=\frac{\mathrm{PV} \text { of Inflows }}{\text { PV of Outflows }}$ |  |  |
| Machine A | $=\frac{5,42,469}{5,00,000}$ | $=$ | 1.085 |
| Machine B | $=\frac{5,97,977}{5,80,000}$ | $=1.031$ |  |

## Working note:

Calculation of Initial Investment

| Particulars | Machine $\boldsymbol{A}$ | Machine $\boldsymbol{B}$ |
| :--- | :---: | :---: |
| Cost of Machine | $5,00,000$ | $5,00,000$ |
| Add: Cost of Utilities | $1,00,000$ | $2,00,000$ |
| Less: Salvage of Old Machine | $(1,00,000)$ | $(1,00,000)$ |
| Less: Salvage of Old Utilities | - | $(20,000)$ |
| Initial Investment | $\mathbf{F 5}, 00,000$ | $\mathbf{F 5 , 8 0 , 0 0 0}$ |

(b) Since the absolute surplus in the case of A is more than B and also the desirability factor, it is better to choose A. The discounted payback period in both the cases is same, also the net present value is
positive in both the cases but the desirability factor (profitability index) is higher in the case of Machine A, it is therefore better to choose Machine A.

## BQ 33

Hindlever Company is considering a new product line to supplement its range line. It is anticipated that the new product line will involve cash investments of ₹ $7,00,000$ at time 0 and ₹ $10,00,000$ in year 1. After-tax cash inflows of ₹ $2,50,000$ are expected in year 2 , ₹ $3,00,000$ in year $3, ₹ 3,50,000$ in year 4 and $₹ 4,00,000$ each year thereafter through year 10 . Although the product line might be viable after year 10, the company prefers to be conservative and end all calculations at that time.
(a) If the required rate of return is 15 per cent, what is the net present value of the project? Is it acceptable?
(b) What would be the case if the required rate of return were 10 per cent?
(c) What is its internal rate of return?
(d) What is the project's payback period?

## Answer

(a) Statement of NPV

| Years | Cash Inflow ( $₹$ ) | PVF @ 15\% | Present Value |
| :---: | :---: | :---: | :---: |
| 0 | $(7,00,000)$ | 1.000 | $(7,00,000)$ |
| 1 | $(10,00,000)$ | 0.870 | $(8,70,000)$ |
| 2 | $2,50,000$ | 0.756 | $1,89,000$ |
| 3 | $3,00,000$ | 0.658 | $1,97,400$ |
| 4 | $3,50,000$ | 0.572 | $2,00,200$ |
| $5-10$ | $4,00,000$ | 2.164 | $8,65,600$ |
| $\boldsymbol{N P V}$ |  |  | $\mathbf{( 1 , 1 7 , 8 0 0}$ |

(b) Statement of NPV

| Years | ₹ | PVF @ 10\% | $\boldsymbol{P V}$ |
| :---: | :---: | :---: | :---: |
| 0 | $(7,00,000)$ | 1.000 | $(7,00,000)$ |
| 1 | $(10,00,000)$ | 0.909 | $(9,09,000)$ |
| 2 | $2,50,000$ | 0.826 | $2,06,500$ |
| 3 | $3,00,000$ | 0.751 | $2,25,300$ |
| 4 | $3,50,000$ | 0.683 | $2,39,050$ |
| $5-10$ | $4,00,000$ | 2.975 | $11,90,000$ |
| $\boldsymbol{N P V} \boldsymbol{V}$ |  |  | $\mathbf{2 , 5 1 , 8 5 0}$ |

(c) IRR

$$
=\quad \mathrm{LR}+\frac{\mathrm{NPV}_{\mathrm{LR}}}{\mathrm{NPV}_{\mathrm{LR}}-\mathrm{NPV}_{\mathrm{HR}}} \times(\mathrm{HR}-\mathrm{LR})=10 \%+\frac{2,51,850}{2,51,850+1,17,800} \times(15 \%-10 \%)
$$

= $13.41 \%$
(d)

$$
\begin{aligned}
\text { Payback Period }= & -7,00,000-10,00,000+2,50,000+3,00,000+3,50,000+4,00,000+ \\
& =\quad 6,00,000
\end{aligned}
$$

## BQ 34

Elite Cooker Company is evaluating three investment situations: (1) produce a new line of aluminum skillets, (2) expand its existing cooker line to include several new sizes, and (3) develop a new, higherquality line of cookers. If only the project in question is undertaken, the expected present values and the amounts of investment required are:

| Project | Investment required | PV of future cash flows |
| :---: | :---: | :---: |
| 1 | $₹ 2,00,000$ | $₹ 2,90,000$ |
| 2 | $₹ 1,15,000$ | $₹ 1,85,000$ |
| 3 | $₹ 2,70,000$ | $₹ 4,00,000$ |

If projects 1 and 2 are jointly undertaken, there will be no economies; the investments required and present values will simply be the sum of the parts. With projects 1 and 3 , economies are possible in investment because one of the machines acquired can be used in both production processes. The total investment required for projects 1 and 3 combined is $₹ 4,40,000$. If projects 2 and 3 are undertaken, there are economies to be achieved in marketing and producing the products but not in investment. The expected present value of future cash flows for projects 2 and 3 is ₹ $6,20,000$. If all three projects are undertaken simultaneously, the economies noted will still hold. However, a ₹ $1,25,000$ extension on the plant will be necessary, as space is not available for all three projects.

Which project or projects should be chosen?

## Answer

## Statement of Cumulative NPV of Different Combinations

| Project | Investment required | PV offuture CF | Net Present Value |
| :---: | :---: | :---: | :---: |
| 1 | $₹ 2,00,000$ | $₹ 2,90,000$ | $₹ 90,000$ |
| 2 | $₹ 1,15,000$ | $₹ 1,85,000$ | $₹ 70,000$ |
| 3 | $₹ 2,70,000$ | $₹ 4,00,000$ | $₹ 1,30,000$ |
| 1 and 2 | $₹ 3,15,000$ | $₹ 4,75,000$ | $₹ 1,60,000$ |
| 1 and 3 | $₹ 4,40,000$ | $₹ 6,90,000$ | $₹ 2,50,000$ |
| 2 and 3 | $₹ 3,85,000$ | $₹ 6,20,000$ | $₹ 2,35,000$ |
| 1,2 and 3 | $₹ 6,80,000^{*}$ | $₹ 9,10,000$ | $₹ 2,30,000$ |
| (Refer working note) |  |  |  |

## Calculation of total investment required if all the three projects are undertaken simultaneously:

Total investment $=$ Investment in project $1 \& 3+$ Investment in project $2+$ Plant extension cost

$$
=4,40,000+1,15,000+1,25,000=\text { F } 6,80,000
$$

Advise: Projects 1 and 3 should be chosen, as they provide the highest net present value.

## BQ 35

Following data has been available for a capital project:

| Annual cost of saving | $₹ 1,00,000$ |
| :--- | :--- |
| Useful life | 4 years |
| Salvage value | zero |
| Internal rate of return | $12 \%$ |
| Profitability index | 1.064 |

You are required to calculate the following for this project:
(a) Cost of the project
(b) Cost of capital
(c) Net present value
(d) Payback period

## PV factors at different rates are given below:

| Discount Factor | Years |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ |
| $12 \%$ | 0.893 | 0.797 | 0.712 | 0.636 |
| $11 \%$ | 0.901 | 0.812 | 0.731 | 0.659 |
| $10 \%$ | 0.909 | 0.826 | 0.751 | 0.683 |
| $9 \%$ | 0.917 | 0.842 | 0.772 | 0.702 |

## Answer

(a) Cost of the project:

At IRR,

Present value of inflows
Present value of outflows
$=\quad$ Present value of outflows
$=\quad$ Annual cost of saving $\times$ Cumulative discount factor @ IRR $12 \%$ for 4 years
$=$ ₹ $1,00,000 \times 3.038$
$=$ F3,03,800
(b) Cost of Capital:

Cum DF @ cost of capital for 4 years $=\frac{\text { Present Value of Inflows }}{\text { Annual Inflows }}=\frac{3,23,243.20}{1,00,000}$
$=3.232$
From the discount factor table, at discount rate of 9\%, the cumulative discount factor for four years is $3.233(0.917+0.842+0.772+0.702)$

Hence, Cost of capital
$=\quad 9 \%$
(c) Net Present Value of cash inflows:

| PI | = | PV of Inflows |  |
| :---: | :---: | :---: | :---: |
|  |  | PV of Outflows |  |
| 1.064 | $=$ | PV of Inflows |  |
|  |  | 3,03,800 |  |
| PV of Inflows | = | $3,03,800 \times 1.064=$ | F3,23,243 |
| NPV | = | PV of inflows - PV of outflows |  |
|  | = | $₹ 3,23,243.20$ - ₹3,03,800 = | ₹19,443.20 |

(d) Payback Period:

$$
\text { Payback period } \quad=\frac{\text { Initial Outflow }}{\text { Equal Annual Cash Inflows }}=\frac{3,03,800}{1,00,000}
$$

$$
=\quad 3.038 \text { years }
$$

BQ 36
Alley Pvt. Ltd. is planning to invest in a machinery that would cost ₹ $1,00,000$ at the beginning of year 1. Net cash inflows from operations have been estimated at ₹ 36,000 per annum for 3 years. The company has two options for smooth functioning of the machinery: one is service, and another is replacement of parts. If the company opts to service a part of the machinery at the end of year 1 at ₹ 20,000 , in such a case, the scrap value at the end of year 3 will be ₹ 25,000 . However, if the company decides not to service the part, then it will have to be replaced at the end of year 2 at $₹ 30,800$ and in this case, the machinery
will work for the $4^{\text {th }}$ year also and get operational cash inflow of $₹ 36,000$ for the $4^{\text {th }}$ year. It will have to be scrapped at the end of year 4 at $₹ 18,000$.

Assuming cost of capital at $10 \%$ and ignoring taxes, determine the purchase of this machinery based on the net present value of its cash flows? If the supplier gives a discount of $\mathfrak{F} 10,000$ for purchase, what would be your decision?

The PV factors at $10 \%$ are:

| Year | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PV Factor | 1 | 0.9091 | 0.8264 | 0.7513 | 0.6830 | 0.6209 | 0.5645 |

## Answer

Option 1 (Part of the Machine is serviced):
Statement of NPV

| Year | Particulars | ₹ | PV Factor @ 10\% | PV of Cash flow |
| :---: | :--- | :---: | :---: | :---: |
| 0 | Initial Outflows | $(1,00,000)$ | 1.0000 | $(1,00,000)$ |
| 1 | Inflows - Service | $36,000-20,000$ | 0.9091 | 14,546 |
| 2 | Charges | 36,000 | 0.8264 | 29,750 |
| 3 | Inflows | $36,000+25,000$ | 0.7513 | 45,829 |
|  | Inflows + Salvage | NPV |  |  |
| $\mathbf{( 9 , 8 7 5 )}$ |  |  |  |  |

Option 2 (Part of the Machine is replaced):
Statement of NPV

| Year | Particulars | ₹ | PV Factor @ 10\% | PV of Cash flow |
| :---: | :--- | :---: | :---: | :---: |
| 0 | Initial Outflows | $(1,00,000$ | 1.0000 | $(1,00,000)$ |
| 1 | Inflows | 36,000 | 0.9091 | 32,728 |
| 2 | Inflows - Replacement | $36,000-30,800$ | 0.8264 | 4,297 |
| 3 | Inflows | 36,000 | 0.7513 | 27,047 |
| 4 | Inflows + Salvage | $36,000+18,000$ | 0.6830 | 36,882 |
| NPV |  |  |  | $\mathbf{9 5 4}$ |

Decision: Option I has a negative NPV whereas option II has a positive NPV ₹954. Therefore, option II (replacement of part) shall be opted.

If the supplier gives a discount of $\mathfrak{₹ 1 0 , 0 0 0}$ for purchases:

| Option 1: NPV | $=$ | $(9,875)+10,000$ | $=$ | 125 |
| :--- | :--- | :--- | :--- | :--- |
| Option 2: NPV | $=$ | $954+10,000$ |  | 10,954 |

Decision: Option I with very small NPV is not considerable, Option II having higher NPV shall be opted (student can also show annualized NPV due to difference in life of projects).

BQ 37
A large profit making company is considering the installation of a machine to process the waste produced by one of its existing manufacturing process to be converted into a marketable product. At present, the waste is removed by a contractor for disposal on payment by the company of ₹ 150 lakh per
annum for the next four years. The contract can be terminated upon installation of the aforesaid machine on payment of a compensation of ₹ 90 lakh before the processing operation starts. This compensation is not allowed as deduction for tax purposes.

The machine required for carrying out the processing will cost ₹ 600 lakh. At the end of the $4^{\text {th }}$ year, the machine can be sold for ₹ 60 lakh and the cost of dismantling and removal will be ₹ 45 lakh.

Sales and direct costs of the product emerging from waste processing for 4 years are estimated as under:
(₹In Lakh)

| Year | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ |
| :--- | :---: | :---: | :---: | :---: |
| Sales | 966 | 966 | 1,254 | 1,254 |
| Material consumption | 90 | 120 | 255 | 255 |
| Wages | 225 | 225 | 255 | 300 |
| Other expenses | 120 | 135 | 162 | 210 |
| Factory overheads | 165 | 180 | 330 | 435 |
| Depreciation (as per income tax rules) | 150 | 114 | 84 | 63 |

Initial stock of materials required before commencement of the processing operations is ₹ 60 lakh at the start of year 1 . The stock levels of materials to be maintained at the end of year 1,2 and 3 will be ₹ 165 lakh and the stocks at the end of year 4 will be nil. The storage of materials will utilise space which would otherwise have been rented out for ₹ 30 lakh per annum. Labour costs include wages of 40 workers, whose transfer to this process will reduce idle time payments of ₹ 45 lakh in the year 1 and ₹ 30 lakh in the year 2. Factory overheads include apportionment of general factory overheads except to the extent of insurance charges of ₹ 90 lakh per annum payable on this venture. The company's tax rate is $30 \%$.

## Present value factors for four years are as under:

| Year | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: |
| PV Factors @14\% | 0.877 | 0.769 | 0.674 | 0.592 |

Advise the management on the desirability of installing the machine for processing the waste. All calculations should form part of the answer.

## Answer

| Net Present Value |  | (₹In Lakh) |  |  |
| :---: | :--- | :---: | :---: | :---: |
| Year | Particulars | ₹ | DF @ 14\% | PV |
| 0 | Initial outflows (Cost of Machine + Compensation | $(750)$ | 1.000 | $(750)$ |
|  | + Material stock) (600 + 90 + 60) |  |  |  |
| 1 | CFAT - Increase in stock (469.2-105) | 364.2 | 0.877 | 319.40 |
| 2 | CFAT | 416.4 | 0.769 | 320.21 |
| 3 | CFAT | 453.6 | 0.674 | 305.73 |
| 4 | CFAT + Decrease in stock + Net salvage | 562.2 | 0.592 | 332.82 |
|  | $(382.2+165+15)$ |  |  | $\mathbf{5 P V}$ |
|  |  |  |  |  |

Advice: Since the net present value of cash flows is ₹ 528.16 lakhs which is positive the management should install the machine for processing the waste.

| Statement of CFAT |  |  | (₹In Lakh) |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Particulars | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ |
| Sales | 966 | 966 | 1,254 | 1,254 |
| Add: Saving in Contract payment | 150 | 150 | 150 | 150 |


| Less: Material consumption | $(90)$ | $(120)$ | $(255)$ | $(255)$ |
| :--- | :---: | :---: | :---: | :---: |
| Less: Wages (net of reduction in idle time) | $(180)$ | $(195)$ | $(255)$ | $(300)$ |
| Less: Other expenses | $(120)$ | $(135)$ | $(162)$ | $(210)$ |
| Less: Factory overheads (only insurance charges) | $(90)$ | $(90)$ | $(90)$ | $(90)$ |
| Less: Loss of rent (opportunity cost) | $(30)$ | $(30)$ | $(30)$ | $(30)$ |
| Less: Depreciation (as per income tax rules) | $(150)$ | $(114)$ | $(84)$ | $(63)$ |
| PBT | 456 | 432 | 528 | 456 |
| Less: Tax @ 30\% | $(136.8)$ | $(129.6)$ | $(158.4)$ | $(136.8)$ |
| PAT | 319.2 | 302.4 | 369.6 | 319.2 |
| Add: Depreciation $\quad$ CFAT | 150 | 114 | 84 | 63 |
|  | $\mathbf{4 6 9 . 2}$ | $\mathbf{4 1 6 . 4}$ | $\mathbf{4 5 3 . 6}$ | $\mathbf{3 8 2 . 2}$ |

## Notes:

1. Material stock increases are taken in cash flows.
2. Idle time wages have also been considered.
3. Apportioned factory overheads are not relevant only insurance charges of this project are relevant.
4. Sale of machinery - Net income after deducting removal expenses taken. Tax on Capital gains is ignored.
5. Saving in contract payment and income tax thereon is considered in the cash flows.

## BQ 38

Alpha Company is considering the following investment projects:

| Projects | Cash Flows ( ₹) |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\boldsymbol{C}_{\boldsymbol{0}}$ | $\boldsymbol{C}_{\boldsymbol{1}}$ | $\boldsymbol{C}_{\boldsymbol{2}}$ | $\boldsymbol{C}_{\boldsymbol{3}}$ |
| A | $-10,000$ | $+10,000$ |  |  |
| B | $-10,000$ | $+7,500$ | $+7,500$ |  |
| C | $-10,000$ | $+2,000$ | $+4,000$ | $+12,000$ |
| D | $-10,000$ | $+10,000$ | $+3,000$ | $+3,000$ |

(a) Rank the projects according to each of the following methods: (i) Payback, (ii) ARR, (iii) IRR and (iv) NPV, assuming discount rates of 10 and 30 per cent.
(b) Assuming the projects are independent, which one should be accepted? If the projects are mutually exclusive, which project is the best?

## Answer

(a) Calculation of Payback, ARR, IRR and NPV:
(i) Payback Period:

| Project A | $=$ | $10,000 \div 10,000$ | $=$ |
| :--- | :--- | :--- | :--- |
| Project B | $=$ | year |  |
| Project C | $=$ | $=$ | 1.33 years |
| Project D | $=1000+2,500 \div 7,500$ | $=$ | 2.33 years |
|  |  | $10,000 \div 10,000$ | $=14$ year |

(ii) ARR using average investment base:

| Project A | $=\frac{(10,000-10,000)}{10,000 \times 1 / 2} \times 100$ | $=\mathbf{0} \%$ |
| :--- | :--- | :--- |
| Project B | $=\frac{(15,000-10,000) \div 2}{10,000 \times 1 / 2} \times 100$ | $=\mathbf{5 0 \%}$ |


| Project C | $=\frac{(18,000-10,000) \div 3}{10,000 \times 1 / 2} \times 100$ | $=53.33 \%$ |
| :--- | :--- | :--- |
| Project D | $=\frac{(16,000-10,000) \div 3}{10,000 \times 1 / 2} \times 100$ | $=40 \%$ |

Note: Average book profit is found by deducting initial investment, otherwise student may deduct depreciation year wise.

## (iii) IRR:

Project $\boldsymbol{A}$ (The net cash proceeds in year 1 are just equal to investment):
IRR $=0 \%$
Project B (Uniform cash inflow, so we can calculate IRR by PVAF):
PVAF for 2 years $=10,000 \div 7,500=1.33$ (This factor is found under $32 \%$ )
IRR $=32 \%$
Project C (Unequal cash inflow, so we can calculate IRR by computing NPV using random rates):
NPV at $20 \%=2,000 \times 0.833+4,000 \times 0.694+12,000 \times 0.579-10,000=+1,390$
NPV at $30 \%=2,000 \times 0.769+4,000 \times 0.592+12,000 \times 0.455-10,000=-634$
IRR $\quad=\quad \mathrm{L}+\frac{\mathrm{NPV}_{\mathrm{L}}}{\mathrm{NPV}_{\mathrm{L}}-\mathrm{NPV}_{\mathrm{H}}} \times(\mathrm{H}-\mathrm{L}) \quad=20 \%+\frac{1,390}{1,390-(-634)} \times(30 \%-20 \%)$
$=26.87 \%$
Project D (Unequal cash inflow, so we can calculate IRR by computing NPV using random rates):

| NPV at $30 \%$ | $=10,000 \times 0.769+3,000 \times 0.592+3,000 \times 0.455-10,000$ |
| ---: | :--- |
|  | $=+831$ |
| NPV at $40 \%$ | $=10,000 \times 0.714+3,000 \times 0.510+3,000 \times 0.364-10,000$ |
|  | $=-238$ |
| IRR | $=\mathrm{L}+\frac{\mathrm{NPV}_{\mathrm{L}}}{\mathrm{NPV}_{\mathrm{L}}-\mathrm{NPV}_{\mathrm{H}}} \times(\mathrm{H}-\mathrm{L})=30 \%+\frac{831}{831-(-238)} \times(40 \%-30 \%)$ |
|  | $=37.77 \%$ |

## (iv) $N P V$ :

## Project A:

| NPV at $10 \%$ | $=$ | $=$ | -910 |
| :--- | :--- | :--- | :--- |
| NPV at $30 \%$ | $=$ | $=$ | $-2,310$ |

## Project B:

NPV at $10 \%=7,500 \times(0.909+0.826)-10,000=\quad+3,013$
NPV at $30 \% \quad=\quad 7,500 \times(0.769+0.592)-10,000=\quad+208$

## Project C:

NPV at $10 \%=2,000 \times 0.909+4,000 \times 0.826+12,000 \times 0.751-10,000$

$$
\begin{array}{rll} 
& = & +4,134 \\
\text { NPV at } 30 \% & = & 2,000 \times 0.769+4,000 \times 0.592+12,000 \times 0.455-10,000 \\
& = & -633
\end{array}
$$

## Project D:

| NPV at $10 \%$ | $=$ | $10,000 \times 0.909+3,000 \times(0.826+0.751)-10,000=$ | $+3,821$ |
| :--- | :--- | :--- | :--- |
| NPV at $30 \%$ | $=$ | $10,000 \times 0.769+3,000 \times(0.592+0.455)-10,000=$ | +831 |

The projects are ranked as follows according to the various methods:

| Ranks |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Projects | PBP | ARR | IRR | NPV 10\% | NPV 30\% |  |
| A | 1 | 4 | 4 | 4 | 4 |  |
| B | 2 | 2 | 2 | 3 | 2 |  |
| C | 3 | 1 | 3 | 1 | 3 |  |
| D | 1 | 3 | 1 | 2 | 1 |  |

(b) Payback and ARR are theoretically unsound method for choosing between the investment projects. Between the two time-adjusted (DCF) investment criteria, NPV and IRR, NPV gives consistent results. If the projects are independent (and there is no capital rationing), either IRR or NPV can be used since the same set of projects will be accepted by any of the methods. In the present case, except Project A all the three projects should be accepted if the discount rate is $10 \%$. Only Projects B and D should be undertaken if the discount rate is $30 \%$.

If it is assumed that the projects are mutually exclusive, then under the assumption of $30 \%$ discount rate, the choice is between B and D ( A and C are unprofitable). Both criteria IRR and NPV give the same results - D is the best. Under the assumption of $10 \%$ discount rate, ranking according to IRR and NPV conflict (except for Project A). If the IRR rule is followed, Project D should be accepted. But the NPV rule tells that Project C is the best. The NPV rule generally gives consistent results in conformity with the wealth maximization principle. Therefore, Project C should be accepted following the NPV rule.

## BQ 39

The expected cash flows of three projects are given below. The cost of capital is 10 per cent.
(a) Calculate the payback period, net present value, internal rate of return and accounting rate of return using average investment base of each project.
(b) Show the rankings of the projects by each of the four methods.

| Period | Project A (₹) | Project B (₹) | Project C (₹) |
| :---: | :---: | :---: | :---: |
| 0 | $(5,000)$ | $(5,000)$ | $(5,000)$ |
| 1 | 900 | 700 | 2,000 |
| 2 | 900 | 800 | 2,000 |
| 3 | 900 | 900 | 2,000 |
| 4 | 900 | 1,000 | 1,000 |
| 5 | 900 | 1,100 | - |
| 6 | 900 | 1,200 | - |
| 7 | 900 | 1,300 | - |
| 8 | 900 | 1,400 | - |
| 9 | 900 | 1,500 | - |


| 10 | 900 | 1,600 | - |
| :---: | :---: | :---: | :---: |

## Answer

## (a) Calculation of Payback, NPV, IRR and ARR:

## Payback Period:

| Project A | $=5,000 \div 900$ | $=5.56$ years |
| :--- | :--- | :--- |
| Project B | $=700+800+900+1,000+1,100+500 \div 1,200$ | $=5.42$ years |
| Project C | $=2,000+2,000+1,000 \div 2,000$ | $=$ |
|  | 2.50 years |  |

## NPV:

Project A:
NPV at $10 \%=900 \times 6.145-5,000=530.50$
Project B:
NPV at $10 \%=700 \times 0.909+800 \times 0.826+900 \times 0.751+1,000 \times 0.683+1,100 \times 0.621$ $+1,200 \times 0.564+1,300 \times 0.513+1,400 \times 0.467+1,500 \times 0.424+1,600 \times$
$0.386-5,000=1,590.20$

## Project C:

NPV at $10 \%=2,000 \times 0.909+2,000 \times 0.826+2,000 \times 0.751+1,000 \times 0.683-5,000$ $=655$

## IRR:

Project $\boldsymbol{A}$ (Uniform cash inflow, so we can calculate IRR by PVAF):

$$
\mathrm{PVAF}_{10 \text { years }}=5,000 \div 900 \quad=\quad 5.55
$$

(This factor is found between $12 \%$ and $13 \%$ )
NPV at $12 \%=900 \times 5.650-5,000=\mathbf{8 5 . 0 0}$
NPV at $13 \%=900 \times 5.426-5,000=(116.60)$
IRR $\quad=\quad \mathrm{L}+\frac{\mathrm{NPV}_{\mathrm{L}}}{\mathrm{NPV}_{\mathrm{L}}-\mathrm{NPV}_{\mathrm{H}}} \times(\mathrm{H}-\mathrm{L}) \quad=\quad 12 \%+\frac{85}{85+116.60}(13 \%-12 \%)$
$=12.42 \%$
Project B (Unequal cash inflow, so we can calculate IRR by computing NPV using random rates):
NPV at $10 \%=1,590.20$
NPV at $20 \%=700 \times 0.833+800 \times 0.694+900 \times 0.579+1,000 \times 0.482+1,100 \times 0.402$ $+1,200 \times 0.335+1,300 \times 0.279+1,400 \times 0.233+1,500 \times 0.194+1,600 \times$ $0.162-5,000$
(775.30)
$\operatorname{IRR} \quad=\quad \mathrm{L}+\frac{\mathrm{NPV}_{\mathrm{L}}}{\mathrm{NPV}_{\mathrm{L}}-\mathrm{NPV}_{\mathrm{H}}} \times(\mathrm{H}-\mathrm{L})=10 \%+\frac{1,590.20}{1,590.20+775.30}(20 \%-10 \%)$
$=16.72 \%$
Project C (Unequal cash inflow, so we can calculate IRR by computing NPV using random rates):

$$
\begin{aligned}
\text { NPV at } 15 \% & =2,000 \times 0.870+2,000 \times 0.756+2,000 \times 0.658+1,000 \times 0.572-5,000 \\
& =140 \\
\text { NPV at } 18 \% & =2,000 \times 0.847+2,000 \times 0.718+2,000 \times 0.609+1,000 \times 0.516-5,000 \\
& =(\mathbf{1 3 6}) \\
& =\mathrm{L}+\frac{\mathrm{NPV}_{\mathrm{L}}}{\mathrm{NPV}_{\mathrm{L}}-\mathrm{NPV}_{\mathrm{H}}} \times(\mathrm{H}-\mathrm{L}) \\
& =15 \%+\frac{140}{140+136}(18 \%-15 \%) \\
& =\mathbf{1 6 . 5 2 \%}
\end{aligned}
$$

ARR using average investment base:
ARR $=\frac{\text { Average Pr ofit }}{\text { Average investment }} \times 100$
Project $A=\frac{400}{5,000 \times 1 / 2} \times 100 \quad=16 \%$
Project B $=\frac{650}{5,000 \times 1 / 2} \times 100=26 \%$
Project C $=\frac{500}{5,000 \times 1 / 2} \times 100=20 \%$
Working Note:
Average Profit $=\frac{\text { Total Cash Inflow }- \text { Initial Investment }}{\text { Life }}$
Project $A=\frac{9,000-5,000}{10 \text { Years }} \quad=\quad 400$ per annum
Project $B=\frac{11,500-5,000}{10 \text { Years }} \quad=\quad 650$ per annum
Project $A=\frac{7,000-5,000}{4 \text { Years }} \quad=\quad 500$ per annum
Note: Average book profit is found by deducting initial investment, otherwise student may deduct depreciation year wise.
(b) The projects are ranked as follows according to the various methods:

| Projects | PBP <br> (Years) | ARR <br> (\%) | IRR <br> (\%) | NPV <br> (₹) | PBP | ARR | IRR | $\boldsymbol{N P V}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | 5.56 | 16 | 12.42 | 530.50 | 3 | 3 | 3 | 3 |
| B | 5.42 | 26 | 16.72 | $1,590.20$ | 2 | 1 | 1 | 1 |
| C | 2.50 | 20 | 16.52 | 655 | 1 | 2 | 2 | 2 |

R plc is considering modernizing its production facilities and it has two proposals under consideration. The expected cash flows associated with these projects and their NPV as per discounting rate of $12 \%$ and IRR is as follows:

| Year | Cash Flow |  |
| :---: | :---: | :---: |
|  | Project A (₹) | Project B (₹) |
| 0 | $(40,00,000)$ | $(20,00,000)$ |
| 1 | $8,00,000$ | $7,00,000$ |
| 2 | $14,00,000$ | $13,00,000$ |
| 3 | $13,00,000$ | $12,00,000$ |
| 4 | $12,00,000$ | - |
| 5 | $11,00,000$ | - |
| 6 | $10,00,000$ | - |
| NPV @12\% | $6,49,094$ | $5,15,488$ |
| IRR | $17.47 \%$ | $25.20 \%$ |

## Identify which project should R plc accept?

## Answer

Although from NPV point of view Project A appears to be better but from IRR point of view Project B appears to be better. Since, both projects have unequal lives selection on the basis of these two methods shall not be proper. In such situation we shall use Equivalent Annualized Criterion:

| Year | Project $\boldsymbol{A}$ | Project B |
| :--- | :---: | :---: |
| NPV @ 12\% | $₹ 6,49,094$ | $5,15,488$ |
| $\div$ PVAF @ 12\% | $\div 4.112$ | $\div 2.402$ |
| Equivalent Annualized Criterion | $₹ 1,57,854$ | $₹ 2,14,608$ |

Thus, Project B should be selected.

## PAST YEAR QUESTIONS

## PYQ 1

FH Hospital is considering to purchase a CT- Scan machine. Presently the hospital is outsourcing the CTScan Machine and is earning commission of 15,000 per month (net of tax). The following details are given regarding the machine:

| Cost of CT-Scan machine | $₹ 15,00,000$ |
| :--- | :--- |
| Operating cost per annum (excluding depreciation) | $₹ 2,25,000$ |
| Expected revenue per annum | $₹ 7,90,000$ |
| Salvage value of machine (after 5 years) | $₹ 3,00,000$ |
| Expected life of machine | 5 years |

Assuming tax rate @ $30 \%$, whether it would be profitable for the hospital to purchase the machine?

## Give your recommendation under:

(i) Net Present Value Method, and
(ii) Profitability Index Method.

PV factors at $12 \%$ are given below:

| Year | 1 | 2 | 3 | 4 | 5 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| PV factor | 0.893 | 0.797 | 0.712 | 0.636 | 0.567 |

[(8 Marks) May 2014]

## Answer

## (i) Net Present Value

| Year | Particulars | ₹ | DF @ 12\% | PV |
| :---: | :--- | :---: | :---: | :---: |
| 0 | Cost of CT-Scan machine | $(15,00,000)$ | 1.000 | $(15,00,000)$ |
| $1-5$ | Cash Flow After Tax | $2,87,500$ | 3.605 | $10,36,438$ |
| 5 | Salvage at the end | $3,00,000$ | 0.567 | $1,70,100$ |
| $\mathbf{N P V}$ |  |  |  | $(2,93,462)$ |

Recommendation: CT-Scan machine should not be purchased having negative NPV.

## (ii) Calculation of Profitability Index:

Profitability Index $=\frac{\mathrm{PV} \text { of Inflows }}{\mathrm{PV} \text { of Outflows }}=\frac{12,06,538}{15,00,000}=\mathbf{0 . 8 0 4}$
Recommendation: Since PI is less than 1, CT-Scan machine should not be purchased.

## Working Notes:

Calculation of Incremental CFAT:

| Particulars | $₹$ |
| :--- | :---: |
| Expected revenue per annum | $7,90,000$ |
| Less: Operating cost per annum (excluding depreciation) | $2,25,000)$ |
| Less: Depreciation $(15,00,000-3,00,000) \div 5$ years | $(2,40,000)$ |


|  | PBT |
| :---: | :---: |
| Less: Tax @ 30\% | PAT |
| Less: Loss of commission income per annum $(15,000 \times 12)$ | $3,25,000$ |
| Add: Depreciation | $2,27,500$ |
|  | CFAT |
|  |  |

## PYQ 2

Given below are the data on a capital project ' $M$ ':

| Annual cash inflow | ₹ 60,000 |
| :--- | :--- |
| Useful life | 4 years |
| Salvage value | zero |
| Internal rate of return | $15 \%$ |
| Profitability index | 1.064 |

## Table of discount factor:

| Discount Factor | Years |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ |
| $15 \%$ | 0.870 | 0.756 | 0.658 | 0.572 |
| $14 \%$ | 0.877 | 0.769 | 0.675 | 0.592 |
| $13 \%$ | 0.886 | 0.783 | 0.693 | 0.614 |
| $12 \%$ | 0.893 | 0.797 | 0.712 | 0.636 |

## You are required to calculate:

(i) Cost of the project
(ii) Payback period
(iii) Cost of capital
(iv) Net present value of cash inflow
[(8 Marks) May 2015]

## Answer

(a) Cost of the project:

At IRR,

| Present value of inflows | $=$ | Present value of outflows |
| :--- | :--- | :--- |
| Present value of outflows | $=$ | Annual cost of saving $\times$ Cumulative discount factor |
|  |  | @ IRR for 4 years |
|  | $=$ | $₹ 60,000 \times 2.855$ |
| Cost of project | $=$ | $₹ 1,71, \mathbf{3 0 0}$ |

(b) Payback Period:

Payback period $=\frac{\text { Initial Outflow }}{\text { Equal Annual Cash Inflows }}=\frac{1,71,000}{60,000}$
$=\quad 2.855$ years
(c) Cost of Capital:

Cum DF @ cost of capital for 4 years $=\frac{\text { Present Value of Inflows }}{\text { Annual Inflows }}=\frac{1,82,263.20}{60,000}$ $=\quad 3.038$

From the discount factor table, at discount rate of $12 \%$, the cumulative discount factor for four years is $3.038(0.893+0.797+0.712+0.636)$
Hence, Cost of capital $=12 \%$
(d) Net Present Value of cash inflows:

| PI | $=\frac{\mathrm{PV} \text { of Inflows }}{\mathrm{PV} \text { of Outflows }}$ |  |
| :--- | :--- | :--- | :--- |
| 1.064 | $=$ | $\frac{\mathrm{PV} \text { of Inflows }}{1,71,300}$ |
| PV of Inflows | $=1,71,300 \times 1.064 \quad=$ |  |
| NPV $1,82,263.2$ |  |  |

## PYQ 3

Domestic services (P) Ltd. is in the business of providing cleaning sewerage line services at homes. There is a proposal before the company to purchase a mechanised sewerage cleaning system for a sum of ₹ 20 lakhs. The present system of the company is to use manual labour for the job.

## You are provided with the following information:

## Proposed Machanised System:

Cost of machine
Life of machine
Depreciation (on straight line basis)
Cash Operating cost of machanised system
₹20 lakhs
10 years
10\%
₹5 lakhs per annum

## Present System (manual):

Manual labour
Cost of manual labour

200 persons
$₹ 10,000$ per person per annum

The company has after tax cost of fund at $10 \%$ per annum. The applicable tax rate is $30 \%$.
PV factor for 10 years at 10\% are as given below:

| Years | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PV factor | 0.909 | 0.826 | 0.751 | 0.683 | 0.621 | 0.564 | 0.513 | 0.467 | 0.424 | 0.386 |

You are required to find out whether it is advisable to purchase he machine. Give your recommendation with workings.
[(8 Marks) June 2015]

## Answer

Net Present Value

| Year | Particulars | ₹ | DF @ 10\% | PV |
| :---: | :--- | :---: | :---: | :---: |
| 0 | Cost of Machine | $(20,00,000)$ | 1.000 | $(20,00,000)$ |
| $1-10$ | Incremental CFAT | $11,10,000$ | 6.144 | $68,19,840$ |
| NPV |  |  | $\mathbf{4 8 , 1 9 , 8 4 0}$ |  |

Recommendation: Company should purchase the machine having positive NPV.
Working Notes:
Calculation of Incremental CFAT:

| Particulars | $₹$ |
| :--- | :---: |
| Saving in labour cost (200 persons @ ₹10,000 p.a.) | $20,00,000$ |
| Less: Cash Operating cost of mechanized system p.a. | $(5,00,000)$ |
| Less: Depareciation | PBT |
|  |  |
| Less: Tax @ 30\% | PAT |
|  | $13,00,000)$ |
| Add: Depreciation $(20,00,000 \div 10$ years $)$ | $(3,90,000$ |
| $\boldsymbol{C F A T}$ | $9,10,000$ |

## PYQ 4

Given below are the data on a capital project ' $C$ ':

| Cost of the project | $₹ 2,28,400$ |
| :--- | :--- |
| Useful life | 4 years |
| Salvage value | zero |
| Internal rate of return | $15 \%$ |
| Profitability index | 1.0417 |

## You are required to calculate:

(a) Annual cash flow
(b) Cost of capital
(c) Net present value (NPV)
(d) Discounted Payback period

Table of discount factor:

| Discount Factor | Years |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ |
| $15 \%$ | 0.869 | 0.756 | 0.658 | 0.572 |
| $14 \%$ | 0.877 | 0.769 | 0.675 | 0.592 |
| $13 \%$ | 0.885 | 0.783 | 0.693 | 0.613 |
| $12 \%$ | 0.893 | 0.797 | 0.712 | 0.636 |

[(8 Marks) May 2016]

## Answer

(a) Annual cash flow:

At IRR,

| Present value of inflows | $=$ | Present value of outflows |
| :--- | :--- | :--- |
| Present value of outflows | $=$ | Annual cash inflow $\times$ Cumulative discount factor @ IRR for |
|  |  | 4 years |
| $2,28,400$ | $=$ | Annual cash inflow $\times 2.855$ |
| Annual cash Inflow | $=$ | $\mathbf{8 0 , 0 0 0}$ |

(b) Cost of Capital:

| Present value of inflows | $=$ | Annual cash inflow $\times$ Cumulative discount factor @ Cost of <br> Capital for 4 years |
| :--- | :--- | :--- |
| Cost of project + NPV | $=$ | $80,000 \times$ Cumulative discount factor @ Cost of Capital for 4 |
|  |  | years |
| $2,28,400+9,524$ | $=$ | $80,000 \times$ PVIFA $_{4}$ |
| PVIFA 4 years | $=13 \%$ |  |
| Cost of capital | $=13 \%$ |  |

## Alternatively

| Cum DF @ cost of capital $4_{4 \text { years }}$ | $=$ | $\frac{\text { Present Value of Inflows }}{\text { Annual Inflows }}=\frac{2,37,924}{80,000}$ |
| ---: | :--- | :--- |
|  | $=$ | 2.974 |
| Cost of capital | $=$ | $\mathbf{1 3 \%}$ |

From the discount factor table, at discount rate of $13 \%$, the cumulative discount factor for four years is $2.974(0.885+0.783+0.693+0.613)$

## (c) Net Present Value (NPV):

$\mathrm{NPV}=$ Cost of project $\times(\mathrm{PI}-1)=2,28,400 \times(1.0417-1)=₹ 9,524$

## (d) Discounted Payback Period:

Discounted Payback Period $=$ LLY $+\frac{\text { Initial Outflows - Cumulative PV upto LLY }}{\text { PV of inf lows of ULY }}$
$=3$ years $+\frac{2,28,400-1,88,880}{49,040} \quad=3.806$ years

## Working notes:

## Calculation of PV of cash inflow cumulative PV of cash inflow:

Years
1
2
3
4

$$
\begin{array}{cc}
P V \text { of cash inflow } & \text { Cumulative PV of cash inflow } \\
80,000 \times 0.885=70,800 & 70,800 \\
80,000 \times 0.783=62,640 & 1,33,440 \\
80,000 \times 0.693=55,440 & 1,88,880 \\
80,000 \times 0.613=49,040 & 2,37,920
\end{array}
$$

## PYQ 5

X Limited is considering to purchase of new plant worth ₹ $80,00,000$. The rate of cost of capital is $10 \%$. You are required to calculate:
(a) Pay-back period
(b) Net present value at 10 discount factor
(c) Profitability index at 10 discount factor
(d) Internal rate of return with the help of $10 \%$ and $15 \%$ discount factor.

The expected net cash flows after taxes and before depreciation and present value table are as follows:

| Year | Net Cash Flow <br> ( $₹$ ) | Present value of 1 at <br> $\mathbf{1 0 \%}$ discount rate | Present value of 1 at <br> 15\% discount rate |
| :---: | :---: | :---: | :---: |
| 1 | $14,00,000$ | .909 | .870 |
| 2 | $14,00,000$ | .826 | .756 |
| 3 | $14,00,000$ | .751 | .658 |
| 4 | $14,00,000$ | .683 | .572 |
| 5 | $14,00,000$ | .621 | .497 |
| 6 | $16,00,000$ | .564 | .432 |
| 7 | $20,00,000$ | .513 | .376 |
| 8 | $30,00,000$ | .467 | .327 |
| 9 | $20,00,000$ | .424 | .284 |
| 10 | $8,00,000$ | .386 | .247 |

[(8 Marks) May 2017]

## Answer

(a) Payback period:

| Payback period $=$ | $14,00,000+14,00,000+14,00,000+14,00,000+14,00,000+$ |
| ---: | :--- |
| $10,00,000 / 16,00,000$ | $=$ |
| 5.625 Years |  |

(b) Calculation of NPV

| Years | Cash Inflow | PVIF @ 10\% | Present value |
| :---: | :---: | :---: | :---: |
| 0 | $80,00,000$ | 1.000 | $(80,00,000)$ |
| 1 | $14,00,000$ | .909 | $12,72,600$ |
| 2 | $14,00,000$ | .826 | $11,56,400$ |
| 3 | $14,00,000$ | .751 | $10,51,400$ |
| 4 | $14,00,000$ | .683 | $9,56,200$ |
| 5 | $14,00,000$ | .621 | $8,69,400$ |
| 6 | $16,00,000$ | .564 | $9,02,400$ |
| 7 | $20,00,000$ | .513 | $10,26,000$ |
| 8 | $30,00,000$ | .467 | $14,01,000$ |
| 9 | $20,00,000$ | .424 | $8,48,000$ |
| 10 | $8,00,000$ | .386 | $3,08,800$ |
| NPV |  |  | $\mathbf{1 7 , 9 2 , 2 0 0}$ |

(c) Calculation of PI:

Profitability index = PV of Inflow $\div$ PV of Outflow
$=97,92,200 \div 80,00,000 \quad=\quad 1.224$
(d) Calculation of IRR:

NPV at $10 \% \quad=\quad 17,92,200$
NPV at $15 \%=14,00,000 \times 3.353+16,00,000 \times .432+20,00,000 \times .376+$ $30,00,000 \times .327+20,00,000 \times .284+8,00,000 \times .247-80,00,000$
$=-1,16,000$

IRR
$=\quad \mathrm{L}+\frac{\mathrm{NPV}_{\mathrm{L}}}{\mathrm{NPV}_{\mathrm{L}}-\mathrm{NPV}_{\mathrm{H}}} \times \mathrm{H}-\mathrm{L}=\quad 10 \%+\frac{17,92,200}{17,92,200(1,16,000)} \times 5 \%$
$=14.70 \%$

## PYQ 6

A firm can make investment in either of the following projects. The firm anticipates its cost of capital to be $10 \%$. Pre-tax cash flows of the projects for five years are as follows:

| Year | $\boldsymbol{0}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Project A $(₹)$ | $(2,00,000)$ | 35,000 | 80,000 | 90,000 | 75,000 | 20,000 |
| Project $(₹)$ | $(2,00,000)$ | $2,18,000$ | 10,000 | 10,000 | 4,000 | 3,000 |

Ignore taxation. An amount of ₹ 35,000 will be spent on account of sales promotion in year 3 in case of project A. this has not been taken into account in pre-tax cash inflows.

The discount factors are as under:

| Year | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PVF at $10 \%$ | 1 | 0.91 | 0.83 | 0.75 | 0.68 | 0.62 |

## You are required to calculate for each project:

(a) The payback period
(b) The discounted payback period
(c) Desirability factor
(d) Net present value
[(8 Marks) Nov 2017]

## Answer

(a) Payback period:

Payback period $\mathrm{A}=35,000+80,000+55,000+30,000 / 75,000=$
3.4 Years

Payback period B = 2,00,000/2,18,000 $=0.92$ Years

## Calculation of Present Value of pre-tax cash inflows:

| Years | Cash Inflow A | Cash Inflow B | PVIF @ 10\% | Present value <br> $\boldsymbol{A}$ | Present value <br> $\boldsymbol{B}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 35,000 | $2,18,000$ | .91 | 31,850 | $1,98,380$ |
| 2 | 80,000 | 10,000 | .83 | 66,400 | 8,300 |
| 3 | 55,000 | 10,000 | .75 | 41,250 | 7,500 |
| 4 | 75,000 | 4,000 | .68 | 51,000 | 2,720 |
| 5 | 20,000 | 3,000 | .62 | 12,400 | 1,860 |
| Total |  |  |  | $2,02,900$ | $2,18,760$ |

## (b) Discounted payback period:

| Discounted payback A | $=$ | $31,850+66,400+41,250+51,000+9,500 / 12,400$ |
| ---: | :--- | :--- |
|  | $=$ | 4.77 Years |
| Discounted payback B | $=1,98,380+1,620 / 8,300$ | $=$ |
| 1.2 Years |  |  |

## (c) Desirability factor:

Desirability factor
Project A
Project B $=2,18,760 \div 2,00,000=1.0938$
(d) NPV:

| NPV | $=$ | PV of Inflow - PV of Outflow |  |
| :--- | :--- | :--- | :--- |
| Project A | $=2,02,900-2,00,000$ | $=\quad 2,900$ |  |
| Project B | $=2,18,760-2,00,000$ | $=18,760$ |  |

## PYQ 7

A proposal to invest in a project, which has a useful life of 5 years and no salvage value at the end of useful life, is under consideration of a firm. It is anticipated that the project will generate a steady cash inflow of ₹ 70,000 per annum. After analyzing other facts of the project, the following information were revealed:
Internal rate of return
13\%
Profitability index
1.07762

Table of discount factor:

| Discount <br> Factor | Years |  |  |  |  | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |  |
| $10 \%$ | 0.909 | 0.826 | 0.751 | 0.683 | 0.621 | 3.790 |
| $11 \%$ | 0.901 | 0.812 | 0.731 | 0.659 | 0.593 | 3.696 |
| $12 \%$ | 0.893 | 0.797 | 0.712 | 0.636 | 0.567 | 3.605 |
| $13 \%$ | 0.885 | 0.783 | 0.693 | 0.613 | 0.543 | 3.517 |

## You are required to calculate:

(1) Cost of the project
(2) Payback period
(3) Net present value
(4) Cost of capital
[(8 Marks) May 2018]

## Answer

(1) Cost of the project: At IRR,

| Present value of inflows | $=$ | Present value of outflows |
| :--- | :--- | :--- |
| Present value of outflows | $=$ | Annual cash inflows $\times$ Cumulative discount factor |
|  |  | $@$ IRR for 5 years |
|  | $=$ | $₹ 70,000 \times 3.517$ |
| Cost of the project | $=$ | $₹ 2,46,190$ |

(2) Payback Period:

Payback period
$=\frac{\text { Initial Outflow }}{\text { Annual Cash Inflow }}=\frac{2,46,190}{70,000}$
$=3.517$ years
(3) Net Present Value:

| PI | $=$ | $\frac{P V \text { of Inflows }}{\text { PV of Outflows }}$ | $=$ | $\frac{\mathrm{PV} \text { of Inflow }}{2,46,190}$ |
| :--- | :--- | :--- | :--- | :--- |
| PV of Inflows | $=$ | $2,46,190 \times 1.07762$ |  |  |
| $\boldsymbol{N P V} 2,65,299$ |  |  |  |  |
|  |  |  | PV of inflows - PV of outflows |  |

$$
=₹ 2,65,299-₹ 2,46,190 \quad=\quad ₹ 19,109
$$

## (4) Cost of Capital:

$\begin{aligned} \text { Cum DF @ cost of capital for 5years } & = \\ & =\frac{\text { Present Value of Inflows }}{\text { Annual Inflows }}=\frac{2,65,299}{70,000} \\ \text { Cost of capital } & =3.790 \\ & \mathbf{1 0 \%} \text { (Given in table) }\end{aligned}$

## PYQ 8

PD Ltd. an existing company is planning to introduce a new product with projected life of 8 years. Project cost will be $₹ 2,40,00,000$. At the end of 8 years no residual value will be realized. Working capital of ₹ $30,00,000$ will be needed. The $100 \%$ capacity of the project is $2,00,000$ units p.a. but the production and sales volume are expected as under:

| Year | Units |
| :---: | ---: |
| 1 | 60,000 |
| 2 | 80,000 |
| $3-5$ | $1,40,000$ |
| $6-8$ | $1,20,000$ |

## Other information:

1. Selling price per unit ₹200.
2. Variable cost is $40 \%$ of sales.
3. Fixed cost p.a. ₹ $30,00,000$.
4. In addition to these advertisement expenditure will have to be incurred as under:

| Year | (₹in lacs) |
| :---: | :---: |
| 1 | 50 |
| 2 | 25 |
| $3-5$ | 10 |
| $6-8$ | 5 |

5. Income tax is $25 \%$.
6. Straight line method of depreciation is permissible for tax purpose.
7. Cost of capital is $10 \%$.
8. Assume that loss cannot be carried forward.

## Present value table

| Year | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\mathbf{8}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PVF@10\% | 0.909 | 0.826 | 0.751 | 0.683 | 0.621 | 0.564 | 0.513 | 0.467 |

Advise about the project acceptability.
[(10 Marks) Nov 2018]

## Answer

Net Present Value

| Year | Particulars | ₹ | DF @ 10\% | PV |
| :---: | :--- | :---: | :---: | :---: |
| 0 | Initial outflows $(2,40,00,000+30,00,000)$ | $(2,70,00,000)$ | 1.000 | $(2,70,00,000)$ |
| 1 | CFAT | $(8,00,000)$ | 0.909 | $(7,27,200)$ |
| 2 | CFAT | $38,25,000$ | 0.826 | $31,59,450$ |
| $3-5$ | CFAT | $1,03,50,000$ | 2.055 | $2,12,69,250$ |
| $6-8$ | CFAT | $89,25,000$ | 1.544 | $1,37,80,200$ |


| 8 | Working Capital | $30,00,000$ | 0.467 | $14,01,000$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{N P V}$ |  |  |  | $\mathbf{1 , 1 8 , 8 2 , 7 0 0}$ |

Company should accept the proposal having positive NPV of the project. Working Notes:

1. Depreciation: $=\frac{\text { Original Cost less Salvage }}{\text { Life of Equipment }}=\frac{2,40,00,000}{8 \text { Years }}=\mathbf{3 0 , 0 0 , 0 0 0}$

## 2. Statement showing CFAT:

| Particulars | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3 - 5}$ | $\mathbf{6 - 8}$ |
| :--- | :---: | :---: | :---: | :---: |
| Units sold | 60,000 | 80,000 | $1,40,000$ | $1,20,000$ |
| Sales @ ₹200 p.u. | $1,20,00,000$ | $1,60,00,000$ | $2,80,00,000$ | $2,40,00,000$ |
| Less: VC @ 40\% | $48,00,000$ | $64,00,000$ | $1,12,00,000$ | $96,00,000$ |
| Contribution | $72,00,000$ | $96,00,000$ | $1,68,00,000$ | $1,44,00,000$ |
| Less: Advertisement expenses | $(50,00,000)$ | $(25,00,000)$ | $10,00,000)$ | $(5,00,000)$ |
| Less: Cash fixed cost | $(30,00,000)$ | $(30,00,000)$ | $30,00,000)$ | $(30,00,000)$ |
| Less: Depreciation | $(30,00,000)$ | $(30,00,000)$ | $(30,00,000)$ | $(30,00,000)$ |
| PBT | $(38,00,000)$ | $11,00,000$ | $98,00,000$ | $79,00,000$ |
| Less: Tax @ 25\% | - | $(2,75,000)$ | $(24,50,000)$ | $(19,75,000)$ |
| PAT | $(38,00,000)$ | $8,25,000$ | $73,50,000$ | $59,25,000$ |
| Add: Depreciation | $\mathbf{3 0 , 0 0 , 0 0 0}$ | $30,00,000$ | $30,00,000$ | $30,00,000$ |
|  | $\boldsymbol{C F A T}$ | $\mathbf{8 , 0 0 , 0 0 0}$ | $\mathbf{3 8 , 2 5 , 0 0 0}$ | $\mathbf{1 , 0 3 , 5 0 , 0 0 0}$ |
| $\mathbf{8 9 , 2 5 , 0 0 0}$ |  |  |  |  |

## PYQ 9

AT Limited is considering three projects A, B and C. the cash flows associated with the projects are given below:

| Projects | $\boldsymbol{C}_{\boldsymbol{o}}$ | $\boldsymbol{C}_{\boldsymbol{1}}$ | $\boldsymbol{C}_{\boldsymbol{2}}$ | $\boldsymbol{C}_{\boldsymbol{3}}$ | $\boldsymbol{C}_{\boldsymbol{4}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{A}$ | $(10,000)$ | 2,000 | 2,000 | 6,000 | 0 |
| $\boldsymbol{B}$ | $(2,000)$ | 0 | 2,000 | 4,000 | 6,000 |
| $\boldsymbol{C}$ | $(10,000)$ | 2,000 | 2,000 | 6,000 | 10,000 |

## You are required to:

(a) Calculate the payback period of each of the three projects.
(b) If the cut-off period is two years, then which projects should be accepted?
(c) Projects with positive NPV's if the opportunity cost of capital is 10 percent.
(d) "Payback gives too much weight to cash flows that occur after the cut-off date". True or false?
(e) "If a firm used a single cut-off period for all projects, it is likely to accept too many short lived projects." True or false?

## Present value table

| Year | $\boldsymbol{0}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PVF@10\% | 1.000 | 0.909 | 0.826 | 0.751 | 0.683 | 0.621 |

[(10 Marks) May 2019]

## Answer

## (a) Calculation of Cumulative Cash Flows:

| Years | Project A |  | Project B |  | Projects C |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Cash Flow | Cum. CF | Cash Flow | Cum. CF | Cash Flow | Cum. CF |
| 1 | 2,000 | 2,000 | 0 | 0 | 2,000 | 2,000 |


| 2 | 2,000 | 4,000 | 2,000 | 2,000 | 2,000 | 4,000 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | 6,000 | 10,000 | 4,000 | 6,000 | 6,000 | 10,000 |
| 4 | - | - | 6,000 | 12,000 | 10,000 | 20,000 |

## Payback Period:

| Project A | $=3$ Years |  |
| :--- | :--- | :--- |
| Project B | $=$ | 2 Years |
| Project C | $=3$ Years |  |

(b) If cut-off period is two years then company should accept projects B.
(c) NPV:

NPV = Present value of Inflow - Present value of outflow
Project A $=\quad 2,000 \times 0.909+2,000 \times 0.826+6,000 \times 0.751-10,000=(2,024)$
Project $B=0 \times 0.909+2,000 \times 0.826+4,000 \times 0.751+6,000 \times 0.683-2,000$
$=6,754$
Project C $=2,000 \times 0.909+2,000 \times 0.826+6,000 \times 0.751+10,000 \times 0.683-10,000$
$=4,806$
Project B and C have positive NPV.
(d) False: Payback only considers cash flows from the initiation of the project till it's payback period is being reached, and ignores cash flows after the payback period.
(e) True: When a firm use a single cut-off period for all projects, it is likely to accept too many short lived projects having payback period within such cut-off date. Long term projects take time to reach at payback, in case of single cut-off date these long term projects are ignored. Thus, payback is biased towards short-term projects.

## PYQ 10

A company has ₹ $1,00,000$ available for investment and has identified the following four investment in which to invest:

| Project Name | Initial Investment | NPV |
| :---: | :---: | :---: |
| C | $₹ 40,000$ | $₹ 20,000$ |
| D | $₹ 1,00,000$ | $₹ 35,000$ |
| E | $₹ 50,000$ | $₹ 24,000$ |
| F | $₹ 60,000$ | $₹ 18,000$ |

You are required to optimise the returns from a package of projects within the capital spending limit if:
(a) The projects are independent of each other and are divisible.
(b) The projects are not divisible.
[(5 Marks) Nov 2019]

## Answer

(a) Statement of Rank and Selection of Projects (Divisible Situation)

| Projects | PI (1+ NPV/Investment) | Rank | Project Cost | Project (\%) | Investment |
| :---: | :---: | :---: | :---: | :---: | :---: |
| C | $1+20,000 / 40,000=1.50$ | 1 | $₹ 40,000$ | $100 \%$ | $₹ 40,000$ |
| D | $1+35,000 / 1,00,000=1.35$ | 3 | $₹ 1,00,000$ | $10 \%$ | $₹ 10,000$ |


| E | $1+24,000 / 50,000=1.48$ | 2 | $₹ 50,000$ | $100 \%$ | $₹ 50,000$ |
| :---: | :---: | :--- | :---: | :---: | :---: | :---: |
| F | $1+18,000 / 60,000=1.30$ | 4 | $₹ 60,000$ | - | - |
| Total Investment |  |  |  |  |  |

Optimum investment: 100\% of C, E and 1/10 of D.
(b) Statement of Possible Combinations and Combined NPV (Indivisible Situation)

| Possible Combinations | Combined Investment | Combined NPV |
| :---: | :---: | :---: |
| C + E | $₹ 90,000$ | $₹ 44,000$ |
| C F | $₹ 1,00,000$ | $₹ 38,000$ |
| D | $₹ 1,00,000$ | $₹ 35,000$ |

Invest in combination of $C$ and $E$ having highest combined NPV and invest remaining $\mathfrak{₹} 10,000$ elsewhere.

## PYQ 11

CK Ltd. is planning to buy a new machine. Details of which are as follows:

| Cost of the machine at the commencement | $₹ 2,50,000$ |
| :--- | :--- |
| Economic life of the machine | 8 years |
| Residual value | Nil |
| Annual production capacity of the machine | $1,00,000$ units |
| Estimated selling price per unit | $₹ 6$ |
| Estimated variable cost per unit | $₹ 3$ |
| Estimated annual fixed cost | $₹ 1,00,000$ |
| (Excluding depreciation) |  |
| Advertisement expenses in $1^{\text {st }}$ year in addition of fixed cost | $₹ 20,000$ |
| Maintenance expenses in $5^{\text {th }}$ year in addition of fixed cost | $₹ 30,000$ |
| Cost of capital | $12 \%$ |
| Ignore tax. |  |

Analyse the above mentioned proposal using the Net Present Value method and advice.
The PV factors at 12\% are:

| Year | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | 7 | 8 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :--- |
| PV Factor | .893 | .797 | .712 | .636 | .567 | .507 | .452 | .404 |
|  |  |  |  |  |  |  |  |  |
| [(5 Marks) Nov 2020] |  |  |  |  |  |  |  |  |

## Answer

Statement of NPV

| Year | Particulars | ₹ | DF @ 12\% | PV |
| :---: | :--- | :---: | :---: | :---: |
| 0 | Initial outflows | $(2,50,000)$ | 1.000 | $(2,50,000)$ |
| 1 | Cash inflow | $1,80,000$ | 0.893 | $1,60,740$ |
| $2-4$ | Cash inflow | $2,00,000$ | 2.145 | $4,29,000$ |
| 5 | Cash inflow | $1,70,000$ | 0.567 | 96,390 |
| $6-8$ | Cash inflow | $2,00,000$ | 1.363 | $2,72,600$ |
|  |  |  |  |  |

## Working Note:

(a) Calculation of Annual Cash Inflow

| Particulars | 1 | $2-4$ | 5 | $6-8$ |
| :--- | :--- | :--- | :--- | :--- |


| Sales value @ ₹6 per unit of 1,00,000 units | $6,00,000$ | $6,00,000$ | $6,00,000$ | $6,00,000$ |
| :--- | :---: | :---: | :---: | :---: |
| Less: Variable costs @ ₹3 per unit | $3,00,000$ | $3,00,000$ | $3,00,000$ | $3,00,000$ |
| Less: Annual cash fixed cost |  |  |  |  |
| Less: Advertisement expenses | $1,00,000$ | $1,00,000$ | $1,00,000$ | $1,00,000$ |
| Less: Maintenance expenses | 20,000 | - | - | - |
| Cash Inflow | - | - | 30,000 | - |
|  | $\mathbf{1 , 8 0 , 0 0 0}$ | $\mathbf{2 , 0 0 , 0 0 0}$ | $\mathbf{1 , 7 0 , 0 0 0}$ | $\mathbf{2 , 0 0 , 0 0 0}$ |

Advise: CK limited should buy machine having positive NPV.

## PYQ 12

A company wants to buy a machine, and two different models namely A and B are available. Following further particulars are available:

| Particulars | Machine $\boldsymbol{A}$ | Machine $\boldsymbol{B}$ |
| :--- | :---: | :---: |
| Original Cost $(₹)$ | $8,00,000$ | $6,00,000$ |
| Estimated life in years | 4 | 4 |
| Salvage value $(₹)$ | 0 | 0 |

The company provides depreciation under straight line method. Income tax rate applicable is $30 \%$. The present value of ₹ 1 at $12 \%$ discounting factor and net profit before depreciation and tax are as under:

| Year | Net Profit before Depreciation and Tax |  | PV Factor |
| :---: | :---: | :---: | :---: |
|  | Machine $\boldsymbol{A}$ | Machine $\boldsymbol{B}$ |  |
| 1 | $2,30,000$ | $1,75,000$ | 0.893 |
| 2 | $2,40,000$ | $2,60,000$ | 0.797 |
| 3 | $2,20,000$ | $3,20,000$ | 0.712 |
| 4 | $5,60,000$ | $1,50,000$ | 0.636 |

## Calculate:

(1) NPV (Net Present Value)
(2) Discounted Pay- back Period
(3) PI (Profitability Index)
[(10 Marks) Jan 2021]

## Answer

(1) $\quad$ NPV $\quad$ PV of Inflows - PV of Outflows

| Machine A | $=$ | $=18,909-8,00,000$ | $\mathbf{1 8 , 9 0 9}$ |
| :--- | :--- | :--- | :--- |
| Machine B | $=$ | $=17,4,425-6,00,000$ | 17,425 |

(2) Discounted pay-back Period

| Machine A | $=3$ years $+(8,00,000-5,31,437) / 2,87,472=3.93$ years |
| :--- | :--- |
| Machine B | $=3$ years $+(6,00,000-5,22,025) / 95,400=3.82$ years |

(3) PI $=\quad \mathrm{PV}$ of Inflows $\div \mathrm{PV}$ of Outflows

| Machine A | $=$ | $=$ | 1.023 |
| :--- | :--- | :--- | :--- |
| Machine B | $=$ | $=$ | $18,909 \div 8,00,000$ |

Suggestion: As per NPV method Machine A is more beneficial and as per Discounted pay-back period method and PI method Machine B is more beneficial.

## Working Notes:

1. Statement showing Present Value of CFAT and cumulative PV of CFAT of Machine A:

| Particulars | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ |
| :--- | :---: | :---: | :---: | :---: |
| Net Profit before Depreciation and Tax | $2,30,000$ | $2,40,000$ | $2,20,000$ | $5,60,000$ |
| Less: Depreciation (8,00,000 $\div 4$ years) | $(2,00,000)$ | $(2,00,000)$ | $(2,00,000)$ | $(2,00,000)$ |
| PBT | 30,000 | 40,000 | 20,000 | $3,60,000$ |
| Less: Tax @ 30\% | $(9,000)$ | $(12,000)$ | $(6,000)$ | $(1,08,000)$ |
| PAT | 21,000 | 28,000 | 14,000 | $2,52,000$ |
| Add: Depreciation | $2,00,000$ | $2,00,000$ | $2,00,000$ | $2,00,000$ |
| CFAT | $2,21,000$ | $2,28,000$ | $2,14,000$ | $4,52,000$ |
| $\times$ PV Factor | 0,893 | 0.797 | 0.712 | 0.636 |
| Present Value of CFAT | $\mathbf{1 , 9 7 , 3 5 3}$ | $\mathbf{1 , 8 1 , 7 1 6}$ | $\mathbf{1 , 5 2 , 3 6 8}$ | $2,87,472$ |
| Cumulative PV of CFAT | $\mathbf{1 , 9 7 , 3 5 3}$ | $\mathbf{3 , 7 9 , 0 6 9}$ | $\mathbf{5 , 3 1 , 4 3 7}$ | $\mathbf{8 , 1 8 , 9 0 9}$ |

2. Statement showing Present Value of CFAT and cumulative PV of CFAT of Machine B:

| Particulars | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ |
| :--- | :---: | :---: | :---: | :---: |
| Net Profit before Depreciation and Tax | $1,75,000$ | $2,60,000$ | $3,20,000$ | $1,50,000$ |
| Less: Depreciation $(6,00,000 \div 4$ years $)$ | $(1,50,000)$ | $(1,50,000)$ | $(1,50,000)$ | $(1,50,000)$ |
| PBT | 25,000 | $1,10,000$ | $1,70,000$ | - |
| Less: Tax @ 30\% | $(7,500)$ | $(33,000)$ | $(51,000)$ | - |
| PAT | 17,500 | 77,000 | $1,19,000$ | - |
| Add: Depreciation | $1,50,000$ | $1,50,000$ | $1,50,000$ | $1,50,000$ |
| CFAT | $1,67,500$ | $2,27,000$ | $2,69,000$ | $1,50,000$ |
| $\times$ PV Factor | 0,893 | 0.797 | 0.712 | 0.636 |
| Present Value of CFAT | $1,49,578$ | $\mathbf{1 , 8 0 , 9 1 9}$ | $\mathbf{1 , 9 1 , 5 2 8}$ | 95,400 |
| Cumulative PV of CFAT | $\mathbf{1 , 4 9 , 5 7 8}$ | $\mathbf{3 , 3 0 , 4 9 7}$ | $\mathbf{5 , 2 2 , 0 2 5}$ | $\mathbf{6 , 1 7 , 4 2 5}$ |

## PYQ 13

An existing company has a machine in operation for two years, its estimated life is 4 years with no residual value in the end. Its current market value is $₹ 3$ lakhs. The management is considering a proposal to purchase an improved model of a machine which gives increase output. The details are as under:

| Particulars | Existing Machine | New Machine |
| :--- | :---: | :---: |
| Purchase price | $₹ 6,00,000$ | $₹ 10,00,000$ |
| Estimated life | 6 years | 4 years |
| Residual value | 0 | 0 |
| Annual operating days | 300 | 300 |
| Operating hour per day | 6 | 6 |
| Selling price per unit | $₹ 10$ | $₹ 10$ |
| Material cost per unit | $₹ 2$ | $₹ 2$ |
| Output per hour in units | 20 | 40 |
| Labour cost per hour | $₹ 20$ | $₹ 30$ |
| Fixed overhead per annum excluding depreciation | $₹ 1,00,000$ | $₹ 60,000$ |
| Working capital | $₹ 1,00,000$ | $₹ 2,00,000$ |
| Income tax rate | $30 \%$ | $30 \%$ |

Assuming that cost of capital is $10 \%$ and the company uses written down value of depreciation @ 20\% and it has several machines in $20 \%$ block.

Advice the management on the replacement of machine as per NPV method.
The discounting factor table given below:

| Discounting Factors | Year 1 | Year 2 | Year 3 | Year 4 |
| :--- | :--- | :--- | :--- | :--- |
| $10 \%$ | 0.909 | 0.826 | 0.751 | 0.683 |

[(10 Marks) July 2021]

## Answer

Statement of NPV

| Year | Particulars | ₹ | DF @ 10\% | PV |
| :---: | :--- | :---: | :---: | :---: |
| 0 | Initial outflows | $(8,00,000)$ | 1.000 | $(8,00,000)$ |
| 1 | Incremental CFAT | $2,59,000$ | 0.909 | $2,35,431$ |
| 2 | Incremental CFAT | $2,50,600$ | 0.826 | $2,06,996$ |
| 3 | Incremental CFAT | $2,43,880$ | 0.751 | $1,83,154$ |
| 4 | Incremental CFAT + Working Capital | $3,38,504$ | 0.683 | $2,31,198$ |
|  | $(2,38,504+1,00,000)$ |  |  |  |
| $\mathbf{N P V}$ |  |  |  | $\mathbf{5 6 , 7 7 9}$ |

Advise: The company should go ahead with replacement of machine, since it has positive NPV.

## Working Notes:

1. Calculation of initial outflow:

Cost of new machine
Less: Sales value of old machine
Add: Increase in Working Capital
Initial outflow
₹ $10,00,000$
(₹3,00,000)
₹1,00,000
₹ $8,00,000$
2. Total operating hours $=300$ days $\times 6$ hours $=1,800$ hours
3. Increase in output $=1,800$ hours $\times(40-20)=36,000$ units
4. Base for incremental Depreciation:

| Particulars | F |
| :---: | :---: |
| (A) WDV of Existing Machine: |  |
| Purchase price of existing machine | 6,00,000 |
| Less: Depreciation year $1 \quad(6,00,000 \times 20 \%)$ | $(1,20,000)$ |
| Less: Depreciation year $2 \quad(4,80,000 \times 20 \%)$ | $(96,000)$ |
| WDV of Existing Machine (A) | 3,84,000 |
| (B) Depreciation Base of New Machine: |  |
| Purchase price of new machine | 10,00,000 |
| Add: WDV of existing Machine | 3,84,000 |
| Less: Sale value of existing machine | $(3,00,000)$ |
| Depreciation Base of New Machine (B) | 10,84,000 |
| (C) Base for incremental Depreciation (B-A) | 7,00,000 |

## 5. Calculation of incremental CFAT:

| Particulars | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: |
| Increase in Sales ( 36,000 units $\times$ ₹ 10 ) | 3,60,000 | 3,60,000 | 3,60,000 | 3,60,000 |
| + Decrease in Cash Fixed cost (1,00,000-60,000) |  |  |  |  |
| - Increase in Material cost (36,000 units $\times$ ₹ 2 ) | 40,000 | 40,000 | 40,000 | 40,000 |
| - Increase in Labour cost $\{1,800$ hours $\times(30-20)\}$ | $(72,000)$ | $(72,000)$ | $(72,000)$ | $(72,000)$ |
| Less: Increase in Depreciation (Base: 7,00,000) | $(18,000)$ | $(18,000)$ | $(18,000)$ | $(18,000)$ |
| Incremental PBT | (1,40,000) | (1,12,000) | $(89,600)$ | $(71,680)$ |
| Less: Tax @ 30\% | 1,70,000 | 1,98,000 | 2,20,400 | 2,38,320 |
| Incremental PAT | $(51,000)$ | $(59,400)$ | $(66,120)$ | $(71,496)$ |
| Add: Incremental Depreciation | 1,19,000 | 1,38,600 | 1,54,280 | 1,66,824 |
| Incremental CFAT | 1,40,000 | 1,12,000 | 89,600 | 71,680 |
|  | 2,59,000 | 2,50,600 | 2,43,880 | 2,38,504 |

Notes: Since company has several machines in 20\% block of assets, there is no tax benefit on loss on sale of machine because block will remain in existance.

## PYQ 14

Stand Ltd is contemplating replacement of one of it's machine which has become outdated and inefficient. It's financial manager has prepared a report outlining two possible replacement machines. The details of each machine are as follows:
Initial investment
Estimated useful life
Residual value
Contribution per annum
Fixed maintenance costs per annum
Other fixed operating costs per annum

| Machine 1 | Machine 2 |
| :--- | :--- |
| ₹ $12,00,000$ | ₹ $16,00,000$ |
| 3 Years | 5 Years |
| ₹ $1,20,000$ | ₹ $1,00,000$ |
| ₹ $11,60,000$ | ₹ $12,00,000$ |
| ₹ 40,000 | ₹ 80,000 |
| ₹ $7,20,000$ | ₹ $6,10,000$ |

The maintenance costs are payable annually in advance. All other cash flows apart from the initial investment assumed to occur at the end of each year. Depreciation has been calculated by straight line method and has been included in other fixed operating costs. The expected cost of capital for this project is assumed as $12 \%$ p.a.

Which machine is more beneficial, using Annualized Equivalent Approach? Ignore tax.

| Year | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PVIF $_{0.12, \mathrm{t}}$ | 0.893 | 0.797 | 0.712 | 0.636 | 0.567 | 0.507 |
| PVIFA $_{0.12, \mathrm{t}}$ | 0.893 | 1.690 | 2.402 | 3.038 | 3.605 | 4.112 |

## Answer

## (i) Statement Showing Evaluation of Two Machines

| Particulars | Machine 1 | Machine 2 |
| :--- | :---: | :---: |
| (A) Initial investment | $12,00,000$ | $16,00,000$ |
| (B) PV of Contribution | $27,86,320$ | $43,26,000$ |
|  | $(11,60,000 \times 2.402)$ | $(12,00,000 \times 3.605)$ |
| (C) PV of Cash fixed operating costs | $8,64,720$ | $11,17,550$ |
|  | $(3,60,000 \times 2.402)$ | $(3,10,000 \times 3.605)$ |
| (D) PV of Fixed maintenance costs | $1,07,600$ | $3,23,040$ |
|  | $\{40,000 \times(1.690+1)\}$ | $\{80,000 \times(3.038+1)\}$ |
| (E) PV of residual value | 85,440 | 56,700 |


| Net present value $(\boldsymbol{B}+\boldsymbol{E}-\boldsymbol{A}-\boldsymbol{C}-\boldsymbol{D})$ | $(1,20,000 \times 0.712)$ | $(1,00,000 \times 0.567)$ |
| :---: | :---: | :---: |
|  | $6,99,440$ | $13,42,110$ |
|  | $\div 2.402$ | $\div 3.605$ |
|  | $\mathbf{2 , 9 1 , 1 9 1}$ | $\mathbf{3 , 7 2 , 2 9 1}$ |

## Select the Machine 2 having higher annualized equivalent NPV

## Working Notes:

1. Depreciation: $=$ (Initial investment - Residual value) $\div$ Useful life

Machine $1=(₹ 12,00,000-₹ 1,20,000) \div 3$ years $=₹ 3,60,000$
Machine $2=(₹ 16,00,000-₹ 1,00,000) \div 5$ years $=$ ₹ $3,00,000$
2. Cash fixed operating costs $=$ Fixed operating costs - Depreciation

Machine $1=$ ₹7,20,000 - ₹3,60,000) $=$ ₹3,60,000
Machine $2=\quad=\quad=10,000-₹ 3,00,000 \quad$ F3,10,000

## PYQ 15

Alpha Limited is a manufacturer of computers. It wants to introduce artificial intelligence while making computers. The estimated annual saving from introduction of the artificial intelligence (AI) is as follows:

- Reduction of five employees with annual salaries of ₹ $3,00,000$ each
- Reduction of ₹3,00,000 in production delays caused by inventory problem.
- Reduction in lost sales ₹2,50,000 and
- Gain due to timely billing ₹2,00,000

The purchase price of the system for installation of artificial intelligence is $₹ 20,00,000$ and installation cost is $₹ 1,00,000$. $80 \%$ of the purchase price will be paid in the year of purchase and remaining will be paid in next year.

The estimated life of the system is 5 years and it will be depreciated on a straight-line basis. However, the operation of the new system requires two computer specialists with annual salaries of ₹5,00,000 per person.

In addition to above, annual maintenance and operating cost for five years are as below:
(Amount in ₹)

| Year | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Maintenance \& Operating Cost | $2,00,000$ | $1,80,000$ | $1,60,000$ | $1,40,000$ | $1,20,000$ |

Maintenance and operating cost are payable in advance. The company's tax rate is $30 \%$ and its required rate of return is $15 \%$.

| Year | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| PVIF $_{0.10, \mathrm{t}}$ | 0.909 | 0.826 | 0.751 | 0.683 | 0.621 |
| PVIF $_{0.12, \mathrm{t}}$ | 0.893 | 0.797 | 0.712 | 0.636 | 0.567 |
| PVIF $_{0.15, \mathrm{t}}$ | 0.870 | 0.756 | 0.658 | 0.572 | 0.497 |

Evaluate the project by using Net Present Value and Profitability Index.

## Answer

(1) Net Present value (NPV)

| Year | Particulars | ₹ | PVIF @ 15\% | PV |
| :---: | :---: | :---: | :---: | :---: |
| 0 | Initial Outflows: |  |  |  |
|  | 80\% of Purchase price $(20,00,000 \times 80 \%)$ | $(16,00,000)$ | 1.000 | $(16,00,000)$ |
|  | Installation cost | $(1,00,000)$ | 1.000 | $(1,00,000)$ |
| 1 | 20\% of Purchase Cost | $(4,00,000)$ | 0.870 | $(3,48,000)$ |
| PV of Outflows |  |  |  |  |
| 0 | Maintenance \& Operating cost for year 1 | $(2,00,000)$ | 1.000 | $(2,00,000)$ |
| 1 | CFAT | $8,81,000$ | 0.870 | $7,66,470$ |
| 2 | CFAT | $8,95,000$ | 0.756 | $6,76,620$ |
| 3 | CFAT | $9,09,000$ | 0.658 | $5,98,122$ |
| 4 | CFAT | $9,23,000$ | 0.572 | $5,27,956$ |
| 5 | CFAT | $10,37,000$ | 0.497 | $5,15,389$ |
| PV of Inflows |  |  |  |  |
| NPV |  |  |  |  |

Advice: Accept the proposal having positive NPV.

(2) Profitability Index |  | $=$ | PV of Inflows $\div \mathrm{PV}$ of Outflows |
| ---: | :--- | :--- | :--- | :--- |
|  | $=$ | $28,84,557 \div 20,48,000$ |

Advice: Accept the proposal having PI higher than 1.

## Working Note:

## Statement of CFAT

| Particulars | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Saving in employees salaries $(₹ 3,00,000 \times 5)$ | 15,00,000 | 15,00,000 | 15,00,000 | 15,00,000 | 15,00,000 |
| + Reduction in prod. delays | 3,00,000 | 3,00,000 | 3,00,000 | 3,00,000 | 3,00,000 |
| + Reduction in lost sales | 2,50,000 | 2,50,000 | 2,50,000 | 2,50,000 | 2,50,000 |
| + Gain due to timely billing | 2,00,000 | 2,00,000 | 2,00,000 | 2,00,000 | 2,00,000 |
| - Salaries computer specialist $(₹ 5,00,000 \times 2)$ | (10,00,000) | $(10,00,000)$ | $(10,00,000)$ | (10,00,000) | $(10,00,000)$ |
| - Maintenance \& Op. cost | $(2,00,000)$ | $(1,80,000)$ | $(1,60,000)$ | $(1,40,000)$ | $(1,20,000)$ |
| - Depreciation <br> (21,00,000 $\div 5$ years) | $(4,20,000)$ | $(4,20,000)$ | $(4,20,000)$ | $(4,20,000)$ | $(4,20,000)$ |
| PBT | 6,30,000 | 6,50,000 | 6,70,000 | 6,90,000 | 7,10,000 |
| - Tax @ 30\% | $(1,89,000)$ | $(1,95,000)$ | $(2,01,000)$ | $(2,07,000)$ | $(2,13,000)$ |
| PAT | 4,41,000 | 4,55,000 | 4,69,000 | 4,83,000 | 4,97,000 |
| + Depreciation | 4,20,000 | 4,20,000 | 4,20,000 | 4,20,000 | 4,20,000 |
| + Maint. \& Op. cost (accrual) | 2,00,000 | 1,80,000 | 1,60,000 | 1,40,000 | 1,20,000 |
| - Maint. \& Op. cost (Cash) | $(1,80,000)$ | (1,60,000) | $(1,40,000)$ | $(1,20,000)$ | - |
| CFAT | 8,81,000 | 8,95,000 | 9,09,000 | 9,23,000 | 10,37,000 |

## PYQ 16

A firm is in need of a small vehicle to make deliveries. It is intending to choose between two options. One option is to buy a new three wheeler that would cost ₹ $1,50,000$ and will remain in service for 10 years.

The other alternative is to buy a second hand vehicle for ₹ 80,000 that could remain in service for 5 years. Thereafter the firm, can buy another second hand vehicle for ₹ 60,000 that will last for another 5 years.

The scrap value of the discarded vehicle will be equal to it written down value (WDV). The firm pays $30 \%$ tax and is allowed to claim depreciation on vehicles @ $25 \%$ on WDV basis. The cost of capital of the firm is $12 \%$.

You are required to advise the best option.

## Given:

| $\boldsymbol{t}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\mathbf{8}$ | $\mathbf{9}$ | $\mathbf{1 0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PVIF (t, 12\%) | 0.892 | 0.797 | 0.711 | 0.635 | 0.567 | 0.506 | 0.452 | 0.403 | 0.360 | 0.322 |

[(10 Marks) Nov 22]

## Answer

Statement of PV of outflow under Option 1

| Year | Particulars | ₹ | DF @ 12\% | PV |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Tax Shield on depreciation ( $37,500 \times 0.3$ ) | 11,250 | 0.892 | 10,035 |
| 2 | Tax Shield on depreciation ( $28,125 \times 0.3$ ) | 8,438 | 0.797 | 6,725 |
| 3 | Tax Shield on depreciation ( $21,094 \times 0.3$ ) | 6,328 | 0.711 | 4,499 |
| 4 | Tax Shield on depreciation ( $15,820 \times 0.3$ ) | 4,746 | 0.635 | 3,014 |
| 5 | Tax Shield on depreciation ( $11,865 \times 0.3$ ) | 3,560 | 0.567 | 2,019 |
| 6 | Tax Shield on depreciation ( $8,899 \times 0.3$ ) | 2,670 | 0.506 | 1,351 |
| 7 | Tax Shield on depreciation (6,674 $\times 0.3$ ) | 2,002 | 0.452 | 905 |
| 8 | Tax Shield on depreciation ( $5,006 \times 0.3$ ) | 1,502 | 0.403 | 605 |
| 9 | Tax Shield on depreciation ( $3,754 \times 0.3$ ) | 1,126 | 0.360 | 405 |
| 10 | Tax Shield on depreciation ( $2,816 \times 0.3$ ) | 845 | 0.322 | 272 |
| 10 | Scrap value new three wheeler | 8,447 | 0.322 | 2,720 |
| PV of Inflows |  |  |  | 32,550 |
| PV of Outflows (Initial Cost of new three wheeler) |  |  |  | 1,50,000 |
| Net PV of Outflows (1,50,000-32,550) |  |  |  | 1,17,450 |

Statement of PV of outflow under Option 2

| Year | Particulars | ₹ | DF @ 12\% | PV |
| :---: | :--- | :---: | :---: | :---: |
| 1 | Tax Shield on depreciation $(20,000 \times 0.3)$ | 6,000 | 0.892 | 5,352 |
| 2 | Tax Shield on depreciation $(15,000 \times 0.3)$ | 4,500 | 0.797 | 3,587 |
| 3 | Tax Shield on depreciation $(11,250 \times 0.3)$ | 3,375 | 0.711 | 2,400 |
| 4 | Tax Shield on depreciation $(8,438 \times 0.3)$ | 2,531 | 0.635 | 1,607 |
| 5 | Tax Shield on depreciation (6,328 $\times 0.3)$ | 1,898 | 0.567 | 1,076 |
| 5 | Scrap value of second hand vehicle 1 | 18,984 | 0.567 | 10,764 |
| 6 | Tax Shield on depreciation $(15,000 \times 0.3)$ | 4,500 | 0.506 | 2,277 |
| 7 | Tax Shield on depreciation $(11,250 \times 0.3)$ | 3,375 | 0.452 | 1,526 |
| 8 | Tax Shield on depreciation $(8,438 \times 0.3)$ | 2,531 | 0.403 | 1,020 |
| 9 | Tax Shield on depreciation (6,328 $\times 0.3)$ | 1,898 | 0.360 | 683 |
| 10 | Tax Shield on depreciation (4,746 $\times 0.3)$ | 1,424 | 0.322 | 459 |
| 10 | Scrap value of second hand vehicle 2 | 14,238 | 0.322 | 4,585 |
| PV of Inflows |  |  |  |  |
| PV of Outflows (80,000 $+60,000 \times 0.567)$ |  |  |  |  |

Advise: Select option 2 having lower Net PV of Outflows.

## PYQ 17

A hospital is considering to purchase a diagnostic machine costing ₹ 80,000 . The projected life of the machine is 8 years and has an expected salvage value of $₹ 6,000$ at the end of 8 years. The annual operating cost of the machine is $₹ 7,500$. It is expected to generate revenues of $₹ 40,000$ per year for eight years. Presently, the hospital is outsourcing the diagnostic work and is earning commission income of ₹ 12,000 per annum. Consider tax rate of $30 \%$ Discounting Rate as $10 \%$.

Advise: Whether it would be profitable for the hospital to purchase the machine?

## Give your recommendation as per Net Present Value method and Present Value Index method under below mentioned two situations:

(i) If Commission income of ₹ 12,000 p.a. is before taxes.
(ii) If Commission income of ₹ 12,000 p.a. is net of taxes.

| $\boldsymbol{t}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\boldsymbol{8}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PVIF (t, 10\%) | 0.909 | 0.826 | 0.751 | 0.683 | 0.621 | 0.564 | 0.513 | 0.467 |

[(10 Marks) Nov 2022]

## Answer

(i) Net Present Value and Present Value Index when commission income is before tax:

Net Present Value

| Year | Particulars | ₹ | DF @ 10\% | DCF |
| :---: | :--- | :---: | :---: | :---: |
| 0 | Initial Outflows | $(80,000)$ | 1.000 | $(80,000)$ |
| $1-8$ | Cash Flow After Tax | 17,125 | 5.334 | 91,345 |
| 8 | Salvage | 6,000 | 0.467 | 2,802 |
| NPV |  |  |  | $\mathbf{1 4 , 1 4 7}$ |

Profitability Index $=\frac{\text { PV of Inflows }}{\text { PV of Outflows }}=\frac{94,147}{80,000}=1.18$

Advise: Since the net present value (NPV) is positive and profitability index is also greater than 1, it is profitable for the hospital to purchase the machine.
(ii) Net Present Value and Present Value Index when commission income is before tax:

Net Present Value

| Year | Particulars | ₹ | DF @ 10\% | DCF |
| :---: | :--- | :---: | :---: | :---: |
| 0 | Initial Outflows | $(80,000)$ | 1.000 | $(80,000)$ |
| $1-8$ | Cash Flow After Tax | 13,525 | 5.334 | 72,142 |
| 8 | Salvage | 6,000 | 0.467 | 2,802 |
| NPV |  |  |  | $(5,056)$ |

$$
\text { Profitability Index }=\frac{\mathrm{PV} \text { of Inflows }}{\mathrm{PV} \text { of Outflows }} \quad=\quad \frac{74,944}{80,000}=0.94
$$

Advise: Since the net present value (NPV) is negative and profitability index is also lower than 1, it is not profitable for the hospital to purchase the machine.

## Working Notes:

## Calculation of CFAT:

| Particulars | Case (i) | Case (ii) |
| :--- | :---: | :---: |
| Sales | 40,000 | 40,000 |
| Less: Operating cost | 7,500 | 7,500 |
| Less: Depreciation $(80,000-6,000) \div 8$ years | 9,250 | 9,250 |
| Less: Loss of commission income before tax | $(12,000)$ | - |
| Net Income | 11,250 | 23,250 |
| Less: Tax @ 30\% | $(3,375)$ | $(6,975)$ |
| PAT | 7,875 | 16,275 |
| Add: Depreciation | 9,250 | 9,250 |
| Cash inflows after tax per annum | $\mathbf{1 7 , 1 2 5}$ | 25,525 |
| Less: Loss of commission income after tax | - | $(12,000)$ |
|  | $\mathbf{N e t ~ C F A T ~}$ | $\mathbf{1 7 , 1 2 5}$ |
| $\mathbf{1 3 , 5 2 5}$ |  |  |

## PYQ 18

Four years ago, Z Ltd. had purchased a machine of ₹4,80,000 having estimated useful life of 8 years with zero salvage value. Depreciation charged using SLM method over the useful life. The company want to replace this machine with a new machine. Details of new machine are as below:

- Cost of new machine is $₹ 12,00,000$ Vendor of this machine is agreed to take old machine at a value of ₹ $2,40,000$. Cost of dismantling and removal of old machine will be ₹ $40,000.80 \%$ of net purchase price will be paid on spot and remaining will be paid at the end of one year.
- Depreciation will be charged @ 20\% p.a. under WDV method.
- Estimated useful life of new machine is four years and it has salvage value of ₹ $1,00,000$ at the end of year four.
- Incremental annual sales revenue is ₹ $12,25,000$.
- Contribution margin is $50 \%$.
- Incremental indirect cost (excluding depreciation) is ₹ $1,18,750$ per year.
- Additional working capital of ₹2,50,000 is required at the beginning of the year one and ₹ $3,00,000$ at the beginning of the year three. Working capital at the end of the year four will be nil.
- Tax rate is $30 \%$
- Ignore tax on capital gain.
- Z Ltd. will not make any additional investment, if it yields less than $12 \%$.

Advise, whether existing machine should be replaced or not.

| Year | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |
| ---: | :---: | :---: | :---: | :---: | :---: |
| PVIF $_{0.12, \mathrm{t}}$ | 0.893 | 0.797 | 0.712 | 0.636 | 0.567 |

[(10 Marks) May 23]

## Answer

Statement of NPV

| Year | Particulars | ₹ | DF @12\% | PV |
| :---: | :--- | :---: | :---: | :---: |
| 0 | Initial outflows | $(10,50,000)$ | 1.000 | $(10,50,000)$ |
| 1 | Incremental CFAT - 20\% of Net purchase price | $1,99,625$ | 0.893 | $1,78,265$ |
| 2 | $(3,99,625-20 \%$ of 10,00,000) | 85,225 | 0.797 | 67,924 |


| 3 | $(3,85,225-3,00,000)$ | $3,73,705$ | 0.712 | $2,66,078$ |
| :--- | :--- | :---: | :---: | :---: |
| 4 | Incremental CFAT | $10,14,489$ | 0.636 | $6,45,215$ |
|  | Incremental CFAT + Incremental Salvage + WC |  |  |  |
|  | $(3,64,489+1,00,000+5,50,000)$ | NPV | $\mathbf{1 , 0 7 , 4 8 2}$ |  |

Advise: The company should replace existing machine with new machine having positive NPV

## Working Notes:

## 1. Calculation of initial outflow:

| Cost of new machine | $12,00,000$ |
| :--- | :---: |
| Less: Sales value of old machine net of disposal $(2,40,000-40,000)$ | $(2,00,000)$ |
| Net Purchase Price | $10,00,000$ |
|  |  |
| 80\% of Net purchase price $(80 \%$ of $10,00,000)$ | $8,00,000$ |
| Add: Additional Working Capital | $2,50,000$ |
|  | $\mathbf{1 0 , 5 0 , 0 0 0}$ |

## 2. Calculation of incremental CFAT:

| Particulars | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ |
| :--- | :---: | :---: | :---: | :---: |
| Incremental Contribution $(12,25,000 \times$ | $6,12,500$ | $6,12,500$ | $6,12,500$ | $6,12,500$ |
| $50 \%)$ | $(1,18,750)$ | $(1,18,750)$ | $(1,18,750)$ | $(1,18,750)$ |
| Less: Incremental indirect cost | $(1,80,000)$ | $(1,32,000)$ | $(93,600)$ | $(62,880)$ |
| Less: Incremental Depreciation | $\mathbf{3 , 1 3 , 7 5 0}$ | $\mathbf{3 , 6 1 , 7 5 0}$ | $\mathbf{4 , 0 0 , 1 5 0}$ | $\mathbf{4 , 3 0 , 8 7 0}$ |
| Incremental PBT | $(94,125)$ | $(1,08,525)$ | $(1,20,045)$ | $(1,29,261)$ |
| Less: Tax @ 30\% | $\mathbf{2 , 1 9 , 6 2 5}$ | $\mathbf{2 , 5 3 , 2 2 5}$ | $\mathbf{2 , 8 0 , 1 0 5}$ | $3,01,609$ |
| Incremental PAT | $\mathbf{P A , 8 0 , 0 0 0}$ | $1,3,000$ | 93,600 | 62,880 |
| Add: Incremental Depreciation | $\mathbf{3 , 9 9 , 6 2 5}$ | $\mathbf{3 , 8 5 , 2 2 5}$ | $\mathbf{3 , 7 3 , 7 0 5}$ | $\mathbf{3 , 6 4 , 4 8 9}$ |
| Incremental CFAT |  |  |  |  |

## 3. Incremental Depreciation:

| Year 1 | = | 12,00,000 $\times 20 \%-(4,80,000 \div 8$ years $)$ | = | ₹ $1,80,000$ |
| :---: | :---: | :---: | :---: | :---: |
| Year 2 | = | 9,60,000 $\times 20 \%-60,000$ | = | ₹1,32,000 |
| Year 3 | = | 7,68,000 $\times 20 \%-60,000$ | = | ₹ 93,600 |
| Year 4 | = | 6,14,400 $\times 20 \%-60,000$ | = | ₹ 62,880 |

## PYQ 19

ABC Ltd. is considering to purchase a machine which is priced at $₹ 5,00,000$. The estimated life of machine is 5 years and has an expected salvage value of ₹ 45,000 at the end of 5 years. It is expected to generate revenue of $₹ 1,50,000$ per annum for five years. The annual operating cost of the machine is ₹ 28,125 , Corporate Tax Rate is $20 \%$ and the cost of capital is $10 \%$.

You are required to analyse whether it would be profitable for the company to purchase the machine by using;
(a) Payback period Method
(b) Net Present value method
(c) Profitability Index Method

Answer
(a) Payback period $=5,00,000 \div 1,15,700=4.32$ years

Project should be accepted having payback period less than life of project.
(b) Statement of NPV

| Years | Particulars | ₹ | DF @ 10\% | PV |
| :---: | :--- | :---: | :---: | :---: |
| 0 | Investment (outflow) | $(5,00,000)$ | 1.000 | $(5,00,000)$ |
| $1-5$ | CFAT | $1,15,700$ | 3.791 | $4,38,619$ |
| 5 | Salvage | 45,000 | 0.621 | 27,945 |
| NPV |  |  | $(33,436)$ |  |

Project should be rejected having negative NPV.
(c) Profitability Index $=4,66,564 \div 5,00,000=0.93$

Project should be rejected having PI less than 1.

## Working Note:

## Calculation of CFAT

| Particulars | ₹ |
| :---: | :---: |
| Sales value | 1,50,000 |
| Less: Operating cost ( 50,000 gallon $\times$ ₹ 5 ) | $(28,125)$ |
| Less: Depreciation (5,00,000-45,0000 $\div 5$ years | $(91,000)$ |
| PBT | 30,875 |
| Less: Tax @ 20\% | $(6,175)$ |
| PAT | 24,700 |
| Add: Depreciation | 91,000 |
| Annual CFAT | 1,15,700 |

## SUGGESTED REVISION FOR EXAM:

BQ: $\quad 2,12,14,15,16,18,21,22,23,24,25,28,30,31,34,35,36,37$
PYQ: 6, 9, 13, 14, 15

## BQ 1

Vishnu steels Ltd. has issued 30,000 irredeemable 14\% debentures of ₹ 150 each. The cost of flotation of debentures is $5 \%$ of the total issued amount. The company's taxation rate is $40 \%$.

## Calculate the cost of debt.

[ $K_{d} 8.84 \%$ ]

## BQ 2

Five years ago, Sona Limited issued 12 per cent irredeemable debentures at ₹103, at ₹ 3 premium to their par value of ₹ 100 . The current market price of these debentures is ₹ 94 . If the company pays corporate tax at a rate of 35 per cent What is its current cost of debenture capital?
[ $K_{d} 8.30 \%$ ]

## BQ 3

Surya Industries Ltd. has raised funds through issue of 10,000 debentures of ₹ 150 each at a discount of ₹ 10 per debenture with 10 years maturity. The coupon rate is $16 \%$. The flotation cost is $₹ 5$ per debenture. The debentures are redeemable with a $10 \%$ premium. The corporate taxation rate is $40 \%$.

## Calculate the cost of debenture.

[ $K_{d} 11.60 \%$ ]

## BQ 4

Business machines Ltd. has issued redeemable debentures of ₹100 each repayable at the end of 8 year period on a coupon rate of $14 \%$. The flotation expenses are $10 \%$ of issue amount.

## Calculate the cost of debt.

[ $K_{d} 16.05 \%$ ]

## BQ 5

A company issued $10,000,10 \%$ debentures of $₹ 100$ each at a premium of $10 \%$ on 1.4 .2020 to be matured on 1.4.2025. The debentures will be redeemed on maturity. Compute the cost of debentures assuming $35 \%$ as tax rate.
[ $K_{d} 4.28 \%$ ]

## BQ 6

A company issued $10,000,10 \%$ debentures of $₹ 100$ each on 1.4.2020 to be matured on 1.4.2025. The company wants to know the current cost of its existing debt and the market price of the debentures is ₹ 80 . Compute the cost of existing debentures assuming $35 \%$ tax rate.
[ $K_{d} 11.67 \%$ ]

## BQ 7

Express cargo Ltd has issued 4 years Zero Coupon Bonds of ₹ 1,000 each at a price of ₹ 636 .

BQ 8
Institutional Development Bank (IDB) issued Zero interest deep discount bonds of face value of ₹ $1,00,000$ each issued at ₹ 2,500 \& repayable after 25 years.

Compute the cost of debt if there is no corporate tax.

## Answer

Here,
Redemption Value (RV) = ₹ $1,00,000$
Net Proceeds (NP) $=\quad ₹ 2,500$
Interest $=0$
Life of bond $=25$ years
There is huge difference between RV and NP therefore in place of approximation method we should use trial \& error method.

| FV | $=$ | $\mathrm{PV} \times(1+r)^{\mathrm{n}}$ |
| :--- | :--- | :--- |
| $1,00,000$ | $=$ | $2,500 \times(1+r)^{25}$ |
| 40 | $=$ | $(1+r)^{25}$ |

Trial 1: $r \quad=\quad 15 \%, \quad(1.15)^{25} \quad=\quad 32.919$
Trial 2: $r=16 \%, \quad(1.16)^{25} \quad=\quad 40.874$

Here:

| L | = | 15\% |  |  |
| :---: | :---: | :---: | :---: | :---: |
| H | = | 16\% |  |  |
| $\mathrm{NPV}_{\mathrm{L}}$ | = | 32.919-40 | = | - 7.081 |
| $\mathrm{NPV}_{\mathrm{H}}$ | = | 40.874-40 | = | + 0.874 |
| IRR/ $\mathrm{K}_{\mathrm{d}}$ | = | $\mathrm{LR}+\frac{\mathrm{NPV}_{\mathrm{L}}}{\mathrm{NPV}_{\mathrm{L}}-\mathrm{NPV}_{\mathrm{H}}} \times(\mathrm{H}-\mathrm{L})$ |  |  |
|  | = | $15 \%+\frac{-7.081}{-7.081-0.874} \times(16 \%-15 \%)$ | = | 15.89\% |

## BQ 9

A company issued $10,000,10 \%$ debentures of $₹ 100$ each on 1.4.2020 to be matured on 1.4.2025. The company wants to know the current cost of its existing debt and the market price of the debentures is ₹80.

Compute the cost of existing debentures by using Present value method/Yield to maturity approach (YTM) assuming 35\% tax rate.

## Answer

(a) Identification of relevant cash flows:

| Year | Cash Flows |
| :---: | :--- |
| 0 | Current market price $\left(\mathrm{P}_{0}\right)=₹ 80$ |
| 1 to 5 | Interest net of tax $[\mathrm{I}(1-\mathrm{t})]=10 \%$ of ₹ $100(1-0.35)=₹ 6.5$ |
| 5 | Redemption value $(\mathrm{RV})=$ Face value i.e. ₹ 100 |

(b) Calculation of NPV at two discount rates:

| Year | Cash Flow | Present Value |  | Present Value |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $10 \%$ | DCF | $15 \%$ | DCF |


| 0 | 80 | 1.000 | $(80)$ | 1.000 | $(80)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $1-5$ | 6.5 | 3.791 | 24.64 | 3.352 | 21.79 |
| 5 | 100 | 0.621 | 62.10 | 0.497 | 49.70 |
|  |  |  | $\mathbf{+ 6 . 7 4}$ | $\mathbf{- 8 . 5 1}$ |  |

(c) Calculation of IRR $/ K_{d}$

$$
\begin{aligned}
I R R / K_{\mathrm{d}} & =\mathrm{LR}+\frac{\mathrm{NPV}_{\mathrm{L}}}{\mathrm{NPV}_{\mathrm{L}}-\mathrm{NPV}_{\mathrm{H}}} \times(\mathrm{H}-\mathrm{L})=10 \%+\frac{6.74}{6.74-(-8.51)} \times(15 \%-10 \%) \\
& =12.21 \%
\end{aligned}
$$

YTM or present value method is a superior method of determining cost of debt of a company to approximation method and it is also preferred in the field of finance.

## BQ 10

A company issued $10,000,15 \%$ Convertible debentures of ₹ 100 each with a maturity period of 5 years. At maturity the debenture holders will have the option to convert the debentures into equity shares of the company in the ratio of $1: 10$ ( 10 shares for each debenture). The current market price of the equity shares is ₹ 12 each and historically the growth rate of the shares are $5 \%$ per annum.

Compute the cost of debentures assuming 35\% tax rate.

## Answer

## Determination of Redemption value:

Higher of
(i) The cash value of debentures $=$ ₹ 100
(ii) Value of equity shares $=10$ shares $\times ₹ 12(1+0.05)^{5}$
$=10$ shares $\times ₹ 12 \times 1.276=₹ 153.12$
₹ 153.12 will be taken as redemption value as it is higher than the cash option and attractive to the investors.

## Calculation of Cost of Convertible debenture:

## Alternative 1: Using approximation method:

$$
K_{d}=\quad \frac{I(1-\mathrm{t})+\frac{\mathrm{RV}-\mathrm{NP}}{\mathrm{n}}}{\frac{\mathrm{RV}+\mathrm{NP}}{2}} \times 100=\quad \frac{15(1-0.35)+\frac{153.12-100}{5}}{\frac{153.12+100}{2}} \times 100=16.09 \%
$$

## Alternative 2: Using present value method:

## Calculation of NPV at two discount rates:

| Year | Cash Flow | Present Value |  | Present Value |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathbf{1 5 \%}$ | $\boldsymbol{D C F}$ | $\mathbf{2 0} \%$ | $\boldsymbol{D C F}$ |
| 0 | 100 | 1.000 | $(100)$ | 1.000 | $(100)$ |
| $1-5$ | 9.75 | 3.352 | 32.68 | 2.991 | 29.16 |
| 5 | 153.12 | 0.497 | 76.10 | 0.402 | 61.55 |
| NPV |  |  | $\mathbf{+ 8 . 7 8}$ |  | $\mathbf{- 9 . 2 9}$ |

$\mathrm{IRR} / \mathrm{K}_{\mathrm{d}}=\quad \mathrm{LR}+\frac{\mathrm{NPV}_{\mathrm{L}}}{\mathrm{NPV}_{\mathrm{L}}-\mathrm{NPV}_{\mathrm{H}}} \times(\mathrm{H}-\mathrm{L})=15 \%+\frac{8.78}{8.78-(-9.29)} \times(20 \%-15 \%)=\mathbf{1 7 . 4 3 \%}$

## BQ 11

RBML is proposing to sell a 5 -year bond of ₹ 5,000 at 8 per cent rate of interest per annum. The bond amount will be amortised equally over its life.

What is the bond's present value for an investor if he expects a minimum rate of return of 6 per cent?

## Answer

The amount of interest will go on declining as the outstanding amount of bond will be reducing due to amortisation. The amount of interest for five years will be:

| First year | $:$ | $₹ 5,000 \times 0.08$ | $=$ | $₹ 400$ |
| :--- | :--- | :--- | :--- | :--- |
| Second year | $:$ | $(₹ 5,000-₹ 1,000) \times 0.08$ | $=$ | $₹ 320$ |
| Third year | $:$ | $(₹ 4,000-₹ 1,000) \times 0.08$ | $=$ | $₹ 240$ |
| Fourth year | $:$ | $(₹ 3,000-₹ 1,000) \times 0.08$ | $=$ | $₹ 160 ;$ and |
| Fifth year | $:$ | $(₹ 2,000-₹ 1,000) \times 0.08$ | $=$ | $₹ 80$. |

The outstanding amount of bond will be zero at the end of fifth year. Since RBML will have to return ₹ 1,000 every year, the outflows every year will consist of interest payment and repayment of principal:

| First year | $:$ | $₹ 1,000+₹ 400$ | $=$ | $₹ 1,400$ |
| :--- | :--- | :--- | :--- | :--- |
| Second year | $:$ | $₹ 1,000+₹ 320$ | $=$ | $₹ 1,320$ |
| Third year | $:$ | $₹ 1,000+₹ 240$ | $=$ | $₹ 1,240$ |
| Fourth year | $:$ | $₹ 1,000+₹ 160$ | $=$ | $₹ 1,160 ;$ and |
| Fifth year | $:$ | $₹ 1,000+₹ 80$ | $=$ | $₹ 1,080$. |

The above cash flows of all five years will be discounted with the cost of capital. Here the expected rate i.e. $6 \%$ will be used. Value of the bond is calculated as follows:

$$
\begin{align*}
V_{B} & =\frac{1,400}{(1.06)^{1}}+\frac{1,320}{(1.06)^{2}}+\frac{1,240}{(1.06)^{3}}+\frac{1,160}{(1.06)^{4}}+\frac{1,080}{(1.06)^{5}} \\
& =₹ 1,320.75+₹ 1,174.80+₹ 1,041.14+₹ 918.88+₹ 807.05
\end{align*}
$$

COST OF PREFERENCE SHARE CAPITAL ( $K_{p}$ )

## BQ 12

XYZ Ltd. issues 2,000 10\% preference shares of ₹100 each at ₹95 each. The company proposes to redeem the preference shares at the end of $10^{\text {th }}$ year from the date of issue.

## Calculate the cost of preference share capital.

## Answer

$$
\mathrm{K}_{\mathrm{p}}=\frac{\mathrm{PD}+\left(\frac{\mathrm{RV}-\mathrm{NP}}{\mathrm{n}}\right)}{\frac{\mathrm{RV}+\mathrm{NP}}{2}} \times 100=\frac{10+\left(\frac{100-95}{10}\right)}{\frac{100+95}{2}} \times 100 \quad=10.77 \%
$$

## BQ 13

XYZ \& Co. issues 2,000 10\% preference shares of ₹ 100 each at ₹ 95 each.

Answer

$$
\mathrm{K}_{\mathrm{p}}=\frac{\mathrm{PD}}{\mathrm{NP}} \times 100=\frac{10}{95} \times 100=10.53 \%
$$

BQ 14
If R Energy is issuing preferred stock at ₹ 100 per share, with a stated dividend of ₹ 12 , and a floatation cost of $3 \%$ then,

What is the cost of preference share?

## Answer

$$
\mathrm{K}_{\mathrm{p}}=\frac{\mathrm{PD}}{\mathrm{IP}(1-\text { Floatation Cost })} \times 100=\frac{12}{100(1-.03)} \times 100=12.37 \%
$$

## COST OF EQUITY SHARE CAPITAL (Ke)

## BQ 15

Radiant Ltd. has disbursed a dividend of ₹ 30 on each Equity share of $₹ 10$. The current market price of share is ₹ 80 .

Calculate the cost of equity as per dividend yield method.
[ $\left.K_{e} 37.50 \%\right]$
BQ 16
Prabhat Ltd. has 50,000 equity shares of ₹ 10 each and its current market value is ₹ 45 each. The after tax profit of the company for the year is ₹9,60,000.

Calculate the cost of equity based on price earnings/yield method.

## Answer

| $K_{e}$ | $=\frac{E P S}{M P S} \times 100$ |
| :--- | :--- |
| EPS | $=\frac{19.20}{45.00} \times 100$ |
| No. of Equity shares | $=\frac{9,60,000}{50,000}=$ ₹arings 19.20 |

## BQ 17

Fox Ltd. issued new 10,000 equity shares of $₹ 10$ each at a premium of $₹ 2$ each. The company has incurred issue expenses of $₹ 5,000$. The equity shareholder's expects the rate of dividend to $18 \%$ p.a.

Calculate the cost of equity share capital. Will your answer be different if these shares are existing shares and the current market price of share is ₹21?

## Answer

(a) Since the Equity shares are newly issued, the cost of equity of it can be calculated as follows:

$$
\begin{aligned}
\mathrm{K}_{\mathrm{e}}(\text { New share }) & =\frac{\text { Expected dividend }}{\text { Net proceeds }} \times 100 \\
& =\frac{1.80}{11.50} \times 100
\end{aligned}
$$

$$
\text { Net proceeds per share }=\frac{(10,000 \text { Equity shares } \times 12.00)-5,000}{10,000 \text { Shares }}=₹ 11.50
$$

(b) In case of existing equity shares, market price is to be taken as basis for calculation of cost of equity capital as follows:
$\mathrm{K}_{\mathrm{e}}=\frac{\text { Expected dividend }}{\text { Current market price }} \times 100=\frac{1.80}{21.00} \times 100=\mathbf{8 . 5 7 \%}$
BQ 18
A company has paid dividend of ₹ 1 per share (of face value of ₹ 10 each) last year and it is expected to grow @ $10 \%$ next year. Calculate the cost of equity if the market price of share is ₹55.

## Calculate the cost of equity.

## Answer

$$
\mathrm{K}_{\mathrm{e}} \quad=\frac{\mathrm{D}_{1}}{\mathrm{P}_{0}}+\mathrm{g}=\frac{1(1+0.10)}{55}+.10=12 \%
$$

## BQ 19

The equity of Mercury Ltd. are traded in the market at $₹ 90$ each. The current year expected dividend per share is ₹ 18 . The subsequent growth in dividends is expected at the rate of $6 \%$.

## Calculate the cost of equity capital.

[ $K_{e}$ 26\%]

## BQ 20

Bright Star Ltd. has its equity shares of ₹10 each quoted in a stock exchange has market price of ₹56. A constant expected annual growth rate of $6 \%$ and a dividend of ₹ 3.60 per share has been paid for the current year.

Calculate the cost of capital.
[ $K_{e}$ 12.81\%]

## BQ 21

(a) A Company's shares are quoted at ₹250. The dividend just paid was ₹50. Face value per share $₹ 100$. No growth in dividend is expected. Compute K .
(b) Presume in the above part the anticipated growth rate in dividend is $10 \%$ p.a. Compute $\mathrm{K}_{\mathrm{e}}$.
(c) Presume in part (a), investors in the company have a required rate of return of $15 \%$. Current dividends of $₹ 30$ per share have just been paid. No increase is anticipated. Estimate the share price today.
(d) Presume in part (c), dividends are expected to grow @ 5\% p.a. Estimate share price today.

$$
\left[(a) K_{e} 20 \% \text {, (b) } K_{e} 32 \% \text {, (c) } P_{o} ₹ 200,(d) P_{o}\right. \text { ₹315] }
$$

BQ 22
Sun Ltd. has its shares of ₹10 each quoted on the stock exchange; the current price per share is ₹ 24 . During the previous 3 years, dividends have steadily increased from ₹ 1.20 to ₹ 1.60 per share.

## BQ 23

Calculate the cost of equity capital of $H$ Ltd., whose risk free rate of return equals $10 \%$. The firm's beta equals 1.75 and the return on the market portfolio equals to $15 \%$.

## Answer

$$
\mathrm{K}_{\mathrm{e}}=\mathrm{R}_{\mathrm{f}}+\beta\left(\mathrm{R}_{\mathrm{m}}-\mathrm{R}_{\mathrm{f}}\right)=10 \%+1.75 \times(15 \%-10 \%)=18.75 \%
$$

## BQ 24

The risk free return is $10 \%$ and the risk premium is $5 \%$ with beta of a company is 1.6 . During the previous 5 years, dividends have steadily increased from ₹ 2.115 to ₹ 2.966 per share. The company's earnings and the dividend experienced constant growth.

Find out the intrinsic value (Market value of share) of the shares.

## Answer

| $\mathrm{P}_{0}$ | $=\frac{\mathrm{D}_{1}}{\mathrm{~K}_{\mathrm{e}}-\mathrm{g}}$ | $=\frac{3(1+.07)}{18 \%-7 \%}$ | $=$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{K}_{\mathrm{e}} 29.18$ |  |  |  |
| Growth rate | $=$ | $\mathrm{R}_{\mathrm{f}}+\beta\left(\mathrm{R}_{\mathrm{m}}-\mathrm{R}_{\mathrm{f}}\right)=$ | $10 \%+1.6 \times(5 \%)$ |
|  | $=\sqrt[5]{\frac{\text { Latest Dividend }}{\text { First Dividend }}}-1$ | $=\sqrt[5]{\frac{2.966}{2.115}}-1$ | $=$ |

## BQ 25

Mr. Mehra had purchased a share of Alpha Limited for ₹ 1,000 . He received dividend for a period of five years at the rate of 10 percent. At the end of the fifth year, he sold the share of Alpha Limited for ₹ 1,128 .

You are required to compute the cost of equity as per realised yield approach.

## Answer

## Calculation of NPV at two discount rates:

| Year | Cash Flow | Present Value |  | Present Value |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathbf{1 1 \%}$ | DCF | $\mathbf{1 3 \%}$ | DCF |
| 0 | 1,000 | 1.000 | 1,000 | 1.000 | $(1,000)$ |
| $1-5$ | 100 | 3.696 | 369.60 | 3.517 | 351.70 |
| 5 | 1,128 | 0.593 | 668.90 | 0.543 | 612.50 |
|  |  |  | +38.50 |  | -35.80 |

Calculation of $\operatorname{IRR} / K_{e}$ :
$\mathrm{K}_{\mathrm{e}}=\mathrm{LR}+\frac{\mathrm{NPV}_{\mathrm{L}}}{\mathrm{NPV}_{\mathrm{L}}-\mathrm{NPV}_{\mathrm{H}}} \times(\mathrm{H}-\mathrm{L})=11 \%+\frac{38.50}{38.50-(-35.80)} \times(13 \%-11 \%)=\mathbf{1 2 . 0 4 \%}$
BQ 26
Calculate the cost of equity from the following data using realized yield approach:

| Year | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |
| :--- | :---: | :---: | :--- | :---: | :--- |
| Dividend per share |  |  |  |  |  |
| Price per share (at the beginning) | 9.00 | 1.00 | 1.20 | 1.25 | 1.15 |
| Pr | 9.75 | 11.50 | 11.00 | 10.60 |  |

## Answer

In this questions we will first calculate yield for last 4 years and then calculate it geometric mean as follows:

| $1+\mathrm{Y}_{1}$ | $=\frac{\mathrm{D}_{1}+\mathrm{P}_{1}}{\mathrm{P}_{0}}$ | $=\frac{1+9.75}{9}$ | $=$ | 1.1944 |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $1+\mathrm{Y}_{2}$ | $=$ | $\frac{\mathrm{D}_{2}+\mathrm{P}_{2}}{\mathrm{P}_{1}}$ | $=$ | $\frac{1+11.50}{9.75}$ | $=$ |
| $1+\mathrm{Y}_{3}$ | $=\frac{\mathrm{D}_{3}+\mathrm{P}_{3}}{\mathrm{P}_{2}}$ | $=$ | 1.2821 |  |  |
| $1+\mathrm{Y}_{4}$ | $=$ | $\frac{1.2+11}{11.50}$ | $=$ | 1.0609 |  |
| $\mathrm{P}_{3}$ |  |  | $\frac{1.25+10.60}{11}$ | $=$ | 1.0772 |

## Geometric mean:

$$
\begin{aligned}
& \mathrm{K}_{\mathrm{e}}=\left[\left(1+Y_{1}\right) \times\left(1+Y_{2}\right) \times \ldots \ldots\left(1+Y_{n}\right)\right]^{1 / n}-1 \\
& \mathrm{~K}_{\mathrm{e}} \quad=\quad[1.1944 \times 1.2821 \times 1.0609 \times 1.0772]^{1 / 4}-1=\boldsymbol{0 . 1 5} \text { or } \mathbf{1 5 \%}
\end{aligned}
$$

BQ 27
ABC Company's equity share is quoted in the market at ₹ 25 per share currently. The company pays a dividend of ₹ 2 per share and the investor's market expects a growth rate of $6 \%$ per year.

## You are required to:

(i) Calculate the company's cost of equity capital.
(ii) If the company issues $10 \%$ debentures of face value of ₹ 100 each and realises ₹96 per debenture while the debentures are redeemable after 12 years at a premium of $12 \%$, calculate cost of debenture using YTM?

Assume Tax Rate to be $50 \%$.

## Answer

(i) Cost of Equity Capital ( $K_{e}$ ):

$$
\mathrm{K}_{\mathrm{e}} \quad=\frac{\mathrm{D}_{1}}{\mathrm{P}_{0}}+\mathrm{g} \quad=\frac{2(1+0.06)}{25}+.06 \quad=\quad 14.48 \%
$$

Note: Dividend ₹2 is treated as $\mathrm{D}_{0}$, student may treat it as $\mathrm{D}_{1}$ and answer will change accordingly.
(ii) Cost of Debenture ( $K_{d}$ ):

## Identification of relevant cash flows:

| Year | Cash Flows |
| :---: | :--- |
| 0 | Current market price $\left(\mathrm{P}_{0}\right)=₹ 96$ |
| 1 to 12 | Interest net of tax $[\mathrm{I}(1-\mathrm{t})]=10 \%$ of $₹ 100(1-0.50)=₹ 5$ |
| 12 | Redemption value $(\mathrm{RV})=₹ 112$ |

Calculation of NPV at two discount rates

| Year | Cash Flow | Present Value |  | Present Value |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $5 \%$ | DCF | $10 \%$ | DCF |


| 0 | 96 | 1.000 | $(96)$ | 1.000 | $(96)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $1-12$ | 5 | 8.863 | 44.32 | 6.814 | 34.07 |
| 12 | 112 | 0.557 | 62.38 | 0.319 | 35.73 |
|  |  | $\mathbf{+ 1 0 . 7 0}$ |  | $\mathbf{- 2 6 . 2 0}$ |  |

## Calculation of IRR/K $K_{d}$

$$
\mathrm{IRR} / \mathrm{K}_{\mathrm{d}}=\quad \mathrm{LR}+\frac{\mathrm{NPV}_{\mathrm{L}}}{\mathrm{NPV}_{\mathrm{L}}-\mathrm{NPV}_{\mathrm{H}}} \times(\mathrm{H}-\mathrm{L})=5 \%+\frac{10.70}{10.70-(26.20)}(10 \%-5 \%)=
$$

## COST OF RETAINED EARNINGS ( $K_{r}$ )

## BQ 28

ABC Company provides the following details:

$\mathrm{D}_{0}=$ ₹ $4.19 \quad \mathrm{P}_{0}=$|  |
| :--- |
| 50 |

## Calculate the cost of retained earnings.

## Answer

$$
\mathrm{Kr}=\frac{\mathrm{D}_{1}}{\mathrm{P}_{0}}+\mathrm{g} \quad=\quad \frac{4.19(1+.05)}{50}+0.05 \quad=13.80 \%
$$

BQ 29
ABC Company provides the following details:

$$
\operatorname{Rf}=7 \% \quad B \quad=1.20 \quad \mathrm{Rm}-\mathrm{Rf}=6 \%
$$

Calculate the cost of retained earnings based on CAPM method.

## Answer

$$
\mathrm{Kr}=\mathrm{R}_{\mathrm{f}}+\beta\left(\mathrm{R}_{\mathrm{m}}-\mathrm{R}_{\mathrm{f}}\right)=7 \%+1.2 \times(6 \%)=14.20 \%
$$

## BQ 30

Face value of equity shares of a company is ₹ 10 , while current market price is ₹ 200 per share. Company is going to start a new project, and is planning to finance it partially by new issue and partially by retained earnings.

You are required to calculate cost of equity shares as well as cost of retained earnings if issue price will be ₹ 190 per share and floatation cost will be ₹ 5 per share. Dividend at the end of first year is expected to be ₹ 10 and growth rate will be $5 \%$.

Answer

$$
\begin{aligned}
\mathrm{Kr} & =\frac{\mathrm{D}_{1}}{\mathrm{P}_{0}}+\mathrm{g} \\
\mathrm{Kr} & =\frac{10}{200}+0.05 \\
\text { Ke (New Shares) } & =\frac{\mathrm{D}_{1}}{\mathrm{NP}}
\end{aligned}=\mathbf{1 0 \%}, \quad=\frac{10}{185}+0.05=\mathbf{1 0 . 4 1} \%
$$

BQ 31
The Capital structure of Vikas Ltd. is as follows:

| Sources of Fund | Book Value | Market Value |
| :--- | :---: | :---: |
| Equity Share Capital | $₹ 10,00,000$ | $₹ 20,00,000$ |
| Retained Earnings | $₹ 5,00,000$ | Nil |
| 14\% Preference Share Capital | $₹ 7,00,000$ | $₹ 7,00,000$ |
| 12\% Debentures | $₹ 6,00,000$ | $₹ 6,00,000$ |

After tax, cost of capital of these different sources is Equity share capital 18\%, Retained earnings $15 \%$, Preference share capital $14 \%$, and Debentures $8 \%$. Calculate the weighted average cost of capital of the company on the basis of (a) Book Value Weights and (b) Market Value Weights.

## Answer

(a) Statement of WACC (Book Value Weights)

| Capital Structure | Amount | Weight | Specific Cost | Cost of Capital |
| :--- | :---: | :---: | :---: | :---: |
| Equity Share Capital | $10,00,000$ | 0.357 | 0.18 | 0.0643 |
| Retained Earnings | $5,00,000$ | 0.179 | 0.15 | 0.0268 |
| 14\% Preference Share Capital | $7,00,000$ | 0.250 | 0.14 | 0.0350 |
| 12\% Debentures | $6,00,000$ | 0.214 | 0.08 | 0.0171 |
| Total | $\mathbf{2 8 , 0 0}, 000$ | $\mathbf{1 . 0 0 0}$ | WACC | $\mathbf{0 . 1 4 3 2}$ |

## (b) Statement of WACC (Market Value Weights)

| Capital Structure | Amount | Weight | Specific Cost | Cost of Capital |
| :---: | :---: | :---: | :---: | :---: |
| Equity Share Capital | $* 13,33,333$ | 0.404 | 0.18 | 0.0727 |
| Retained Earnings | $* 6,66,667$ | 0.202 | 0.15 | 0.0303 |
| 14\% Preference Share Capital | $7,00,000$ | 0.212 | 0.14 | 0.0297 |
| 12\% Debentures | $6,00,000$ | 0.182 | 0.08 | 0.0146 |
| Total | $\mathbf{3 3 , 0 0 , 0 0 0}$ | $\mathbf{1 . 0 0 0}$ | WACC | $\mathbf{0 . 1 4 7 3}$ |

*Market Value of equity has been apportioned in the ratio of Book Value of equity and retained earnings.

## BQ 32

Cost of equity of a company is $10.41 \%$ while cost of retained earnings is $10 \%$. There are 50,000 equity shares of ₹ 10 each and retained earnings of ₹ $15,00,000$. Market price per equity share is ₹ 50 .

Calculate WACC using market value weights if there is no other sources of finance.

## Answer

| Book value of paid up equity capital | $=$ | $₹ 5,00,000$ |  |
| :--- | :--- | :--- | :--- |
| Book value of retained earnings | $=$ | $₹ 15,00,000$ |  |
| Ratio Paid up equity capital \& retained earnings | $=$ | $500000: 1500000$ | $=1: 3$ |
| Market value of paid equity capital \& retained earnings | $=$ | $₹ 50,000 \times ₹ 50$ | $=₹ 25,00,000$ |
| Market value of paid up equity capital | $=$ | $₹ 25,00,000 \times 1 / 4$ | $=₹ 6,25,000$ |
| Market value of retained earnings | $=$ | $₹ 25,00,000 \times 3 / 4$ | $=₹ 18,75,000$ |

Statement of WACC (Market Value Weights)

| Capital Structure | Amount | Weight | Specific Cost | Cost of Capital |
| :---: | :---: | :---: | :---: | :---: |
| Equity Shares | $* 6,25,000$ | 0.25 | 0.1041 | 0.0260 |
| Retained Earnings | $* 18,75,000$ | 0.75 | 0.1000 | 0.0750 |
| Total | $\mathbf{2 5 , 0 0 , 0 0 0}$ | $\mathbf{1 . 0 0}$ | WACC | $\mathbf{0 . 1 0 1 0}$ |

*Market Value of equity has been apportioned in the ratio of Book Value of equity and retained earnings.

## BQ 33

The capital structure of Bombay Traders Ltd. as on 31.03.2022 is as follows:
(₹Crores)
Equity Share Capital ( 100 lakhs equity shares of $₹ 10$ each)
10
Reserves
2
$14 \%$ Debentures of $₹ 100$ each
3

For the year ended 31.03 .2023 the company is likely to pay equity dividend at $20 \%$. As the company is a market leader with good future, dividend is likely to grow by $5 \%$ every year. The equity shares are now traded at ₹ 80 per share in the stock exchange. Income-tax rate applicable to the company is $50 \%$.

## Required:

(a) The current weighted cost of capital.
(b) The company has plans to raise a further ₹ 5 crores by way of long term loan at $16 \%$ interest. When this take place the market value of the equity shares is expected to fall to ₹ 50 per share. What will be the new weighted average cost of capital of the company?
[(a) $K_{e} \mathbf{7 . 5 0 \%}, K_{r} 7.50 \%, K_{d} 7 \%, K_{o} 7.40 \%$; (b) $\left.K_{e} 9 \%, K_{r} 9 \%, K_{d} 7 \%, K_{T L} 8 \%, K_{o} 8.45 \%\right]$
BQ 34
Gamma limited has in issue 5,00,000; ₹ 1 ordinary shares whose current ex-dividend market price is ₹ 1.50 per share. The company has just paid a dividend of 27 paise per share, and dividends are expected to continue at this level for some time.

## If the company has no debt capital, compute the weighted average cost of capital?

## Answer

$$
\begin{array}{cccc}
\mathrm{K}_{\mathrm{e}}=\frac{\mathrm{D}_{1}}{\mathrm{P}_{0}}=\frac{0.27}{1.50} & =\mathbf{1 8 \%} \\
\text { Since, there is no debt capital, WACC }= & \mathrm{K}_{\mathrm{e}} & = & \mathbf{1 8} \%
\end{array}
$$

## BQ 35

Determine cost of capital using market value weights as well as book value weights using following data:

## Book value of capital structure:

| Debenture ( $₹ 1,000$ each) | $₹ 16,00,000$ |
| :--- | ---: |
| Preference Shares ( $₹ 10$ each) | $₹ 4,00,000$ |
| Equity share Capital (Shares of ₹ 100 each) | $₹ 20,00,000$ |

## Market price:

Debentures
Preference Shares
Equity Shares
₹ 1,100 each
₹ 12 each
₹200 each

Debentures carry 8 percent interest, issued at par, redeemable at par, maturity period 20 years. Flotation cost 4 percent. Preference shares carry 10 percent dividend rate, issue and redemption at par. Maturity period 15 years. Flotation cost 5 percent. Equity dividend expected at the end of the year, i.e. ₹20 per share. Anticipated growth rate in dividends is 5 percent. Corporate tax rate 55 percent.

## Answer

$$
\begin{array}{ll}
K_{d}=\frac{\mathrm{I}(1-\mathrm{t})+\left(\frac{\mathrm{RV}-\mathrm{NP}}{\mathrm{n}}\right)}{\frac{\mathrm{RV}+\mathrm{NP}}{2}} \times 100=\frac{80(1-0.55)+\left(\frac{1,000-960}{20}\right)}{\frac{1,000+960}{2}} \times 100=3.88 \% \\
K_{p}=\frac{\mathrm{PD}+\left(\frac{\mathrm{RV}-\mathrm{NP}}{\mathrm{n}}\right)}{\frac{R V+\mathrm{NP}}{2}} \times 100 & =\frac{1.00+\left(\frac{10-9.50}{15}\right)}{\frac{10+9.50}{2}} \times 100 \\
K_{e}=10.60 \% \\
& =\frac{D_{1}}{\mathrm{P}_{0}}+\mathrm{g} \\
=15 \%
\end{array}
$$

Statement of WACC (Book Value Weights)

| Capital Structure | Amount | Weight | Specific Cost | Cost of Capital |
| :--- | :---: | :---: | :---: | :---: |
| Debentures | $16,00,000$ | 0.40 | $3.88 \%$ | $1.552 \%$ |
| Preference Share Capital | $4,00,000$ | 0.10 | $10.60 \%$ | $1.06 \%$ |
| Equity Share Capital | $20,00,000$ | .050 | $15 \%$ | $7.50 \%$ |
| Total | $\mathbf{4 0 , 0 0 , 0 0 0}$ | $\mathbf{1 . 0 0}$ | WACC | $\mathbf{1 0 . 1 1 2 \%}$ |

Statement of WACC (Market Value Weights)

| Capital Structure | Amount | Weight | Specific Cost | Cost of <br> Capital |
| :--- | :---: | :---: | :---: | :---: |
| Debentures | $17,60,000$ | 0.2821 | $3.88 \%$ | $1.095 \%$ |
| Preference Share Capital | $4,80,000$ | 0.0769 | $10.60 \%$ | $0.815 \%$ |
| Equity Share Capital | $40,00,000$ | 0.6410 | $15 \%$ | $9.615 \%$ |
| Total | $\mathbf{6 2 , 4 0 , 0 0 0}$ | $\mathbf{1 . 0 0}$ | WACC | $\mathbf{1 1 . 5 2 5 \%}$ |

## BQ 36

Masco Limited wishes to raise additional finance of ₹10 lakhs for meeting its investment plans. It has $₹ 2,10,000$ in the form of retained earnings available for investment purposes. The following are further details:

Debt-equity mix
Cost of debt:
Upto ₹ $1,80,000$
beyond ₹ $1,80,000$
Current Earning per share
Dividend payout

## 3:7

10\% (before tax)
16\% (before tax)
₹4
50\% of earnings
Expected growth rate in dividend $10 \%$

Current market price per share ₹44
Tax rate

## You are required:

(a) To determine the pattern for raising the additional finance.
(b) To determine the post-tax average cost of additional debt.
(c) To determine the cost of retained earnings and cost of equity, and
(d) Compute the overall weighted average after tax cost of additional finance.
[(a) 3,00,000 Debt (1,80,000 @ 10\% and balance 1,20,000 @ 16\%) and 7,00,000 Equity (2,10,000 through retained earnings and 4,90,000 through fresh issue); (b) $K_{d} 6.2 \%$; (c) $K_{e} 15 \%, K_{r} 15 \%$; (d) $\left.K_{o} 12.36 \%\right]$
Assumption: DPS is treated at $D_{0}$.

## BQ 37

As a financial analyst of a large electronics company, you are required to determine the weighted average cost of capital of the company using (a) book value weights and (b) market value weights. The following information if available for your perusal.

## The company's present book value capital structure is:

| Debentures (₹100 per debenture) | $₹ 8,00,000$ |
| :--- | :--- |
| Preference shares (₹100 per share) | $₹ 2,00,000$ |
| Equity shares (₹10 per share) | $₹ 10,00,000$ |

## All these securities are traded in capital markets. Recent price are:

Debentures
Preference shares
Equity shares
₹110 per debenture
₹120 per share
₹22 each

## Anticipated external financing opportunities are:

(i) ₹100 per debenture redeemable at par, $11 \%$ coupon rate, $4 \%$ floatation cost, 10 years of maturity, sale price, ₹ 100 .
(ii) ₹100 per preference share redeemable at par, $12 \%$ dividend rate, $5 \%$ floatation cost, 10 years of maturity, sale price, ₹100.
(iii) Equity share has ₹2 floatation cost and sale price per share of ₹22.

In addition, the dividend expected on the equity share at the end of the year is ₹2 per share with annual growth of $7 \%$. The firm has a practice of paying all earnings in the form of dividends. Corporate Incometax rate is $35 \%$.

## Answer

(a) Calculation of Weighted Average Cost of Capital by Using Book Value Weight

| Particular | Book Value | Weight | Cost (K) | Weighted cost |
| :--- | :---: | :---: | :---: | :---: |
| 11\% Debenture | $8,00,000$ | 0.40 | $7.70 \%$ | $3.080 \%$ |
| 12\% Preference share | $2,00,000$ | 0.10 | $12.82 \%$ | $1.282 \%$ |
| Equity Share Capital | $10,00,000$ | 0.50 | $17.00 \%$ | $8.500 \%$ |
| Total | $\mathbf{2 0 , 0 0 , 0 0 0}$ | $\mathbf{1 . 0 0}$ | WACC | $\mathbf{1 2 . 8 6 2} \%$ |

(b) Calculation of Weighted Average Cost of Capital by Using Market Value Weight

| Particular | Market value | Weight | Cost (K) | Weighted cost |
| :--- | :---: | :---: | :---: | :---: |
| 11\% Debenture | $8,80,000$ | 0.265 | $7.70 \%$ | $2.041 \%$ |
| 12\% Preference share | $2,40,000$ | 0.072 | $12.82 \%$ | $0.923 \%$ |
| Equity Share Capital | $22,00,000$ | 0.663 | $17.00 \%$ | $11.271 \%$ |
| Total | $\mathbf{3 3 , 2 0 , 0 0 0}$ | $\mathbf{1 . 0 0 0}$ | WACC | $\mathbf{1 4 . 2 3 5 \%}$ |

## Working notes:

$$
\begin{array}{llll}
\mathrm{K}_{\mathrm{e}} & =\frac{\mathrm{D}_{1}}{\mathrm{P}_{0}-\mathrm{F}}+\mathrm{g} & =\frac{2}{22-2}+0.07 & =17 \% \\
\mathrm{~K}_{\mathrm{d}} & =\frac{\mathrm{I}(1-\mathrm{t})+\left(\frac{\mathrm{RV}-\mathrm{NP}}{\mathrm{n}}\right)}{\frac{\mathrm{RV}+\mathrm{NP}}{2}} \times 100 & =\frac{11(1-0.35)+\left(\frac{100-96}{10}\right)}{\frac{100+96}{2}} \times 100 & =1.70 \% \\
K_{p} & =\frac{\mathrm{PD}+\left(\frac{\mathrm{RV}-\mathrm{NP}}{\mathrm{n}}\right)}{\frac{R V+N P}{2}} \times 100 & =\frac{12+\left(\frac{100-95}{10}\right)}{\frac{100+95}{}} \times 100 & =12.82 \%
\end{array}
$$

BQ 38
Calculate the WACC using the following data by using:
(a) Book value weights
(b) Market value weights

The capital structure of the company is as under:

| Debentures (₹100 per debenture) | $₹ 5,00,000$ |
| :--- | :--- |
| Preference shares (₹100 per share) | $₹ 5,00,000$ |
| Equity shares (₹10 per share) | $₹ 10,00,000$ |

The market prices of these securities are:

Debentures
Preference shares
Equity shares
₹105 per debenture
₹ 110 per share
₹24 each

## Additional information:

(i) ₹100 per debenture redeemable at par, $10 \%$ coupon rate, $4 \%$ floatation cost, 10 years of maturity. The market price per debenture is ₹105.
(ii) ₹100 per preference share redeemable at par, 5\% coupon rate, 2\% floatation cost, 10 years of maturity.
(iii) Equity share has ₹4 floatation cost and market price per share of ₹ 24 .

The next year expected dividend is ₹1 per share with annual growth of $5 \%$. The firm has a practice of paying all earnings in the form of dividends. Corporate tax rate is $30 \%$. Use YTM method to calculate cost of debentures and preference shares.

Answer
(a) Calculation of Weighted Average Cost of Capital by Using Book Value Weight

| Particular | Book Value | Weight | Cost (K) | Weighted cost |
| :--- | :---: | :---: | :---: | :---: |
| 10\% Debenture | $5,00,000$ | 0.25 | $6.89 \%$ | $1.72 \%$ |
| 5\% Preference share | $5,00,000$ | 0.25 | $4.09 \%$ | $1.02 \%$ |
| Equity Share Capital | $10,00,000$ | 0.50 | $10.00 \%$ | $5.00 \%$ |
| Total | $\mathbf{2 0 , 0 0 , 0 0 0}$ | $\mathbf{1 . 0 0}$ | WACC | $\mathbf{7 . 7 4 \%}$ |

(b) Calculation of Weighted Average Cost of Capital by Using Market Value Weight

| Particular | Market value | Weight | Cost | Weighted cost |
| :--- | :---: | :---: | :---: | :---: |
| 10\% Debenture | $5,25,000$ | 0.151 | $6.89 \%$ | $1.04 \%$ |
| 5\% Preference share | $5,50,000$ | 0.158 | $4.09 \%$ | $0.65 \%$ |
| Equity Share Capital | $24,00,000$ | 0.691 | $10.00 \%$ | $6.90 \%$ |
| Total | $\mathbf{3 4 , 7 5 , 0 0 0}$ | $\mathbf{1 . 0 0 0}$ | WACC | $\mathbf{8 . 5 9 \%}$ |

Working notes:
(a) $K_{e}=\frac{\mathrm{D}_{1}}{\mathrm{P}_{0}-\mathrm{F}}+\mathrm{g} \quad=\quad \frac{1}{24-4}+0.05=10 \%$
(b) Cost of Debt $\left(K_{d}\right)$ :

Calculation of IRR $/ K_{d}$
$\begin{aligned} \mathrm{IRR} / \mathrm{K}_{\mathrm{d}} & =\mathrm{LR}+\frac{\mathrm{NPV}_{\mathrm{L}}}{\mathrm{NPV}_{\mathrm{L}}-\mathrm{NPV}_{\mathrm{H}}} \times(\mathrm{H}-\mathrm{L})=5 \%+\frac{14.65}{14.65-(-0.83)} \times(7 \%-5 \%) \\ & =6.89 \%\end{aligned}$

Calculation of NPV at discount rate of 5\% and 7\%

| Year | Cash Flow | Present Value |  | Present Value |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathbf{5 \%}$ | $\boldsymbol{D C F}$ | $\mathbf{7 \%}$ | $\boldsymbol{D C F}$ |
| 0 | $105-4 \%$ of 105 | 1.000 | $(100.80)$ | 1.000 | $(100.80)$ |
| $1-10$ | $10(1-0.30)$ | 7.722 | 54.05 | 7.024 | 49.17 |
| 10 | 100 | 0.614 | 61.40 | 0.508 | 50.80 |
|  |  |  | +14.65 |  | -0.83 |

(c) Cost of Preference shares $\left(K_{p}\right)$ :

Calculation of IRR/K $\boldsymbol{K}_{d}$
$\begin{aligned} \mathrm{IRR} / \mathrm{K}_{\mathrm{d}} & =\mathrm{LR}+\frac{\mathrm{NPV}_{\mathrm{L}}}{\mathrm{NPV}_{\mathrm{L}}-\mathrm{NPV}_{\mathrm{H}}} \times(\mathrm{H}-\mathrm{L})=3 \%+\frac{9.25}{9.25-(-7.79)} \times(5 \%-3 \%) \\ & =4.09 \%\end{aligned}$
Calculation of NPV at discount rate of 3\% and 5\%

| Year | Cash Flow | Present Value |  | Present Value |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathbf{3 \%}$ | DCF | $\mathbf{5 \%}$ | $\boldsymbol{D C F}$ |
| 0 | $110-2 \%$ of 110 | 1.000 | $(107.80)$ | 1.000 | $(107.80)$ |
| $1-10$ | 5 | 8.530 | 42.65 | 7.722 | 38.61 |
| 10 | 100 | 0.744 | 74.40 | 0.614 | 61.40 |
| NPV |  |  | +9.25 |  | -7.79 |

## BQ 39

Determine the cost of capital of Best Luck Limited using the book value (BV) and market value (MV) weights from the following information:

| Sources of Fund | Book Value | Market Value |
| :--- | ---: | ---: |
| Equity Shares | $₹ 1,20,00,000$ | $₹ 2,00,00,000$ |
| Retained Earnings | $₹ 30,00,000$ | Nil |
| Preference Shares | $₹ 36,00,000$ | $₹ 33,75,000$ |
| Debentures | $₹ 9,00,000$ | $₹ 10,40,000$ |

## Additional Information:

1. Equity: Equity shares are quoted at $₹ 130$ per share and a new issue priced at $₹ 125$ per share will be fully subscribed; flotation costs will be ₹5 per share.
2. Dividend: During the previous 5 years, dividends have steadily increased from ₹ 10.60 to ₹ 14.19 per share. Dividend at the end of the current year is expected to be ₹ 15 per share.
3. Preference Shares: $15 \%$ Preference shares with face value of $₹ 100$ would realise $₹ 105$ per share.
4. Debentures: The company proposes to issue 11 year $15 \%$ debentures but the yield on debentures of similar maturity and risk class is $16 \%$; flotation cost is $2 \%$.
5. Tax: Corporate tax rate is $35 \%$. Ignore dividend tax.

Floatation cost would be calculated on face value.

## Answer

(a) Calculation of Weighted Average Cost of Capital by Using Book Value Weight

| Particulars | Book Value | Weight (W) | Cost (K) | Weighted cost |
| :---: | :---: | :---: | :---: | :---: |
| Equity Shares | $₹ 1,20,00,000$ | 0.615 | 0.1850 | 0.1138 |
| Retained Earnings | $₹ 30,00,000$ | 0.154 | 0.1800 | 0.0277 |
| Preference Shares | $₹ 36,00,000$ | 0.185 | 0.1429 | 0.0264 |
| Debentures | $₹ 9,00,000$ | 0.046 | 0.1095 | 0.0050 |
| Total | $₹ 1,95,00,000$ | $\mathbf{1 . 0 0 0}$ | WACC | $\mathbf{0 . 1 7 2 9}$ |

(b) Calculation of Weighted Average Cost of Capital by Using Market Value Weight

| Particulars | Market Value | Weight (W) | Cost (K) | Weighted cost |
| :---: | :---: | :---: | :---: | :---: |
| *Equity Shares | $₹ 1,60,00,000$ | 0.655 | 0.1850 | 0.1212 |
| *Retained Earnings | $₹ 40,00,000$ | 0.164 | 0.1800 | 0.0295 |
| Preference Shares | $₹ 33,75,000$ | 0.138 | 0.1429 | 0.0197 |
| Debentures | $₹ 10,40,000$ | 0.043 | 0.1095 | 0.0047 |
| Total | $\mathfrak{F 2 , 4 4 , 1 5 , 0 0 0}$ | $\mathbf{1 . 0 0 0}$ | WACC | $\mathbf{0 . 1 7 5 1}$ |

## Working notes:

| $\mathrm{K}_{\mathrm{e}}$ | $=\frac{\mathrm{D}_{1}}{\mathrm{P}_{0}-\mathrm{F}}+\mathrm{g}$ | $=\frac{15}{125-5}+6 \%$ |
| :--- | :--- | :--- |
| g | $=\sqrt[5]{\frac{14.19}{10.60}}$ | $=6 \%$ |


| $\mathrm{K}_{\mathrm{r}}$ | = | $\frac{D_{1}}{P_{0}}+g$ | = | $\frac{15}{125}+6 \%$ | = | 18\% |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{K}_{\mathrm{d}}$ | = | $\begin{aligned} & \frac{\mathrm{I}(1-\mathrm{t})+\left(\frac{\mathrm{RV}-\mathrm{NP}}{\mathrm{n}}\right)}{\frac{\mathrm{RV}+\mathrm{NP}}{2}} \times 100 \\ & 10.95 \% \end{aligned}$ | = | $\frac{15(1-0.35)+\left(\frac{100-91.75}{11}\right)}{\frac{100+91.75}{2}}$ | 10 |  |
| $\mathrm{K}_{\mathrm{p}}$ | = | $\frac{\mathrm{PD}}{\mathrm{NP}} \times 100$ | = | $\frac{15}{105} \times 100$ | = | 14.29\% |
| MV of Debenture | = | $\frac{\text { Interest }}{\text { Market rate of Interest }}$ | $=$ | $\frac{15 \% \text { of } 100}{16 \%} \times 100$ | = | F93.75 |
| NP of Debenture | $=$ $=$ | MV of Debenture - F ₹ 93.75 - ₹ 2 ( $2 \%$ of ₹ | $\begin{gathered} \text { n Co } \\ = \end{gathered}$ | F91.75 |  |  |

*Since yield on similar type of debentures is 16 per cent, the company would be required to offer debentures at discount.

Market value of Equity Shares $=$ ₹ $2,00,00,000 \times 120 / 150=$ ₹ $1,60,00,000$
Market value of Retained Earnings $=$ ₹2,00,00,000 $\times 30 / 150=$ ₹ $40,00,000$
*Market Value of equity has been apportioned in the ratio of Book Value of equity and retained earnings.

## BQ 40

Kalyanam Ltd. has an operating profit of ₹ $34,50,000$ and has employed Debt which gives total Interest Charge of $₹ 7,50,000$. The firm has an existing Cost of Equity and Cost of Debt as $16 \%$ and $8 \%$ respectively. The firm has a new proposal before it, which requires funds of ₹ 75 Lakhs and is expected to bring an additional profit of ₹ $14,25,000$. To finance the proposal, the firm is expecting to issue an additional debt at $8 \%$ and will not be issuing any new equity shares in the market. Assume no tax culture.

## You are required to calculate the Weighted Average Cost of Capital (WACC) of Kalyanam Ltd.:

(a) Before the new Proposal
(b) After the new Proposal.

## Answer

(1) Value of Debt

$$
\begin{aligned}
& =\quad \frac{\text { Interest }}{\text { Cost of debt }\left(\mathrm{K}_{\mathrm{d}}\right)} \quad=\quad \frac{7,50,000}{8 \%} \\
& =\text { ₹93,50,000 }
\end{aligned}
$$

(2) Value of Equity Capital

$$
\begin{aligned}
& =\quad \frac{\text { Operating Profit }- \text { Interest }}{\text { Cost of equity }\left(\mathrm{K}_{\mathrm{e}}\right)}=\frac{34,50,000-7,50,000}{16 \%} \\
& =\quad \text { ₹1,68,75,000 }
\end{aligned}
$$

## (3) New cost of Equity after proposal:

$$
\begin{aligned}
& =\frac{\text { Operating Profit }- \text { Interest }}{\text { Equity Capital }} \\
& =\frac{34,50,000+14,25,000-7,50,000-8 \% \text { of } 75,00,000}{1,68,75,000}=20.90 \%
\end{aligned}
$$

(a) Calculation of WACC Before the New Proposal

| Particulars | Book Value | Weight (W) | Cost (K) | Weighted cost |
| :---: | :---: | :---: | :---: | :---: |
| Equity Shares | $₹ 1,68,75,000$ | 0.6429 | 0.16 | 0.1029 |
| Debt | $₹ 93,75,000$ | 0.3571 | 0.08 | 0.0286 |
| Total | $₹ 2,62,50,000$ | $\mathbf{1 . 0 0 0}$ | WACC | $\mathbf{0 . 1 3 1 5}$ |

(b) Calculation of WACC After the New Proposal

| Particulars | Book Value | Weight (W) | Cost (K) | Weighted cost |
| :---: | :---: | :---: | :---: | :---: |
| Equity Shares | $₹ 1,68,75,000$ | 0.5 | 0.209 | 0.1045 |
| Debt (₹93,75,000 + ₹75,00,000) | $₹ 1,68,75,000$ | 0.5 | 0.080 | 0.0400 |
| Total | $₹ 3,37,50,000$ | $\mathbf{1 . 0}$ | WACC | $\mathbf{0 . 1 4 4 5}$ |

## MARGINAL WEIGHTED AVERAGE COST OF CAPITAL (MACC)

## BQ 41

Bulldog Ltd. has a debt of $14 \%$ in the past. It can raise a fresh debt at $12.5 \%$. The company is in a tax bracket of $35 \%$. Bulldog Ltd. plans to follow dividend discount model to estimate the cost of equity. The company plans to pay ₹ 4 per share as dividends in the next year. The DPS of the company is expected to grow at the rate of $8 \%$ p.a. The current MPS of the company's equity shares is ₹ 40 .

You are required to compute the marginal weighted average cost of capital if the target debt to value ratio of the company is $20 \%$.

## Answer

$$
\text { Marginal WACC } \quad=\quad K_{e} W_{e}+K_{d} W_{d}=18 \% \times 0.80+8.125 \% \times 0.20=\mathbf{1 6 . 0 2 5} \%
$$

## Calculation of Marginal $K_{e}$ and $K_{d}$

| $\mathrm{K}_{\mathrm{e}}$ | $=\frac{\mathrm{D}_{1}}{\mathrm{P}_{0}}+\mathrm{g}$ | $=\frac{4}{40}+.08$ | $=18 \%$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{~K}_{\mathrm{d}}$ | $=$ | $\mathrm{I}(1-\mathrm{t})$ | $=$ |
|  |  | $12.50 \%(1-0.35)$ | $=$ |

BQ 42
ABC Ltd. has the following capital structure, which is considered to be optimum at on 31st March, 2022:
14\% debenture
₹ 30,000
$11 \%$ preference share capital
₹10,000
Equity share capital ( 10,000 shares)
₹ $1,60,000$

The company's share has a current market price of ₹ 23.60 per share. The expected dividend per share in next year is 50 percent of the 2021 EPS. The EPS of last 10 years is as follows. The past trends are expected to continue:

| Year | 2012 | 2013 | 2014 | 2015 | 2016 | 2017 | 2018 | 2019 | 2020 | 2021 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| EPS (₹) | 1.00 | 1.10 | 1.21 | 1.33 | 1.46 | 1.61 | 1.77 | 1.95 | 2.15 | 2.36 |

The company issued new debentures carrying $16 \%$ rate of interest and the current market price of debenture is ₹96. Preference shares ₹ 9.20 (with dividend of ₹ 1.1 per share) were also issued. The company is in $50 \%$ tax bracket.
(i) Calculate the after tax (a) Cost of New Debts, (b) Cost of New Preference Share, and (c) Cost of New Equity Share (assuming new equity from retained earnings).
(ii) Calculate the marginal cost of capital when no new share was issued.
(iii) Determine the amount that can be spent for capital investment before new ordinary shares must be sold. Assuming that retained earnings for next year's investment are $50 \%$ of 2021.
(iv) Compute marginal cost of capital when the fund exceeds the amount calculated in (iii), assuming new equity is issued at ₹ 20 per share?

## Answer

(i) (a) After tax cost of new debt

$$
\mathrm{K}_{\mathrm{d}}=\frac{\mathrm{I}(1-\mathrm{t})}{\mathrm{NP}} \times 100=\frac{16(1-.50)}{96} \times 100=8.33 \%
$$

(b) After tax cost of new preference shares

$$
\mathrm{K}_{\mathrm{p}} \quad=\frac{\mathrm{PD}}{\mathrm{NP}} \times 100 \quad=\frac{1.10}{9.20} \times 100=11.96 \%
$$

(c) Cost of new equity or cost of retained earnings

$$
\mathrm{K}_{\mathrm{r}} \quad=\frac{\mathrm{D}_{1}}{\mathrm{P}_{0} \text { (old) }}+\mathrm{g} \quad=\quad \frac{2.36 \times 50 \%}{23.60}+0.10=15 \%
$$

(ii) MCC (Kon when no new equity share was issued:
$\mathrm{K}_{\mathrm{d}} \mathrm{W}_{\mathrm{d}}+\mathrm{K}_{\mathrm{p}} \mathrm{W}_{\mathrm{p}}+\mathrm{K}_{\mathrm{r}} \mathrm{W}_{\mathrm{r}}=8.33 \% \times .15+11.96 \% \times .05+15 \% \times .80=13.85 \%$
(iii) The company can pay the following amount before issue of new shares:

Equity (retained earnings in this case) $=80 \%$ of the total capital
Therefore, investment before new issue $=\frac{11,800}{80 \%}=₹ \mathbf{1 4 , 7 5 0}$
Retained earnings $=₹ 2.36 \times 50 \% \times 10,000=₹ 11,800$
(iv) MCC ( $K_{o}$ ) when funds exceeds $₹ 14,750$
$\mathrm{K}_{\mathrm{d}} \mathrm{W}_{\mathrm{d}}+\mathrm{K}_{\mathrm{p}} \mathrm{W}_{\mathrm{p}}+\mathrm{K}_{\mathrm{e}} \mathrm{W}_{\mathrm{e}}=\quad 8.33 \% \times .15+11.96 \% \times .05+15.90 \% \times .80=\mathbf{1 4 . 5 7} \%$
If the company pay more than ₹ 14,750 , it will have to issue new shares. The cost of new issue of ordinary share is:

$$
\mathrm{K}_{\mathrm{e}} \quad=\quad \frac{\mathrm{D}_{1}}{\mathrm{P}_{0}(\text { new })}+\mathrm{g} \quad=\frac{1.18}{20}+0.10 \quad=15.90 \%
$$

## WN: Calculation of growth:

Growth from year 2012 to $2013=(1.10-1.00) \div 1.00=10 \%$
[Same rate of growth is found in future years]

## BQ 43

M/s Navya Corporation has a capital structure of $40 \%$ debt and $60 \%$ equity. The company is presently considering several alternative investment proposals costing less than ₹ $20,00,000$. The corporation always raises the required funds without disturbing its present debt equity ratio. The cost of raising the debt and equity are as under:

| Project cost | Cost of debt | Cost of equity |
| :--- | :---: | :---: |
| Upto ₹2,00,000 | $10 \%$ | $12 \%$ |
| Above ₹2,00,000 \& upto ₹5,00,000 | $11 \%$ | $13 \%$ |
| Above ₹5,00,000 \& upto ₹10,00,000 | $12 \%$ | $14 \%$ |
| Above ₹10,00,000 \& upto ₹20,00,000 | $13 \%$ | $14.5 \%$ |

Assuming tax rate at $50 \%$, calculate:
(a) Cost of capital of two projects X and Y whose funds requirements are ₹ $6,50,000$ and $₹ 14,00,000$ respectively.
(b) If a project is expected to give after tax return of $10 \%$, determine under what conditions it would be acceptable?

## Answer

(a) Statement Showing Weighted Average Cost of Capital

| Project cost | Financing | Weight (W) | Cost (K) | Weighted cost |
| :---: | :---: | :---: | :---: | :---: |
| Upto ₹ $2,00,000$ | Debt Equity | $\begin{aligned} & 0.4 \\ & 0.6 \end{aligned}$ | $\begin{gathered} 10 \%(1-0.50)=5 \% \\ 12 \% \end{gathered}$ | 2.00\% |
|  |  |  |  | 7.20\% |
|  |  |  |  | 9.20\% |
| Above ₹2,00,000 \& upto ₹5,00,000 | Debt Equity | $\begin{aligned} & \hline 0.4 \\ & 0.6 \end{aligned}$ | $\begin{gathered} 11 \%(1-0.50)=5.5 \% \\ 13 \% \end{gathered}$ | 2.20\% |
|  |  |  |  | 7.80\% |
|  |  |  |  | 10.00\% |
| Above ₹5,00,000 \& upto ₹ $10,00,000$ | Debt Equity | $\begin{aligned} & \hline 0.4 \\ & 0.6 \end{aligned}$ | $\begin{gathered} 12 \%(1-0.50)=6 \% \\ 14 \% \end{gathered}$ | 2.40\% |
|  |  |  |  | 8.40\% |
|  |  |  |  | 10.80\% |
| Above ₹ $10,00,000$ \& upto ₹20,00,000 | Debt Equity | $\begin{aligned} & \hline 0.4 \\ & 0.6 \end{aligned}$ | $\begin{gathered} 13 \%(1-0.50)=6.5 \% \\ 14.50 \% \end{gathered}$ | 2.60\% |
|  |  |  |  | 8.70\% |
|  |  |  |  | 11.30\% |


| Project | Fund requirement | Cost of capital |
| :--- | :---: | :---: |
| Project X | $₹ 6,50,000$ | $10.80 \%$ |
| Project Y | $₹ 14,50,000$ | $11.30 \%$ |

(b) If a project is expected to give after tax return of $10 \%$, it would be acceptable provided its cost does not exceeds $5,00,000$ or, after tax return should be more than or at least equal to the weighted average cost of capital.

## PAST YEAR QUESTIONS

## PYQ 1

The following details are provided by GPS Limited:

| Equity Share capital | $₹ 65,00,000$ |
| :--- | :--- |
| $12 \%$ Preference Share Capital | $₹ 12,00,000$ |
| $15 \%$ Redeemable Debentures | $₹ 20,00,000$ |
| $10 \%$ Convertible Debentures | $₹ 8,00,000$ |

The cost of equity capital for the company is $16.30 \%$ and Income Tax rate for the company is $30 \%$.
You are required to calculate the Weighted Average Cost of Capital (WACC) of the company.
[(5 Marks) May 2014]
Answer

$$
\begin{aligned}
\text { WACC } & =\mathrm{K}_{\mathrm{e}} \mathrm{~W}_{\mathrm{e}}+\mathrm{K}_{\mathrm{p}} \mathrm{~W}_{\mathrm{p}}+\mathrm{K}_{\mathrm{rd}} \mathrm{~W}_{\mathrm{rd}}+\mathrm{K}_{\mathrm{cd}} \mathrm{~W}_{\mathrm{cd}} \\
& =16.30 \% \times \frac{65}{105}+12 \% \times \frac{12}{105}+10.50 \% \times \frac{20}{105}+7 \% \times \frac{8}{105}=13.9952 \%
\end{aligned}
$$

## Working Notes:

(i) Calculation of cost of Preference Share Capital ( $K_{p}$ ):
$\mathrm{K}_{\mathrm{p}}=$ Rate of Preference Dividend $=12 \%$
(ii) Calculation of cost of Redeemable Debentures ( $K_{r d}$ ):
$\mathrm{K}_{\mathrm{rd}}=\mathrm{I}(1-\mathrm{t})=15 \%(1-0.30)=\mathbf{1 0 . 5 0} \%$

## (iii) Calculation of cost Convertible Debentures ( $K_{c d}$ ):

$\mathrm{K}_{\mathrm{cd}}=\mathrm{I}(1-\mathrm{t})=10 \%(1-0.30)=7 \%$

## PYQ 2

A Ltd. wishes to raise additional finance of ₹ 30 lakhs for meeting its investment plans. The company has ₹ $6,00,000$ in the form of retained earnings available for investment purposes. The following are the further details:

Debt equity ratio : $30: 70$
Cost of debt:
Upto ₹3,00,000
Beyond ₹3,00,000
Earning per share :
Dividend payout :
Expected growth rate :
Current market price :
Company's tax rate :
Shareholder's personal tax rate : 20\%.

## You are required to:

1. Calculate the post tax average cost of additional debt.
2. Calculate the cost of retained earnings and cost of equity.
3. Calculate the overall weighted average (after tax) cost of additional finance.
[(8 Marks) May 2015]

## Answer

Total capital required is ₹30 lakhs. With a debt - equity ratio of $30: 70$. It means ₹9 lakhs is to be raised through debt and ₹21 lakhs through equity. Out of ₹21 lakhs, ₹6 lakhs are available in the form of retained earnings hence $₹ 15$ lakhs will have to raise by issuing equity shares.

## 1. Post tax average cost of additional debt:

| $\mathrm{K}_{\mathrm{d} 1}$ | $=$ | $\mathrm{I}(1-\mathrm{t})$ | $=$ | $11 \%(1-0.30)$ |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{K}_{\mathrm{d} 2}$ | $=$ | $=$ | $\mathbf{7 . 7 0 \%}$ |  |
| Average $\mathrm{K}_{\mathrm{d}}(1-\mathrm{t})$ | $=$ | $\mathrm{K}_{\mathrm{d} 1} \mathrm{~W}_{\mathrm{d} 1}+\mathrm{K}_{\mathrm{d} 2} \mathrm{~W}_{\mathrm{d} 2}$ | $=$ | $14 \%(1-0.30)$ |
|  |  |  |  | $9.8 \% \times \frac{3}{9}+9.8 \% \times \frac{6}{9}$ |

2. Cost of retained earning \& cost of equity:

| $\mathrm{K}_{\mathrm{e}}$ | $=\frac{\mathrm{D}_{1}}{\mathrm{P}_{0}}+\mathrm{g}$ | $=\frac{10.50+10 \%}{90}+0.10$ | $=22.83 \%$ |
| ---: | :--- | ---: | :--- |
| $\mathrm{~K}_{\mathrm{r}}$ | $=\mathrm{K}(1-\mathrm{PT})$ | $=\mathrm{F})$ |  |
| $\mathrm{D}_{0}$ | $=22.83 \%(1-.20)$ | $=18.27 \%$ |  |

## 3. Overall cost of additional finance:

$\mathrm{K}_{0}$

$$
\begin{array}{lll}
= & \mathrm{K}_{\mathrm{e}} \mathrm{~W}_{\mathrm{e}}+\mathrm{K}_{\mathrm{r}} \mathrm{~W}_{\mathrm{r}}+\mathrm{K}_{\mathrm{d}} \mathrm{~W}_{\mathrm{d}} & \\
= & 22.83 \% \times \frac{15}{30}+18.27 \% \times \frac{6}{30}+9.10 \% \times \frac{9}{30} \quad 17.80 \%
\end{array}
$$

Assumption: DPS $₹ 10.50$ is treated at $D_{o}$.

## PYQ 3

A company issues $25,000,14 \%$ debentures of $₹ 1,000$ each. The debentures are redeemable after the expiry period 5 years. Tax rate applicable to the company is $35 \%$.

Calculate the cost of debt after tax if debentures are issued at 5\% discount with 2\% flotation cost.
[(5 Marks) Nov 2015]

## Answer

$$
\begin{aligned}
\mathrm{K}_{\mathrm{d}} & =\frac{\mathrm{I}(1-\mathrm{t})+\left(\frac{\mathrm{RV}-\mathrm{NP}}{\mathrm{n}}\right)}{\frac{\mathrm{RV}+\mathrm{NP}}{2}} \times 100=\frac{140(1-0.35)+\left(\frac{1000-930}{5}\right)}{\frac{1000+930}{2}} \times 100 \\
& =10.88 \% \\
\text { Net Proceeds } & =1,000-5 \% \text { Discount }-2 \% \text { Flotation cost }=930
\end{aligned}
$$

Note: Floatation cost has been calculated on the basis of face value (i.e. 2\% of ₹ 1,000 or ₹ 950 whichever is higher).

## PYQ 4

The X Company has following capital structure at 31 ${ }^{\text {st }}$ March, 2015, which is considered to be optimum:

| $14 \%$ debenture | $₹ 3,00,000$ |
| :--- | :--- |
| $11 \%$ preference share capital | $₹ 1,00,000$ |
| Equity share capital $(1,00,000$ shares $)$ | $₹ 16,00,000$ |

The company's share has a current market price of ₹ $23 . .60$ per share. The expected dividend per share in next year is 50 percent of the 2015 EPS. The EPS of last 10 years is as follows. The past trends are expected to continue:

| Year | 2006 | 2007 | 2008 | 2009 | 2010 | 2011 | 2012 | 2013 | 2015 | 2015 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| EPS (₹) | 1.00 | 1.10 | 1.21 | 1.33 | 1.46 | 1.61 | 1.77 | 1.95 | 2.15 | 2.36 |

The company issued new debentures carrying 16\% rate of interest and the current market price of debenture is ₹96. Preference shares ₹ 9.20 (with dividend of ₹ 1.1 per share) were also issued. The company is in $50 \%$ tax bracket.
(i) Calculate the after tax cost of (a) New Debts, (b) New Preference Share, and (c) New Equity Share (assuming new equity from retained earnings).
(ii) Calculate the marginal cost of capital when no new share was issued.
(iii) How much can be spent for capital investment before new ordinary shares must be sold? Assuming that retained earnings for next year's investment are $50 \%$ of 2015.
(iv) What will be marginal cost of capital when the fund exceeds the amount calculated in (iii), assuming new equity is issued at ₹ 20 per share?
[(8 Marks) May 2016]

## Answer

(i) (a) After tax cost of new debt

$$
\mathrm{K}_{\mathrm{d}} \quad=\frac{\mathrm{I}(1-\mathrm{t})}{\mathrm{NP}} \times 100=\frac{16(1-.50)}{96} \times 100=8.33 \%
$$

(b) After tax cost of new preference shares

$$
\mathrm{K}_{\mathrm{p}}=\frac{\mathrm{PD}}{\mathrm{NP}} \times 100=\frac{1.10}{9.20} \times 100=11.96 \%
$$

(a) Cost of new equity or cost of retained earnings

$$
\mathrm{K}_{\mathrm{r}} \quad=\frac{\mathrm{D}_{1}}{\mathrm{P}_{0} \text { (old) }}+\mathrm{g}=\frac{2.36 \times 50 \%}{23.60}+0.10=\mathbf{1 5 \%}
$$

(ii) MCC (K) when no new equity share was issued:

$$
\mathrm{K}_{\mathrm{d}} \mathrm{~W}_{\mathrm{d}}+\mathrm{K}_{\mathrm{p}} \mathrm{~W}_{\mathrm{p}}+\mathrm{K}_{\mathrm{r}} \mathrm{~W}_{\mathrm{r}}=8.33 \% \times .15+11.96 \% \times .05+15 \% \times .80=13.85 \%
$$

(iii) The company can pay the following amount before issue of new shares:

Equity (retained earnings in this case) $=80 \%$ of the total capital

| Therefore, investment before new issue | $=\frac{1,18,000}{80 \%}$ | $=\mathfrak{₹} \mathbf{1 , 4 7 , 5 0 0}$ |
| :--- | :--- | :--- |
| Retained earnings | $=₹ 2.36 \times 50 \% \times 1,00,000$ | $=\mathfrak{₹} \mathbf{1 , 1 8 , 0 0 0}$ |

(iv) MCC (Kon when funds exceeds $\mathfrak{₹} 1,47,500$
$\mathrm{K}_{\mathrm{d}} \mathrm{W}_{\mathrm{d}}+\mathrm{K}_{\mathrm{p}} \mathrm{W}_{\mathrm{p}}+\mathrm{K}_{\mathrm{e}} \mathrm{W}_{\mathrm{e}}=\quad 8.33 \% \times .15+11.96 \% \times .05+15.90 \% \times .80=\mathbf{1 4 . 5 7} \%$

If the company pay more than $₹ 1,47,500$, it will have to issue new shares. The cost of new issue of ordinary share is:

$$
\mathrm{K}_{\mathrm{e}} \quad=\quad \frac{\mathrm{D}_{1}}{\mathrm{P}_{0} \text { (new) }}+\mathrm{g} \quad=\quad \frac{1.18}{20}+0.10 \quad=15.90 \%
$$

## WN: Calculation of growth:

Growth from year 2006 to $2007=(1.10-1.00) \div 1.00=10 \%$
[Same rate of growth is found in future years]

## PYQ 5

ABC Company’s equity share is quoted in the market at ₹ 25 per share currently. The company pays a dividend of ₹ 2 per share and the investor's market expects a growth rate of $6 \%$ per year.

## You are required to:

(i) Calculate the company's cost of equity capital.
(ii) If the anticipated growth rate is $8 \%$ per annum, calculate the indicated market price per share.
(iii) If the company issues $10 \%$ debentures of face value of ₹ 100 each and realises ₹ 96 per debenture while the debentures are redeemable after 12 years at a premium of $12 \%$, what will be the cost of debenture? Assume Tax Rate to be 50\%.
[(5 Marks) Nov 2016]

## Answer

(i) $\quad \mathrm{K}_{\mathrm{e}} \quad=\frac{\mathrm{D}_{1}}{\mathrm{P}_{0}}+\mathrm{g}$
$=\quad \frac{2}{25}+0.06$
$=14 \%$

Note: The cost of equity can be calculated with taking the effect of growth on dividend (i.e. $\mathrm{D}_{1}=2.12$ ).
(ii) $\mathrm{P}_{\mathrm{o}}=\frac{\mathrm{D}_{1}}{\mathrm{Ke}-\mathrm{g}}$

$$
=\quad \frac{2}{14 \%-8 \%} \quad=\quad \text { F33.33 }
$$

(iii) $\mathrm{K}_{\mathrm{d}}=\frac{\mathrm{I}(1-\mathrm{t})+\left(\frac{\mathrm{RV}-\mathrm{NP}}{\mathrm{n}}\right)}{\frac{\mathrm{RV}+\mathrm{NP}}{2}} \times 100=\frac{10(1-0.50)+\left(\frac{112-96}{12}\right)}{\frac{112+96}{2}} \times 100$

## PYQ 6

Following is the capital structure of RBT Ltd. As on 31st March 2016:

| Equity Share of ₹10 each | ₹50,00,000 | ₹ $1,05,00,000$ |
| :--- | :---: | :---: |
| Retained Earnings | ₹ $13,00,000$ | Nil |
| $11 \%$ Preference Share of ₹100 each | $₹ 7,00,000$ | $₹ 9,00,000$ |
| $14 \%$ Debentures of ₹100 each | $₹ 30,00,000$ | $₹ 36,00,000$ |

Market price of equity shares is ₹ 40 per share and it is expected that a dividend of ₹ 4 per share would be declared. The dividend per share is expected to grow at the rate of $8 \%$ every year. Income tax rate applicable to the company is $40 \%$ and shareholder's personal income tax rate is $20 \%$.

## You are required to calculate:

(i) Cost of capital for each source of capital,
(ii) Weighted average cost of capital on the basis of book value weights,
(iii) Weighted average cost of capital on the basis of market value weights.
[(8 Marks) Nov 2016]

## Answer

(i) Calculation of cost of capital for each source of capital:

| $\mathrm{K}_{\mathrm{e}}$ | = | $\frac{D_{1}}{P_{0}}+g$ | = | $\frac{4}{40}+0.08$ | = | 18\% |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{K}_{\mathrm{r}}$ | = | $\mathrm{K}_{\mathrm{e}}(1-\mathrm{PT})$ | = | 18\% ( $1-0.20$ ) | = | 14.40\% |
| $\mathrm{K}_{\mathrm{d}}$ | = | $\mathrm{I}(1-\mathrm{t})$ | = | 14\% ( $1-0.40$ ) | = | 8.40\% |
| K | = | Rate of PD | = | 11\% |  |  |

(ii) Calculation of WACC ( $K_{o}$ ) using book value proportions

| Name of Source | Amount | Proportion | $\boldsymbol{K}$ | $\boldsymbol{K}_{\boldsymbol{o}}$ |
| :--- | :---: | :---: | :---: | :---: |
| Equity Share Capital | $50,00,000$ | 0.50 | $18 \%$ | $9.00 \%$ |
| Retained Earnings | $13,00,000$ | 0.13 | $14.40 \%$ | $1.87 \%$ |
| Preference Share Capital | $7,00,000$ | 0.07 | $11 \%$ | $0.77 \%$ |
| Debentures | $30,00,000$ | 0.30 | $8.40 \%$ | $2.52 \%$ |
| Total | $\mathbf{1 , 0 0 , 0 0 , 0 0 0}$ | $\mathbf{1 . 0 0}$ | WACC | $\mathbf{1 4 . 1 6 \%}$ |

(iii) Calculation of WACC ( $K_{o}$ ) using market value proportions

| Name of Source | Amount | Proportion | $\boldsymbol{K}$ | $\boldsymbol{K}_{\boldsymbol{o}}$ |
| :--- | :---: | :---: | :---: | :---: |
| Equity Share Capital | $83,33,333$ | 0.555 | $18 \%$ | $9.99 \%$ |
| Retained Earnings | $21,66,667$ | 0.145 | $14.40 \%$ | $2.09 \%$ |
| Preference Share Capital | $9,00,000$ | 0.060 | $11 \%$ | $0.66 \%$ |
| Debentures | $36,00,000$ | 0.240 | $8.40 \%$ | $2.02 \%$ |
| Total | $\mathbf{1 , 5 0 , 0 0 , 0 0 0}$ | $\mathbf{1 . 0 0 0}$ | $\boldsymbol{W A C C}$ | $\mathbf{1 4 . 7 6 \%}$ |


| Market value of Equity Share Capital $=$ | $₹ 1,05,00,000 \times 50 / 63=$ | $₹ 83,33,333$ |
| :--- | :--- | :--- | :--- |
| Market value of Retained Earnings | $=\quad ₹ 1,05,00,000 \times 13 / 63=$ | $₹ 21,66,667$ |

*Market Value of equity has been apportioned in the ratio of Book Value of equity and retained earnings.

## PYQ 7

JC Ltd. is planning an equity issue in current year. It has an earning per share (EPS) of ₹ 20 and proposes to pay $60 \%$ dividend at the current year end with a P/E ratio 6.25 , it wants to offer the issue at market price. The flotation cost is expected to be $4 \%$ of the issue price.

You are required to determine rate of return for equity share (cost of equity) before the issue and after the issue.
[(5 Marks) May 2018]

| Answer |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Market price of share ( $\mathrm{P}_{0}$ ) | $=$ | EPS $\times$ PE | = | ₹ $20 \times 6.25$ | = | ₹125 |
| Net proceeds | $=$ | 125-4\% |  |  | = | ₹120 |
| Return on Equity (ROE) | = | 1/PE | = | 1/6.25 | = | 16\% |
| Growth rate | $=$ | $\mathrm{r} \times \mathrm{b}$ | = | 16\% $\times 40 \%$ | = | 6.40\% |
| $\mathrm{K}_{\mathrm{e}}$ (before issue) | $=$ | $\frac{\mathrm{D}_{1}}{\mathrm{P}_{0}}+\mathrm{g}$ | = | $\frac{60 \% \text { of } 20}{125}+6.40 \%$ | = | 16\% |
| $\mathrm{K}_{\text {e }}$ (after issue) | $=$ | $\frac{\mathrm{D}_{1}}{\mathrm{NP}}+\mathrm{g}$ | = | $\frac{60 \% \text { of } 20}{120}+6.40 \%$ | = | 16.40\% |

## PYQ 8

Alpha Ltd. has furnished the following information:

| Earning per share (EPS) | $:$ | ₹4.00 |
| :--- | :--- | :--- |
| Dividend payout ratio | $:$ | $25 \%$ |
| Market price per share | $:$ | $₹ 50$ |
| Rate of tax | $:$ | $30 \%$ |
| Growth rate of dividend | $:$ | $10 \%$ |

The company wants to raise additional capital of ₹ 10 lakhs including debt of ₹ 4 lakhs. The cost of debt (before tax) is $10 \%$ upto ₹ 2 lakhs and $15 \%$ beyond that.

Compute the after tax cost equity and debt and the weighted average cost of capital.
[(5 Marks) May 2019]

## Answer

| Ke | = | $\frac{\mathrm{D}_{1}}{\mathrm{P}_{0}}+\mathrm{g}$ | $=$ | $\frac{4.00 \times 25 \% \times 110 \%}{50}+0.10$ | = | 12.20\% |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{K}_{\mathrm{d} 1}$ | = | I ( $1-\mathrm{t}$ ) | = | 10\% (1-0.30) | = | 7\% |
| $\mathrm{K}_{\text {d2 }}$ | = | I (1-t) | = | 15\% (1-0.30) | = | 10.50\% |
| K | = | $\mathrm{K}_{\mathrm{e}} \mathrm{W}_{\mathrm{e}}+\mathrm{K}_{\mathrm{d} 1} \mathrm{~W}_{\mathrm{d} 1}+\mathrm{K}_{\mathrm{d} 2} \mathrm{~W}_{\mathrm{d} 2}$ |  |  |  |  |
|  | = | $12.20 \% \times \frac{6}{10}+7 \% \times \frac{2}{10}+10.50 \% \times \frac{2}{10}$ |  |  | = | 10.82\% |

## PYQ 9

A company wants to raise additional finance of ₹5 crore in next year. The company expected to retain
$₹ 1$ crore in next year. Further details are as follows:
(i) The amount will be raised by equity and debt in the ratio of $3: 1$.
(ii) The additional issue of equity shares will result in price per share being fixed at ₹ 25 .
(iii) The debt capital raised by way of term loan will cost $10 \%$ for the first ₹ 75 lakh and $12 \%$ for the next ₹50 lakh.
(iv) The net expected dividend on equity shares is ₹ 2.00 per share. The dividend is expected to grow at the rate of $5 \%$.
(v) Income tax rate of $25 \%$.

## You are required:

(a) To determine the amount of equity and debt for raising additional finance.
(b) To determine the post tax average cost of additional debt.
(c) To determine the cost of retained earning and cost of equity.
(d) To compute the overall weighted average cost of additional finance after tax.
[(10 Marks) Nov 2019]

## Answer

(a) Total capital required is ₹ 5 crore. With a debt-equity ratio of $1: 3$. It means $₹ 1.25$ crore is to be raised through debt and ₹ 3.75 crores through equity. Out of ₹ 3.75 crore, ₹ 1 crore are available in the form of retained earnings hence ₹ 2.75 crore will have to raise by issuing equity shares.
(b) Post tax average cost of additional debt:

| $\mathrm{K}_{\mathrm{d} 1}$ | $=\mathrm{I}(1-\mathrm{t})$ | $=10 \%(1-0.25)$ | $=$ | $\mathbf{7 . 5} \%$ |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{~K}_{\mathrm{d} 2}$ | $=\mathrm{I}(1-\mathrm{t})$ | $=12 \%(1-0.25)$ | $=$ | $\mathbf{9 \%}$ |
| Average $\mathrm{K}_{\mathrm{d}}$ | $=\mathrm{K}_{\mathrm{d} 1} \mathrm{~W}_{\mathrm{d} 1}+\mathrm{K}_{\mathrm{d} 2} \mathrm{~W}_{\mathrm{d} 2}$ | $=$ | $7.5 \% \times \frac{75}{125}+9 \% \times \frac{50}{125}$ | $=$ |

(c) Cost of retained earning \& cost of equity:

$$
\begin{array}{rlrl}
\mathrm{K}_{\mathrm{e}} & =\frac{\mathrm{D}_{1}}{\mathrm{P}_{0}}+\mathrm{g} & =\frac{2}{25}+0.05 & =13 \% \\
\mathrm{~K}_{\mathrm{r}} & =\mathrm{K}_{\mathrm{e}} & =13 \%
\end{array}
$$

(d) Overall cost of additional finance:
$\mathrm{K}_{\mathrm{o}} \quad=\quad \mathrm{K}_{\mathrm{e}} \mathrm{W}_{\mathrm{e}}+\mathrm{K}_{\mathrm{r}} \mathrm{W}_{\mathrm{r}}+\mathrm{K}_{\mathrm{d}} \mathrm{W}_{\mathrm{d}}$
$=13 \% \times \frac{275}{500}+13 \% \times \frac{100}{500}+8.10 \% \times \frac{125}{500} \quad=11.78 \%$

## PYQ 10

TT Ltd. issued $20,000,10 \%$ Convertible debentures of ₹ 100 each with a maturity period of 5 years. At maturity the debenture holders will have the option to convert the debentures into equity shares of the company in the ratio of $1: 5$ ( 5 shares for each debenture). The current market price of the equity shares is ₹20 each and historically the growth rate of the shares are $4 \%$ per annum. Assuming tax rate is $25 \%$.

Compute the cost of 10\% debentures using Approximation Method and Internal Rate of Return Method.

## PV Factor are as under:

| Year | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| PV Factor @ 10\% | 0.909 | 0.826 | 0.751 | 0.683 | 0.621 |
| PV Factor @ 15\% | 0.870 | 0.756 | 0.658 | 0.572 | 0.497 |

[(5 Marks) Nov 2020]
Answer
(a) Calculation of Cost of Convertible debenture using Approximation Method:

$$
\mathrm{K}_{\mathrm{d}}=\frac{\mathrm{I}(1-\mathrm{t})+\frac{\mathrm{CV}-\mathrm{NP}}{\mathrm{n}}}{\frac{\mathrm{CV}+\mathrm{NP}}{2}} \times 100=\frac{10(1-0.25)+\frac{121.67-100}{5}}{\frac{121.67+100}{2}} \times 100=10.68 \%
$$

(b) Calculation of Cost of Convertible debenture using IRR Method

Calculation of NPV at two discount rates:

| Year | Cash Flow | Present Value |  | Present Value |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathbf{1 0} \%$ | $\boldsymbol{D C F}$ | $\mathbf{1 5 \%}$ | $\boldsymbol{D C F}$ |
| 0 | $(100)$ | 1.000 | $(100)$ | 1.000 | $(100)$ |
| $1-5$ | 7.50 | 3.790 | 28.43 | 3.353 | 25.15 |
| 5 | 121.67 | 0.621 | 75.56 | 0.497 | 60.47 |
| NPV |  |  | $\mathbf{+ 3 . 9 9}$ |  | $\mathbf{- 1 4 . 3 8}$ |

$$
\begin{aligned}
\mathrm{IRR} / \mathrm{K}_{\mathrm{d}} & =\mathrm{LR}+\frac{\mathrm{NPV}_{\mathrm{L}}}{\mathrm{NPV}_{\mathrm{L}}-\mathrm{NPV}_{\mathrm{H}}} \times(\mathrm{H}-\mathrm{L})=10 \%+\frac{3.99}{3.99-(-14.38)} \times(15 \%-10 \%) \\
& =11.09 \%
\end{aligned}
$$

## Determination of Convertible value:

Higher of:
(i) The cash value of debentures $=$ ₹ 100
(ii) Value of equity shares $\begin{aligned}= & 5 \text { shares } \times ₹ 20(1+0.04)^{5}= \\ & =5 \text { shares } \times ₹ 24.333=\end{aligned}$
₹ 121.67 will be taken as redemption value as it is higher than the cash option and attractive to the investors.

## PYQ 11

The capital structure of PQR Ltd. is as follows:

| $10 \%$ Debentures | $₹ 3,00,000$ |
| :--- | :--- |
| $12 \%$ Preference shares | $₹ 2,50,000$ |
| Equity shares (face value ₹10 per share) | $₹ 5,00,000$ |

## Additional information:

(i) ₹100 per debenture redeemable at par has 2\% floatation cost \& 10 years of maturity. The market price per debenture is ₹ 110 .
(ii) ₹100 per preference share redeemable at par has 3\% floatation cost \& 10 years of maturity. The market price per preference share is ₹ 108 .
(iii) Equity share has ₹4 floatation cost and market price per share of ₹ 25 . The next year expected dividend is ₹ 2 per share with annual growth of $5 \%$. The firm has a practice of paying all earnings in the form of dividends.
(iv) Corporate Income tax rate is $30 \%$.

Calculate Weighted Average Cost of Capital (WACC) using market value weights.
[(10 Marks) Jan 2021]

## Answer

Calculation of Weighted Average Cost of Capital by Using Market Value Weight

| Particular | Market value | Weight | Cost | Weighted cost |
| :--- | :---: | :---: | :---: | :---: |
| 10\% Debenture | $3,30,000$ | 0.178 | $7.27 \%$ | $1.294 \%$ |
| 12\% Preference share | $2,70,000$ | 0.146 | $12.49 \%$ | $1.823 \%$ |
| Equity Share Capital | $12,50,000$ | 0.676 | $14.52 \%$ | $9.816 \%$ |
| Total | $\mathbf{1 8 , 5 0 , 0 0 0}$ | $\mathbf{1 . 0 0 0}$ | WACC | $\mathbf{1 2 . 9 3 3 \%}$ |

## Working notes:

## 1. Calculation of specific cost of various sources of funds:

$$
\begin{array}{rlll}
\mathrm{K}_{\mathrm{e}} & =\frac{\mathrm{D}_{1}}{\mathrm{P}_{0}-\mathrm{F}} \mathrm{~g} & =\frac{2}{25-4}+.05 & =14.52 \% \\
\mathrm{~K}_{\mathrm{d}} & =\frac{\mathrm{I}(1-\mathrm{t})+\left(\frac{\mathrm{RV}-\mathrm{NP}}{\mathrm{n}}\right)}{\frac{\mathrm{RV}+\mathrm{NP}}{2}} \times 100 & =\frac{10(1-0.30)+\left(\frac{100-98}{10}\right)}{\frac{100+98}{2}} \times 100 & =1.27 \% \\
\mathrm{~K}_{\mathrm{p}} & =\frac{\mathrm{PD}+\left(\frac{\mathrm{RV}-\mathrm{NP}}{\mathrm{n}}\right)}{\frac{R V+N P}{2}} \times 100 & =\frac{12+\left(\frac{100-97}{100}\right)}{\frac{100+97}{2}} \times 100 & =12.49 \%
\end{array}
$$

## 2. Calculation of market value of various sources of funds:

| Debentures | $=3,00,000 \times 110 / 100$ | $=3,30,000$ |
| :--- | :--- | :--- |
| Preference shares $=3,50,000 \times 108 / 100$ | $=$ | $2,70,000$ |
| Equity shares | $=5,00,000 \times 25 / 10$ | $=12,50,000$ |

## PYQ 12

Following are the information of TT Ltd.:

| Particulars |  |
| :--- | :---: |
| Earnings per share | $₹ 10$ |
| Dividend per share | $₹ 6$ |
| Expected growth rate in dividend | $6 \%$ |
| Current market price per share | $₹ 120$ |
| Tax rate | $30 \%$ |
| Requirement of additional finance | $₹ 30,00,000$ |


| Debt Equity ratio (for additional finance) <br> Cost of Debt: | $2: 1$ |
| :--- | :---: |
| $0-5,00,000$ | $10 \%$ |
| 5,00,001-10,00,000 | $9 \%$ |
| Above $10,00,000$ | $8 \%$ |

Assuming that there is no Reserve and Surplus available in TT Ltd.

## You are required to:

(a) Find the pattern of finance for additional requirement.
(b) Calculate post tax average cost of additional debt.
(c) Calculate cost of equity.
(d) Calculate overall weighted average after tax cost of additional finance.
[(10 Marks) July 2021]

## Answer

(a) Pattern for additional requirement: Total requirement of additional fund is ₹30,00,000. With a Debt Equity ratio of $2: 1$. It means ₹ $20,00,000$ is to be raised through debt and ₹ $10,00,000$ through equity. Out of ₹ $20,00,000$ debt, first ₹ $5,00,000 @ 10 \%$, next ₹ $5,00,000 @ 9 \%$ and remaining ₹ $10,00,000 @ 8 \%$. Entire equity finance of ₹ $10,00,000$ through issuing equity shares.
(b) Post tax average cost of additional debt:

| $\mathrm{K}_{\mathrm{d} 1}$ | $=$ | I (1-t) | $=$ | 10\% (1-0.30) | = | 7\% |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{K}_{\mathrm{d} 2}$ | = | $\mathrm{I}(1-\mathrm{t})$ | = | 9\% (1-0.30) | = | 6.30\% |
| $\mathrm{K}_{\mathrm{d} 3}$ | = | I (1-t) | = | 8\% (1-0.30) | = | 5.60\% |
| Average $\mathrm{K}_{\mathrm{d}}$ | = | $\mathrm{K}_{\mathrm{d} 1} \mathrm{~W}_{\mathrm{d} 1}+\mathrm{K}_{\mathrm{d} 2} \mathrm{~W}_{\mathrm{d} 2}+\mathrm{K}_{\mathrm{d} 3} \mathrm{~W}_{\mathrm{d} 3}$ |  |  |  |  |

(c) Cost of Equity:
$\mathrm{K}_{\mathrm{e}} \quad=\frac{\mathrm{D}_{1}}{\mathrm{P}_{0}}+\mathrm{g} \quad=\quad \frac{6(1+0.06)}{120}+0.06=11.30 \%$

## (d) Overall WACC after tax of additional finance:

K

$$
\begin{array}{ll}
= & \mathrm{K}_{\mathrm{e}} \mathrm{~W}_{\mathrm{e}}+\mathrm{K}_{\mathrm{d}} \mathrm{~W}_{\mathrm{d}} \\
= & \mathbf{7 . 8 5 \%}
\end{array}
$$

$$
=\quad 11.30 \% \times \frac{10}{30}+6.125 \% \times \frac{20}{30}
$$

Assumption: DPS is treated at $\mathrm{D}_{\mathrm{o}}$.
PYQ 13
Book value of capital structure of B Ltd. is as follows:

| Sources | Amount |
| :--- | :---: |
| 12\% 6,000 Debentures @ ₹100 each | $₹ 6,00,000$ |
| Retained earnings | $₹ 4,50,000$ |
| 4,500 Equity shares @ ₹100 each | $₹ 4,50,000$ |
|  | $₹ 15,00,000$ |

Currently the market value of debenture is ₹ 110 per debenture and equity share is ₹ 180 per share. The expected rate of return to equity shareholder is $24 \%$ p.a. Company is paying tax @30\%.

Calculate WACC on the basis of market value weights.
[(5 Marks) Dec 2021]

## Answer

Statement of WACC (Market Value Weights)

| Capital Structure | Amount | Weight | Specific Cost | Cost of Capital |
| :---: | :---: | :---: | :---: | :---: |
| 12\% Debentures | $6,60,000$ | 0.449 | 0.0764 | 0.0343 |
| Equity Fund including | $8,10,000$ | 0.551 | 0.1333 | 0.0734 |
| Retained earning |  |  |  |  |
| Total | $\mathbf{1 4 , 7 0 , 0 0 0}$ | $\mathbf{1 . 0 0 0}$ | WACC | $\mathbf{0 . 1 0 7 7}$ |

WACC $\left(K_{o}\right) \quad=\quad 0.1077$ or $10.77 \%$

## Working Notes:

## (1) Calculation of Market Value:

Market value of debenture $=(₹ 6,00,000 \div ₹ 100) \times ₹ 110=₹ 6,60,000$
Market value of Equity and Retained earnings:

$$
=\quad(₹ 4,50,000 \div ₹ 100) \times ₹ 180=₹ 8,10,000
$$

## (2) Calculation of $K_{e}$ :

$$
\mathrm{K}_{\mathrm{e}}=\frac{\mathrm{D}_{1}}{\mathrm{P}_{0}} \times 100=\frac{24 \% \text { of } 100}{180}=13.33 \%
$$

## (3) Calculation of $K_{d}$ :

$$
K_{d} \quad=\quad \frac{I(1-t)}{N P} \times 100=\frac{12 \% \text { of } 100(1-0.3)}{110} \times 100=7.64 \%
$$

## PYQ 14

A company issues:

- $15 \%$ convertible debentures of ₹ 100 each at par with a maturity period of 6 years. On maturity, each debenture will be converted into 2 equity shares of the company. The risk-free rate of return is $10 \%$, market risk premium is $18 \%$ and beta of the company is 1.25 . The company has paid dividend of $₹ 12.76$ per share. Five year ago, it paid dividend of ₹ 10 per share. Flotation cost is $5 \%$ of issue amount.
- $5 \%$ preference shares of $₹ 100$ each at premium of $10 \%$. These shares are redeemable after 10 years at par. Flotation cost is $6 \%$ of issue amount.

Assuming corporate tax rate is 40\%.
(a) Calculate the cost of convertible debentures using the approximation method.
(b) Use YTM method to calculate cost of preference shares.

| Year | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\mathbf{8}$ | $\mathbf{9}$ | $\mathbf{1 0}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PVIF $_{0.03, \mathrm{t}}$ | 0.971 | 0.943 | 0.915 | 0.888 | 0.863 | 0.837 | 0.813 | 0.789 | 0.766 | 0.744 |
| PVIF $_{0.05, \mathrm{t}}$ | 0.952 | 0.907 | 0.864 | 0.823 | 0.784 | 0.746 | 0.711 | 0.677 | 0.645 | 0.614 |
| PVIFA $_{0.33, \mathrm{t}}$ | 0.971 | 1.913 | 2.829 | 3.717 | 4.580 | 5.417 | 6.230 | 7.020 | 7.786 | 8.530 |
| PVIFA $_{0.05, \mathrm{t}}$ | 0.952 | 1.859 | 2.723 | 3.546 | 4.329 | 5.076 | 5.786 | 6.463 | 7.108 | 7.722 |


| Interest rate | $\mathbf{1 \%}$ | $\mathbf{2 \%}$ | $\mathbf{3 \%}$ | $\mathbf{4 \%}$ | $\mathbf{5 \%}$ | $\mathbf{6 \%}$ | $\mathbf{7 \%}$ | $\mathbf{8 \%}$ | $\mathbf{9 \%}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{FVIF}_{\mathrm{i}, 5}$ | 1.051 | 1.104 | 1.159 | 1.217 | 1.276 | 1.338 | 1.403 | 1.469 | 1.539 |
| $\mathrm{FVIF}_{\mathrm{i}, 6}$ | 1.062 | 1.126 | 1.194 | 1.265 | 1.340 | 1.419 | 1.501 | 1.587 | 1.677 |
| $\mathrm{FVIF}_{\mathrm{i}, 7}$ | 1.072 | 1.149 | 1.230 | 1.316 | 1.407 | 1.504 | 1.606 | 1.714 | 1.828 |

[(10 Marks) May 2022]

## Answer

(a) Calculation of cost of Convertible Debentures using Approximation method:

$$
\mathrm{K}_{\mathrm{d}}=\frac{\mathrm{I}(1-\mathrm{t})+\frac{\mathrm{RV}-\mathrm{NP}}{\mathrm{n}}}{\frac{\mathrm{RV}+\mathrm{NP}}{2}} \times 100=\frac{15(1-0.40)+\frac{130.58-95}{6}}{\frac{130.58+95}{2}} \times 100=13.24 \%
$$

## Working Notes:

## Determination of Redemption value:

Higher of:
(i) The cash value of debentures $=₹ 100$
(ii) Value of equity shares $=2$ shares $\times ₹ 48.72(1+0.05)^{6}=\quad ₹ 130.58$
$₹ 130$ will be taken as redemption value as it is higher than the cash option and attractive to the investors.
Calculation of Value of Share today:

| $\mathrm{P}_{0}$ | $=$ | $\frac{\mathrm{D}_{1}}{\mathrm{~K}_{\mathrm{e}}-\mathrm{g}}$ | $=$ | $\frac{12.76(1+0.05)}{32.50 \%-5 \%}$ | $=$ | ₹ 48.72 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{K}_{\text {e }}$ | = | $\mathrm{R}_{\mathrm{f}}+\beta\left(\mathrm{R}_{\mathrm{m}}-\mathrm{R}_{\mathrm{f}}\right)$ | = | $10 \%+1.25 \times 18 \%$ | = | 32.50\% |
| g | = | $\sqrt[5]{\frac{12.76}{10.00}}$ | = | 5\% or |  |  |
| g | = | $12.76 \div 10.00$ | = | 1.276 (5\% for 5 year | giv | in interest |

(b) Calculation of Cost of Preference shares using YTM method::

Calculation of NPV at two discount rates:

| Year | Cash Flow | Present Value |  | Present Value |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathbf{3 \%}$ | $\boldsymbol{D C F}$ | $\mathbf{5 \%}$ | $\boldsymbol{D C F}$ |
| 0 | 103.40 | 1.000 | $(103.40)$ | 1.000 | $(103.40)$ |
| $1-10$ | 5 | 8.530 | 42.65 | 7.722 | 38.61 |
| 10 | 100 | 0.744 | 74.40 | 0.614 | 61.40 |
| NPV |  |  | $\mathbf{+ 1 3 . 6 5}$ |  | -3.39 |

$$
\begin{aligned}
\mathrm{IRR} / \mathrm{K}_{\mathrm{d}} & =\mathrm{LR}+\frac{\mathrm{NPV}_{\mathrm{L}}}{\mathrm{NPV}_{\mathrm{L}}-\mathrm{NPV}_{\mathrm{H}}} \times(\mathrm{H}-\mathrm{L})=3 \%+\frac{13.65}{13.65-(-3.39)} \times(5 \%-3 \%) \\
& =4.60 \%
\end{aligned}
$$

## Working Note:

Net Proceeds $=\quad$ Issue Price - Flotation Cost
$=\quad(100+10 \%$ Premium $)-6 \%=₹ 103.40$

## PYQ 15

The following is the extract of the Balance Sheet of M/s KD Ltd.:

| Particulars | Amount (₹) |
| :--- | :---: |
| Ordinary shares (Face Value ₹10 per share) | $5,00,000$ |
| Share Premium | $1,00,000$ |
| Retained Profits | $6,00,000$ |
| 8\% Preference Shares (Face Value ₹25 per share) | $4,00,000$ |
| 12\% Debentures (Face value ₹100 each) | $6,00,000$ |
|  | $22,00,000$ |

The ordinary shares are currently priced at ₹ 39 ex-dividend and preference share is priced at ₹ 18 Cumdividend. The debentures are selling at 120 percent ex-interest. The applicable tax rate to D Ltd. is 30 percent. KD Ltd.'s cost of equity has been estimated at 19 percent. Calculate the WACC (weighted average cost of capital) of KD Ltd. on the basis of market value.
[(5 Marks) Nov 2022]

## Answer

Statement of WACC (Market Value Weights)

| Capital Structure | Amount | Weight | Specific Cost | Cost of <br> Capital |
| :--- | :---: | :---: | :---: | :---: |
| Ordinary Shares | $8,12,500$ | 0.278 | 0.190 | 0.0528 |
| Share Prem \& Retained Profits | $11,37,500$ | 0.389 | 0.190 | 0.0739 |
| 8\% Preference Shares | $2,56,000$ | 0.087 | 0.125 | 0.0109 |
| 12\% Debentures | $7,20,000$ | 0.246 | 0.070 | 0.0172 |
| Total | $\mathbf{2 9 , 2 6 , 0 0 0}$ | $\mathbf{1 . 0 0 0}$ | WACC | $\mathbf{0 . 1 5 4 8}$ |

WACC $\left(K_{o}\right)=0.1548$ or $15.48 \%$

## Working Notes:

## (1) Calculation of Market Value:

Total Market value of Equity and Retained earnings:

|  | $=$ | $(₹ 5,00,000 \div ₹ 10) \times ₹ 39$ | $=₹ 19,50,000$ |
| :--- | :--- | :--- | :--- |
| Market Value of Equity | $=₹ 19,50,000 \times 5 / 12$ | $=₹ 8,12,500$ |  |
| Market Value of Retained earnings | $=₹ 19,50,000 \times 7 / 12$ | $=₹ 11,37,500$ |  |
| Market Value of Debentures | $=(₹ 6,00,000 \div ₹ 100) \times ₹ 120=₹ 7,20,000$ |  |  |
| Market Value of Preference Shares | $=(₹ 4,00,000 \div ₹ 25) \times ₹ 16^{*}=₹ 2,56,000$ |  |  |

*Market value of 1 Preference Share ex-dividend is used i.e. ₹16 (₹18-8\% of ₹25).
(2) Calculation of $K_{r}$ :

$$
\mathrm{K}_{\mathrm{r}} \quad=\quad \mathrm{K}_{\mathrm{e}} \quad=\quad 19 \%
$$

(3) Calculation of $K_{d}$ :

$$
\mathrm{K}_{\mathrm{d}} \quad=\quad \frac{\mathrm{I}(1-\mathrm{t})}{\mathrm{NP}} \times 100=\frac{12 \% \text { of } 100(1-0.3)}{120} \times 100=7 \%
$$

## (4) Calculation of $K_{p}$ :

$$
\mathrm{K}_{\mathrm{p}}=\frac{\mathrm{PD}}{\mathrm{NP}} \times 100=\frac{8 \% \text { of } 25}{16} \times 100=12.5 \%
$$

PYQ 16
MR Ltd. is having the following capital structure, which is considered to be optimum as on 31.03.2022.

Equity share capital (50,000 shares)
12\% Pref. share capital
15\% Debentures

$$
\begin{aligned}
& \text { ₹ } 8,00,000 \\
& ₹ 50,000 \\
& \text { ₹ } 1,50,000 \\
& \text { ₹10,00,000 }
\end{aligned}
$$

The earnings per share (EPS) of the company were ₹ 2.50 in 2021 and the expected growth in equity dividend is $10 \%$ per year. The next year's dividend per share (DPS) is $50 \%$ EPS of the year 2021. The current market price per share (MPS) is ₹ 25.00 . The $15 \%$ new debentures can be issued by the company. The company's debentures are currently selling at ₹96 per debenture. The new $12 \%$ Pref. Share can be sold at a net price of ₹91.50 (face value ₹100 each). The applicable tax rate is $30 \%$.

## You are required to calculate:

(i) After tax cost of
(a) New debt,
(b) New pref. share capital and
(c) Equity shares assuming that new equity shares come from retained earnings.
(ii) Marginal cost of capital.
(iii) How much can be spent for capital investment before sale of new equity shares assuming that retained earnings for next year investment is 50\% of 2021?
[(6 Marks) Nov 2022]

## Answer

(i) (a) After tax cost of new debt

$$
\mathrm{K}_{\mathrm{d}}=\frac{\mathrm{I}(1-\mathrm{t})}{\mathrm{NP}} \times 100=\frac{15(1-0.30)}{96} \times 100=10.94 \%
$$

(b) After tax cost of new preference shares

$$
\mathrm{K}_{\mathrm{p}}=\frac{\mathrm{PD}}{\mathrm{NP}} \times 100=\frac{12}{91.50} \times 100=13.11 \%
$$

(c) Cost of new equity or cost of retained earnings

$$
\mathrm{K}_{\mathrm{r}}=\frac{\mathrm{D}_{1}}{\mathrm{P}_{0}}+\mathrm{g} \quad=\frac{2.50 \times 50 \%}{25}+0.10=15 \%
$$

(ii) Marginal cost of capital:

$$
\mathrm{K}_{\mathrm{d}} \mathrm{~W}_{\mathrm{d}}+\mathrm{K}_{\mathrm{p}} \mathrm{~W}_{\mathrm{p}}+\mathrm{K}_{\mathrm{r}} \mathrm{~W}_{\mathrm{r}}=10.94 \% \times .15+13.11 \% \times .05+15 \% \times .80=\mathbf{1 4 . 3 0} \%
$$

(iii) The company can pay the following amount before issue of new shares:

Equity (retained earnings in this case) $=80 \%$ of the total capital

| Therefore, investment before new issue $=\frac{62,500}{80 \%}$ | $=$ ₹78,125 |
| :--- | :--- | :--- |
| Retained earnings $=\quad ₹ 2.50 \times 50 \% \times 50,000$ shares | $=$ ₹ 62,500 |

## PYQ 17

Capital structure of D Ltd. as on $31^{\text {st }}$ March, 2023 is given below.

| Particular | ₹ |
| :--- | :---: |
| Equity share capital (₹10 each ) | $30,00,000$ |
| 8\% Preference share capital (₹100 each ) | $10,00,000$ |
| 12\% Debentures (₹100 each ) | $10,00,000$ |

- Current market price of equity share is ₹80 per share. The company has paid dividend of ₹ 14.07 per share. Seven years ago, it paid dividend of ₹10 per share. Expected dividend is ₹ 16 per share.
- $8 \%$ Preference shares are redeemable at $6 \%$ premium after five years. Current market price per preference share is ₹ 104 .
- $12 \%$ debentures are redeemable at $20 \%$ premium after 10 years, Flotation cost is $₹ 5$ per debenture.
- The company is in $40 \%$ tax bracket.
- In order to finance an expansion plan, the company intends to borrow 15\% Long-term loan of ₹ $30,00,000$ from bank. This financial decision is expected to increase dividend on equity share from ₹16 per share to ₹18 per share. However, the market price of equity share is expected to decline from ₹ 80 to ₹ 72 per share, because investors' required rate of return is based on current market conditions.


## Required:

(a) Determine the existing Weighted Average Cost of Capital (WACC) taking book value weights.
(b) Compute Weighted Average Cost of Capital (WACC) after the expansion plan taking book value weights.

| Interest Rate | $\mathbf{1 \%}$ | $\mathbf{2 \%}$ | $\mathbf{3 \%}$ | $\mathbf{4 \%}$ | $\mathbf{5 \%}$ | $\mathbf{6 \%}$ | $\mathbf{7 \%}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{FVIF}_{\mathrm{i}, 5}$ | 1.051 | 1.104 | 1.159 | 1.217 | 1.276 | 1.338 | 1.403 |
| $\mathrm{FVI}_{\mathrm{i}, 6}$ | 1.062 | 1.126 | 1.194 | 1.265 | 1.340 | 1.419 | 1.501 |
| $\mathrm{FVIF}_{\mathrm{i}, 7}$ | 1.072 | 1.149 | 1.230 | 1.316 | 1.407 | 1.504 | 1.606 |

[(10 Marks) May 23]

## Answer

(a) Calculation of Existing Weighted Average Cost of Capital by taking Book Value Weight

| Particulars | Book Value | Weight (W) | Cost (K) | Weighted cost |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Equity Shares | $₹ 30,00,000$ | 0.60 | 0.2500 | 0.1500 |  |  |  |  |  |
| Preference Shares | $₹ 10,00,000$ | 0.20 | 0.0800 | 0.0160 |  |  |  |  |  |
| Debentures | $₹ 10,00,000$ | 0.20 | 0.0902 | 0.0180 |  |  |  |  |  |
| Total |  |  |  |  |  | ₹50,00,000 | $\mathbf{1 . 0 0}$ | WACC | $\mathbf{0 . 1 8 4 0}$ |
|  |  |  |  |  |  |  |  |  |  |
| Existing WACC | $\mathbf{0 . 1 8 4 0}$ or $\mathbf{1 8 . 4 0 \%}$ |  |  |  |  |  |  |  |  |

(b) Calculation of Weighted Average Cost of Capital after expansion by taking Book Value Weight

| Particulars | Book Value | Weight (W) | Cost (K) | Weighted cost |
| :---: | :---: | :---: | :---: | :---: |
| Equity Shares | $₹ 30,00,000$ | 0.375 | 0.3000 | 0.1125 |
| Preference Shares | $₹ 10,00,000$ | 0.125 | 0.0800 | 0.0100 |
| Debentures | $₹ 10,00,000$ | 0.125 | 0.0902 | 0.0113 |
| Long Term Loan | $₹ 30,00,000$ | 0.375 | 0.9000 | 0.0338 |
| Total | $₹ 80,00,000$ | $\mathbf{1 . 0 0 0}$ | WACC | $\mathbf{0 . 1 6 7 6}$ |

Revised WACC $=0.1676$ or $\mathbf{1 6 . 7 6 \%}$

## Working notes:

$$
\mathrm{K}_{\mathrm{e}} \quad=\frac{\mathrm{D}_{1}}{\mathrm{P}_{0}}+\mathrm{g} \quad=\frac{16}{80}+5 \%=25 \%
$$

$$
\mathrm{g} \quad=\sqrt[7]{\frac{14.07}{10}}-1 \quad=5 \%
$$

or

$$
\begin{array}{llll}
\mathrm{g}\left(\mathrm{FVIF}_{\mathrm{i}, 7}\right) & =14.07 \div 10 & =1.407(\mathrm{~g}=5 \% \text { in table }) \\
\mathrm{K}_{\mathrm{p}} & = & \frac{\mathrm{PD}+\left(\frac{\mathrm{RV}-\mathrm{NP}}{\mathrm{n}}\right)}{\frac{\mathrm{RV}+\mathrm{NP}}{2}} \times 100 & =\frac{8+\left(\frac{106-104}{5}\right)}{\frac{106+104}{2}} \times 100=\mathbf{8 \%}
\end{array}
$$

$$
\mathrm{K}_{\mathrm{d}} \quad=\quad \frac{\mathrm{I}(1-\mathrm{t})+\left(\frac{\mathrm{RV}-\mathrm{NP}}{\mathrm{n}}\right)}{\frac{\mathrm{RV}+\mathrm{NP}}{2}} \times 100=\frac{12(1-0.40)+\left(\frac{120-95}{10}\right)}{\frac{120+95}{2}} \times 100=\mathbf{9 . 0 2 \%}
$$

$$
\begin{array}{llll}
\mathrm{K}_{\mathrm{e}}(\text { Revised }) & =\frac{\mathrm{D}_{1}}{P_{0}}+\mathrm{g} & =\frac{18}{72}+5 \% & =\mathbf{3 0 \%} \\
\mathrm{K}_{\mathrm{TL}} & =\mathrm{I}(1-\mathrm{t}) & =15 \%(1-0.4) & =\mathbf{9} \%
\end{array}
$$

PYQ 18
Z Ltd. wishes to raise additional fund of ₹ $25,00,000$ for meeting its investment plan. It has ₹ $5,25,000$ in the form of retained earnings available for investment purposes. Further details are as following:

$$
\begin{array}{ll}
\text { Combination of debt and equity } & 2: 3 \\
\text { Cost of debt } & 8 \% \text { (before tax) } \\
\text { Upto ₹ } 2,50,000 & 10 \% \text { (before tax) } \\
\text { Above ₹ } 2,50,000 \text { and to upto ₹5,00,000 } & 12 \% \text { (after tax) }
\end{array}
$$

| Earning of company | ₹50,00,000 |  |
| :--- | :--- | :--- |
| Retention Ratio | $40 \%$ |  |
| Expected growth of dividend | $15 \%$ |  |
| Market price per share | ₹500 |  |
| Number of outstanding equity shares  $1,00,000$ <br> Tax Rate $30 \%$ ,$l$ |  |  |

## You are required to calculate:

(a) Cost of debt
(b) Cost of retained earnings and cost of equity
(c) Weighted average cost of capital

[(10 Marks) Nov 23]

## Answer

Total capital required is ₹25 lakhs. With a debt-equity ratio of 2:3. It means ₹10 lakhs is to be raised through debt ( $₹ 2,50,000 @ 8 \%$ next ₹ $2,50,000 @ 10 \%$ and ₹ $5,00,000 @ 12 \%$ ) and ₹ 15 lakhs through equity. Out of ₹ 15 lakhs, ₹ $5,25,000$ are available in the form of retained earnings hence ₹ $9,75,000$ lakhs will have to raise by issuing equity shares.
(a) Cost of debt:

| $\mathrm{K}_{\mathrm{d} 1}$ | $=\mathrm{I}(1-\mathrm{t})$ | $=8 \%(1-0.30)$ | $=$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{K}_{\mathrm{d} 2}$ | $\mathrm{I}(1-\mathrm{t})$ | $=10 \%(1-0.30)$ | $=$ |
| $\mathrm{K}_{\mathrm{d} 3}$ | $=$ | $\mathbf{5 . 6 0} \%$ |  |
| Average $\mathrm{K}_{\mathrm{d}}$ |  | $12.00 \%$ (after tax given) |  |
|  |  | $5.6 \% \times \frac{2.5}{10}+7 \% \times \frac{2.5}{10}+12 \% \times \frac{5}{10}$ | $=\mathbf{9 . 1 5 \%}$ |

(b) Cost of retained earning \& cost of equity:

| Ke | = | $\frac{D_{1}}{P_{0}}+g$ | = | $\frac{30+15 \%}{500}+0.15$ | = | 21.90\% |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{K}_{\mathrm{r}}$ | = | $\mathrm{K}_{\text {e }}$ | = | 21.90\% |  |  |
| EPS | = | ₹ $50,00,000$ | 0 Sh |  | = | ₹50 |
| $\mathrm{D}_{0}$ | = | ₹ $50 \times 60 \%$ | = | ₹ 30 |  |  |

(c) Overall cost of additional finance:
$\mathrm{K}_{\mathrm{o}} \quad=\quad \mathrm{K}_{\mathrm{e}} \mathrm{W}_{\mathrm{e}}+\mathrm{K}_{\mathrm{r}} \mathrm{W}_{\mathrm{r}}+\mathrm{K}_{\mathrm{d}} \mathrm{W}_{\mathrm{d}}$

$$
=\quad 21.90 \% \times \frac{9.75}{25}+21.90 \% \times \frac{5.25}{25}+9.15 \% \times \frac{10}{25} \quad=\quad 16.80 \%
$$

Assumption: DPS is treated at $\boldsymbol{D}_{0}$.

## SUGGESTED REVISION FOR EXAM:

$B Q: \quad 8,10,11,21,24,25,26,27,30,33,37,38,39,42$
PYQ: 7, 9, 12, 14, 15, 17

## CHAPTER 9

## BQ 1

Rupa Ltd.'s EBIT is ₹ $5,00,000$. The company has $10 \%$, ₹ 20 lakh debentures. The equity capitalization rate i.e. Ke is $16 \%$.

## You are required to calculate:

(1) Market value of equity and value of firm
(2) Overall cost of capital.

Answer
(1) Statement Showing Market Value of Equity and Value of Firm

| Particulars | $₹$ |
| :--- | :---: |
| Net Operating income | $5,00,000$ |
| Less: Interest on Debt | $2,00,000$ |
| Earnings for Equity Investors | $3,00,000$ |
| Equity Capitalization rate | $16 \%$ |
| Market Value of Equity $(\mathbf{3 , 0 0 , 0 0 0} \div \mathbf{0 . 1 6})$ | $\mathbf{1 8 , 7 5 , 0 0 0}$ |
| Value of debt | $20,00,000$ |
| Total Value of the Firm | $\mathbf{3 8 , 7 5 , 0 0 0}$ |

## (2) Overall cost of capital:

$$
\mathrm{K}_{0}=\frac{\text { EBIT }}{\mathrm{V}} \times 100=\frac{5,00,000}{38,75,000} \times 100=12.90 \%
$$

## BQ 2

Indra Ltd. has EBIT of $₹ 1,00,000$. The company makes use of debt and equity capital. The firm has $10 \%$ debentures of $₹ 5,00,000$ and the firm's equity capitalization rate is $15 \%$.

## You are required to calculate:

(1) Market value of equity and value of firm
(2) Overall cost of capital.

## Answer

## (1) Statement Showing Market Value of Equity and Value of Firm

| Particulars | $₹$ |
| :--- | :---: |
| Net Operating income | $1,00,000$ |
| Less: Interest on Debt | 50,000 |
| Earnings for Equity Investors | 50,000 |
| Equity Capitalization rate | $\mathbf{1 5 \%}$ |
| Market Value of Equity $\mathbf{( 5 0 , 0 0 0} \div \mathbf{0 . 1 5})$ | $\mathbf{3 , 3 3 , 3 3 3}$ |
| Value of debt | $\mathbf{8 , 3 3 , 0 0 0}$ |
| Total Value of the Firm |  |

(2) Overall cost of capital:

$$
\mathrm{K}_{\mathrm{o}}=\frac{\text { EBIT }}{\mathrm{V}} \times 100=\frac{1,00,000}{8,33,333} \times 100=12 \%
$$

BQ 3
Amita Ltd's operating income (EBIT) is ₹5,00,000. The firm's cost of debt is $10 \%$ and currently the firm employs $₹ 15,00,000$ of debt. The overall cost of capital of the firm is $15 \%$.

## You are required to calculate:

(1) Market value of firm.
(2) Cost of Equity.

Answer
(1) Market Value of Firm $=\frac{\text { EBIT }}{\mathrm{K}_{0}}=\frac{5,00,000}{15 \%}=$ ₹33,33,333
(2) Cost of Equity $=\frac{\text { EBIT }-\mathrm{I}}{\text { Market value of Equity }} \times 100=\frac{5,00,000-1,50,000}{18,33,333} \times 100$

## Working note:

$$
\begin{aligned}
\text { Market value of Equity } & =\text { Market value of Firm - Market value of Debt } \\
& =33,33,333-15,00,000=18,33,333
\end{aligned}
$$

## BQ 4

X Ltd. and Y Ltd. are identical except that the former uses debt while the latter does not. Thus levered firm has issued $10 \%$ Debentures of ₹ $9,00,000$. Both the firms earn EBIT of $20 \%$ on total assets of $₹ 15,00,000$. Assuming tax rate is $50 \%$ and capitalization rate is $15 \%$ for an all equity firm.
(i) Compute the value of the two firms using NI approach.
(ii) Compute the value of the two firms using NOI approach.
(iii) Calculate the overall cost of capital, $\mathrm{K}_{0}$ for both the firms using NOI approach.

## Answer

(i) Calculation of Value of firms by NI Approach:

| Particulars | $\boldsymbol{X L t d}$ (₹) | $\boldsymbol{Y}$ Ltd ( $₹$ ) |
| :--- | :---: | :---: |
| EBIT (20\% of ₹15,00,000) | $3,00,000$ | $3,00,000$ |
| Less: Interest on Debt | 90,000 | - |
| Profit Before Tax | $2,10,000$ | $3,00,000$ |
| Less: Tax @ 50\% | $1,05,000$ | $1,50,000$ |
| Profit After Tax | $1,05,000$ | $1,50,000$ |
| Equity Capitalization rate | $15 \%$ | $15 \%$ |
| Market Value of Equity (PAT $\div \mathrm{K}_{\mathrm{e}}$ ) | $7,00,000$ | $10,00,000$ |
| Value of debt | $9,00,000$ | - |
| Total Value of the Firm | $\mathbf{1 6 , 0 0 , 0 0 0}$ | $\mathbf{1 0 , 0 0 , 0 0 0}$ |

(ii) Values of the firm as per NOI Approach:

Value of unlevered firm (Y Ltd) $=\frac{\operatorname{EBIT}(1-\mathrm{t})}{\mathrm{K}_{0}}=\frac{3,00,000(1-0.30)}{0.15}$

$$
=\quad ₹ 10,00,000
$$

Value of levered firm (X Ltd) $=\quad$ Value of unlevered firm + Debt $\times$ tax
$=₹ 10,00,000+9,00,000 \times 50 \%=14,50,000$
This value of ₹ $14,50,000$ can be bifurcated into Debt of ₹ $9,00,000$ and Equity of ₹5,50,000.
(iii) Calculation of $K_{o}$ under NOI Approach:


## Working Notes:

## Calculation of $K_{e}$ of $X$ Ltd:

$\mathrm{K}_{\mathrm{e}} \quad=\quad \frac{\text { Earning for Equity }}{\text { Market value of Equity }} \times 100=\frac{(3,00,000-90,000)(1-0.50)}{5,50,000} \times 100$

## BQ 5

Companies P and Q are identical in all respects including risk factors except for debt-equity, P has issued $10 \%$ debentures of $₹ 18$ lakhs while $Q$ has issued only equity. Both the companies earn $20 \%$ before interest and taxes on their total assets of ₹ 30 lakhs. Assuming a tax rate of $50 \%$ and capitalisation rate of $15 \%$ for an all - equity company.

## Compute the value of companies $P$ and $Q$ using:

(a) Net income approach and
(b) Net operating income approach.

## Answer

(a) Calculation of Value of firms by NI Approach:

| Particulars | P Ltd (₹) | Q Ltd (₹) |
| :--- | :---: | :---: |
| EBIT (20\% of ₹30,00,000) | $6,00,000$ | $6,00,000$ |
| Less: Interest on Debt | $1,80,000$ | - |
| Profit Before Tax | $4,20,000$ | $6,00,000$ |
| Less: Tax @ 50\% | $2,10,000$ | $3,00,000$ |
| Profit After Tax | $2,10,000$ | $3,00,000$ |
| Equity Capitalization rate | $15 \%$ | $15 \%$ |
| Market Value of Equity (PAT $\div \mathrm{K}_{\mathrm{e}}$ ) | $\mathbf{1 4 , 0 0 , 0 0 0}$ | $20,00,000$ |
| Value of debt | $18,00,000$ | - |
| Total Value of the Firm | $\mathbf{3 2 , 0 0 , 0 0 0}$ | $\mathbf{2 0 , 0 0 , 0 0 0}$ |

(b) Values of the firm as per NOI Approach:


## MODIGLIANI \& MILLER HYPOTHESIS

## BQ 6

One third of the total market value of Sanghmani Limited consists of loan stock, which has a cost of 10 per cent. Another company, Samsui Limited, is identical in every respect to Sanghmani Limited, except that its capital structure is all equity, and its cost of equity is 16 per cent. According to Modigliani and Miller, if we ignored taxation and tax relief on debt capital.

## Compute the cost of equity of Sanghmani Limited?

## Answer

| $\mathrm{K}_{\mathrm{o}}$ Sanghmani Limited | $=$ | $\mathrm{K}_{\mathrm{o}}$ Samsui Limited |
| :--- | :--- | :--- |
| $\mathrm{K}_{0}$ Sanghmani Limited | $=$ | $\mathrm{K}_{\mathrm{e}} \mathrm{W}_{\mathrm{e}}+\mathrm{K}_{\mathrm{d}} \mathrm{W}_{\mathrm{d}}$ |
| $16 \%$ | $=$ | $\mathrm{K}_{\mathrm{e}} \times 2 / 3+10 \% \times 1 / 3$ |
| $\mathrm{~K}_{\mathrm{e}}$ Sanghmani Limited | $=$ | $\mathbf{1 9 \%}$ |

## BQ 7

Companies $U$ and $L$ are identical in every respect except that the former does not use debt in its capital structure, while the latter employs ₹ $6,00,000$ of $15 \%$ debt. Assuming that ( $a$ ) all the MM assumptions are met (b) the corporate tax rate is $50 \%$, (c) the EBIT is ₹ $2,00,000$ and (d) the equity capitalization of the unlevered company is $20 \%$.

What will be the value of the firms $U$ and L? Also determine the weighted average cost of capital for both the firms.

## Answer



## BQ 8

Blue Ltd., an all equity financed company is considering the repurchase of ₹ 275 lakhs equity shares and
to replace it with $15 \%$ debentures of the same amount. Current market value of the company is ₹ 1,750 lakhs with its cost of capital of $20 \%$. The company's Earnings before Interest and Taxes (EBIT) are expected to remain constant in future years. The company also has a policy of distributing its entire earnings as dividend. Assuming the corporate tax rate as $30 \%$.

You are required to calculate the impact on the following on account of the change in the capital structure as per Modigliani and Miller (MM) Approach:
(1) Market value of the company,
(2) Overall cost of capital, and
(3) Cost of equity.

## Answer

(1) Market Value (MV) of Blue Ltd:

| MV before repurchase $\left(\mathrm{V}_{\mathrm{UL}}\right)$ | $=$ | 1,750 Lakhs |
| ---: | :--- | :--- |
| MV after repurchase $\left(\mathrm{V}_{\mathrm{L}}\right)$ | $=$ | $\mathrm{V}_{\mathrm{UL}}+$ Debt $\times \mathrm{Tax}$ |
|  | $=$ | $1,750 \mathrm{~L}+275 \mathrm{~L} \times 30 \%$ |
| Impact on MV of firm | $=$ | $1,832.50 \mathrm{~L}-1,750 \mathrm{~L}$ |
|  | $=$ | Increase by $\mathbf{8 2 . 5 0}$ Lakhs |

(2) Overall cost of capital:

WACC before repurchase $=20 \%$
WACC after repurchase $=\frac{\text { EBIT }(1-\mathrm{t})}{\text { Value of firm }} \times 100=\frac{500 \mathrm{~L}(1-0.30)}{1,832.50 \mathrm{~L}} \times 100$

$$
=\quad 19.10 \%
$$

Impact on Cost of capital $=20 \%-19.10 \%=$ Decrease by $\mathbf{0 . 9 0 \%}$
(3) Cost of Equity:
$\mathrm{K}_{\mathrm{e}}$ before repurchase $\quad=\quad 20 \%$
$\mathrm{K}_{\mathrm{e}}$ after repurchase $=\frac{(\text { EBIT }-\mathrm{I})(1-\mathrm{t})}{\text { MV of Equity }} \times 100=\frac{(500 \mathrm{~L}-15 \% \text { of } 275 \mathrm{~L})(1-0.30)}{1,557.50 \mathrm{~L}} \times 100$
$=\quad 20.62 \%$
Impact on $\mathrm{K}_{\mathrm{e}} \quad=\quad 20.62 \%-20 \% \quad=\quad$ Increase by $\mathbf{0 . 6 2 \%}$

## Workings notes:

MV of Equity (before repurchase) $=\frac{\text { EAT }}{\mathrm{K}_{\mathrm{e}}}$
1,750 Lakhs
$=\frac{\mathrm{EAT}}{0.20}$
EAT $=1,750$ Lakhs $\times 20 \%=350 \mathrm{~L}$
EBIT
$=\quad$ EAT $\div(1-\mathrm{t})$
$=350 \mathrm{~L} \div(1-0.3) \quad=\quad 500 \mathrm{~L}$

| MV of Equity (after repurchase) | $=\quad$ Value of firm - Value of Debt |
| ---: | :--- |
|  | $=1,832.50 \mathrm{~L}-275 \mathrm{~L}$ |

## TRADITIONAL APPROACH \& MISCELLANEOUS

## BQ 9

Determine the optimal capital structure of a company from the following information:

| Options | Cost of Debt $\left(K_{d}\right)$ in <br> $\%$ | Cost of Equity $\left(K_{e}\right)$ in <br> $\%$ | \% of Debt on Total Value (Debt + <br> Equity) |
| :---: | :---: | :---: | :---: |
| 1 | 11 | 13 | 0.00 |
| 2 | 11 | 13 | 0.10 |
| 3 | 11.6 | 14 | 0.20 |
| 4 | 12 | 15 | 0.30 |
| 5 | 13 | 16 | 0.40 |
| 6 | 15 | 18 | 0.50 |
| 7 | 18 | 20 | 0.60 |

## Answer

## Calculation of Optimal Debt - Equity Mix

| \% of Debt in capital <br> employed | $\boldsymbol{K}_{\boldsymbol{d}}$ in \% | \% of Equity in capital <br> employed | $\boldsymbol{K}_{\boldsymbol{e}}$ in $\%$ | $\boldsymbol{W} \boldsymbol{W} \boldsymbol{C C}$ <br> $\boldsymbol{K}_{\boldsymbol{o}}=\boldsymbol{K}_{\boldsymbol{e}} \boldsymbol{W}_{\boldsymbol{e}}+\boldsymbol{K}_{\boldsymbol{d}} \boldsymbol{W}_{\boldsymbol{d}}$ |
| :---: | :---: | :---: | :---: | :---: |
| 0.00 | 11 | 1.00 | 13 | $13.00 \%$ |
| 0.10 | 11 | 0.90 | 13 | $12.80 \%$ |
| 0.20 | 11.6 | 0.80 | 14 | $13.52 \%$ |
| 0.30 | 12 | 0.70 | 15 | $14.10 \%$ |
| 0.40 | 13 | 0.60 | 16 | $14.80 \%$ |
| 0.50 | 15 | 0.50 | 18 | $16.50 \%$ |
| 0.60 | 18 | 0.40 | 20 | $18.80 \%$ |

Decision: $2^{\text {nd }}$ option is the best because it has lowest WACC.

## BQ 10

ABC Ltd. with EBIT of ₹ $3,00,000$ is evaluating a number of possible capitals below. Which of the capital structure will you recommend, and why?

| Capital Structure | $\boldsymbol{D e b t}$ | $\boldsymbol{K}_{\boldsymbol{d}}$ | $\boldsymbol{K}_{\boldsymbol{e}}$ |
| :---: | :---: | :---: | :---: |
| I | ₹ $3,00,000$ | $10 \%$ | $12.00 \%$ |
| II | $₹ 4,00,000$ | $10 \%$ | $12.50 \%$ |
| III | ₹5,00,000 | $11 \%$ | $13.50 \%$ |
| IV | $₹ 6,00,000$ | $12 \%$ | $15.00 \%$ |
| V | ₹7,00,000 | $14 \%$ | $18.00 \%$ |

## Answer

Statement of $K_{o}$ and Value of Firm

| Particulars | Plan I | Plan II | Plan III | Plan IV | Plan $\boldsymbol{V}$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| EBIT | $3,00,000$ | $3,00,000$ | $3,00,000$ | $3,00,000$ | $3,00,000$ |
| Less: Interest | 30,000 | 40,000 | 55,000 | 72,000 | 98,000 |
| Net profit | $2,70,000$ | $2,60,000$ | $2,45,000$ | $2,28,000$ | $2,02,000$ |
| $\div \mathrm{K}_{\mathrm{e}}$ | 0.12 | 0.125 | 0.135 | 0.15 | 0.18 |


| Market value of Equity (E) | $22,50,000$ | $20,80,000$ | $18,14,815$ | $15,20,000$ | $11,22,222$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Market value of Debt (D) | $3,00,000$ | $4,00,000$ | $5,00,000$ | $6,00,000$ | $7,00,000$ |
| Market value of firm (V) | $\mathbf{2 5 , 5 0 , 0 0 0}$ | $\mathbf{2 4 , 8 0 , 0 0 0}$ | $\mathbf{2 3 , 1 4 , 8 1 5}$ | $\mathbf{2 1 , 2 0 , 0 0 0}$ | $\mathbf{1 8 , 2 2 , 2 2 2}$ |
| $\boldsymbol{K}_{\boldsymbol{o}}(\mathbf{E B I T} \div \boldsymbol{V})$ | $\mathbf{1 1 . 7 6 \%}$ | $\mathbf{1 2 . 1 0 \%}$ | $\mathbf{1 2 . 9 5 \%}$ | $\mathbf{1 4 . 1 5 \%}$ | $\mathbf{1 6 . 4 6 \%}$ |

The capital structure (Plan I) having $\mathfrak{Y}^{3}, 00,000$ of debt has the lowest cost of capital consequently the highest market value, should be accepted.

## BQ 11

Alpha Limited and Beta Limited are identical except for capital structures. Alpha Ltd. has 50 per cent debt and 50 per cent equity, whereas Beta Ltd. has 20 per cent debt and 80 per cent equity. (All percentages are in market value terms). The borrowing rate for both companies is 8 per cent in a no-tax world, and capital markets are assumed to be perfect.
(a) (i) If you own 2 per cent of the shares of Alpha Ltd., determine your return if the company has net operating income of $₹ 3,60,000$ and the overall capitalisation rate of the company, $\mathrm{K}_{\mathrm{o}}$ is 18 per cent?
(ii) Calculate the implied required rate of return on equity?
(b) Beta Ltd. has the same net operating income as Alpha Ltd. (i) Determine the implied required equity return of Beta Ltd.? (ii) Analyse why does it differ from that of Alpha Ltd.?

## Answer

(a) Value of the Alpha Ltd.

$$
=\frac{\mathrm{NOI}}{\mathrm{~K}_{\mathrm{o}}}=\frac{3,60,000}{18 \%} \quad=\quad \text { F20,00,000 }
$$

Value of Shares of Alpha Ltd. $=50 \%$ of $₹ 20,00,000=$ ₹ $10,00,000$
(i) Return on Shares on Alpha Ltd

| Particulars | $₹$ |
| :--- | :---: |
| Net Operating income | $3,60,000$ |
| Less: Interest on Debt @ 8\% on ₹10,00,0,00 (50\% of ₹20,00,000) | 80,000 |
| Earnings for Equity Investors | $2,80,000$ |
| Return on 2\% Shares (2\% of ₹2,80,000) | $\mathbf{5 , 6 0 0}$ |

(ii) Implied required rate of return on Equity $=\frac{2,80,000}{10,00,000} \times 100=28 \%$
(b) (i) Return on Shares on Beta Ltd

| Particulars | $₹$ |
| :--- | :---: |
| Net Operating income | $3,60,000$ |
| Less: Interest on Debt@ 8\% on ₹4,00,0,00 (20\% of ₹20,00,000) | 32,000 |
| Earnings for Equity Investors | $3,28,000$ |


| Value of Shares of Beta Ltd. | $=80 \%$ of $₹ 20,00,000$ | $=₹ 16,00,000$ |
| :--- | :--- | :--- | :--- |
| Implied required rate of return on Equity | $=\frac{3,28,000}{16,00,000} \times 100$ | $=20.50 \%$ |

(ii) It is lower than the Alpha Ltd. because Beta Ltd. uses less debt in its capital structure. As the equity capitalisation is a linear function of the debt-to-equity ratio when we use the net operating income approach, the decline in required equity return offsets exactly the disadvantage of not employing so much in the way of "cheaper" debt funds.

## ARBITRAGE PROCESS $\left(V_{L}>V_{U L}\right)$

## BQ 12

There are two company N Ltd. and M Ltd., having same earnings before interest and taxes i.e. EBIT of ₹ 20,000 . M Ltd. is a levered company having a debt of ₹ $1,00,000 @ 7 \%$ rate of interest. The cost of equity of N Ltd. is $10 \%$ and of M Ltd. is $11.50 \%$.

Compute how arbitrage process will be carried on?

## Answer

$$
\begin{aligned}
& \text { Value of Equity (S) }=\quad \frac{\text { NOI-Interest }}{\text { Cost of Equity }} \\
& \mathrm{S}_{\mathrm{N}}=\frac{20,000}{10 \%} \quad=\quad ₹ 2,00,000 \\
& \mathrm{~S}_{\mathrm{M}}=\frac{20,000-7,000}{11.50 \%} \quad=\quad ₹ 1,13,043 \\
& \mathrm{~V}_{\mathrm{N}} \quad=\quad \text { ₹2,00,000 } \\
& V_{M} \quad=\quad S_{M}+D \\
& =\text { ₹1,13,043 + ₹1,00,000 = ₹2,13,043 }
\end{aligned}
$$

## Arbitrage Process:

If you have $10 \%$ shares of M Ltd., your value of investment in equity shares is $10 \%$ of ₹ $1,13,043$ i.e. $₹ 11,304.30$ and return will be $10 \%$ of $(₹ 20,000-₹ 7,000)=₹ 1,300$.

## Strategy (Same return with lower investnent):

Sell your $10 \%$ share of levered firm for ₹ $11,304.30$ and borrow $10 \%$ of levered firms debt i.e. $10 \%$ of ₹ $1,00,000$ and invest the money i.e. $10 \%$ in unlevered firms stock:

| Total resources /Money we have | = | ₹ $11,304.30$ + ₹ 10,000 | $=$ | ₹ $21,304.30$ |
| :---: | :---: | :---: | :---: | :---: |
| Invest in 10\% shares of Unlevered firm | = | 10\% of ₹ $2,00,000$ | $=$ | ₹ 20,000 |
| Surplus cash available with you | = | ₹ $21,304.3$ - 20,000 | $=$ | ₹ $1,304.30$ |
| Your return | = | 10\% EBIT of unlevered firm - Interest |  |  |
|  | = | 10\% of ₹ $20,000-7 \%$ of ₹ 10,000 |  |  |
|  | = | ₹ 2,000 - ₹ 700 |  | ₹ 1,300 |

## Conclusion:

Your return is same i.e. ₹ 1,300 which you are getting from N Ltd. before investing in M Ltd. but still you have ₹1,304.3 excess money available with you. Hence, you are better off by doing arbitrage.

## BQ 13

Following data is available in respect of two companies having same business risk:

| Capital employed | $=$ | $₹ 2,00,000$ |
| :--- | :--- | :--- |
| EBIT | $=$ | $₹ 30,000$ |

$\mathrm{K}_{\mathrm{e}} \quad=\quad 12.5 \%$

| Sources | Levered Company (₹) | Unlevered Company (₹) |
| :--- | :---: | :---: |
| Debt (@ 10\%) | $1,00,000$ | - |
| Equity | $1,00,000$ | $2,00,000$ |

Investor is holding $15 \%$ shares in levered company.
Calculate increase in annual earnings of investor if he switches his holding from levered to unlevered company.

## Answer

1. Calculation of Value of firms:

| Particulars | Levered (₹) | Unlevered (₹) |
| :--- | :---: | :---: |
| EBIT | 30,000 | 30,000 |
| Less: Interest @ 10\% | 10,000 | - |
| Earning available to Equity Shareholders | 20,000 | 30,000 |
| Equity Capitalization rate | $12.5 \%$ | $12.5 \%$ |
| Market Value of Equity (Earning for Equity $\div \mathrm{K}_{\mathrm{e}}$ ) | $1,60,000$ | $2,40,000$ |
| Value of Debt | $1,00,000$ | - |
| Value of the Firm | $\mathbf{2 , 6 0 , 0 0 0}$ | $\mathbf{2 , 4 0 , 0 0 0}$ |

Value of Levered company is more than that of unlevered company therefore investor will sell his shares in levered company and buy shares in unlevered company. To maintain the level of risk he will borrow proportionate amount and invest that amount also in shares of unlevered company.

## 2. Investment \& Borrowings:

Sell shares in Levered company (1,60,000 $\times 15 \%$ ) 24,000
Borrow money (1,00,000 $\times 15 \%$ ) 15,000
Buy shares in Unlevered company 39,000

## 3. Change in Return:

Income from shares in Unlevered company (39,000 $\times 12.5 \%) \quad 4,875$
Less: Interest on loan $(15,000 \times 10 \%) \quad 1,500$
Net Income from unlevered firm 3,375
Income from Levered firm ( $24000 \times 12.5 \%) \quad \underline{3,000}$
Incremental Income due to arbitrage 375

## ARBITRAGE PROCESS $\left(V_{U L}>V_{L}\right)$

## BQ 14

There are two companies U Ltd. and L Ltd., having same NOI of ₹ 20,000 except that L Ltd. is a levered company having a debt of ₹ $1,00,000 @ 7 \%$ and cost of equity of $U$ Ltd. \& L Ltd. are $10 \%$ and $18 \%$ respectively.

Compute how arbitrage process will work.

## Answer <br> Calculation of Value of firms:

| Particulars | U Ltd. (₹) | L Ltd. (₹) |
| :--- | :---: | :---: |
| EBIT | 20,000 | 20,000 |
| Less: Interest @ 7\% of ₹1,00,000 | - | 7,000 |
| Earning available to Equity Shareholders | 20,000 | 13,000 |
| Equity Capitalization rate | $10 \%$ | $18 \%$ |
| Market Value of Equity (Earning for Equity $\div \mathrm{K}_{\mathrm{e}}$ ) | $2,00,000$ | 72,222 |
| Value of Debt | - | $1,00,000$ |
| Value of the Firm | $\mathbf{2 , 0 0 , 0 0 0}$ | $\mathbf{1 , 7 2 , 2 2 2}$ |

Assume you have 10\% shares of unlevered firm:

| Investment | $=$ | $10 \%$ of $₹ 2,00,000$ | $=$ |
| :--- | :--- | :--- | :--- |
| Return | $=$ | $10 \%$ on $₹ 20,000$ | $=$ |
| $₹ 2,000$ |  |  |  |

## Strategy (Same return with lower investnent):

Sell your shares in unlevered firm for ₹ 20,000 and buy $10 \%$ shares of levered firm's equity plus debt:

Investment in shares of L Ltd.
Investment in debt of L Ltd.

Total investment
Surplus cash available
Your return in L Ltd.

$$
=10 \% \text { of Earning available for Equity }+ \text { Interest on Debt }
$$

$$
=\quad 10 \% \text { of } ₹ 13,000+7 \% \text { of } ₹ 10,000
$$

$$
=\quad ₹ 1,300+₹ 700
$$

$$
=\quad ₹ 2,000
$$

$$
\begin{aligned}
& =10 \% \text { of ₹72,222 = ₹7,222 } \\
& =10 \% \text { of ₹ } 1,00,000=\text { ₹ } 10,000 \\
& =\quad ₹ 17,222 \\
& =₹ 20,000-₹ 17,222=₹ 2,778
\end{aligned}
$$

In both the cases the return received is ₹ 2,000 and still you have excess cash of ₹ 2,778 . Hence, you are better off. In the above solution we have not invested entire amount received from "sale of shares of Unlevered company". Alternatively, we could have invested entire amount in Levered company. In that case annual earnings would have increased.

## BQ 15

Following data is available in respect of two companies having same business risk:

$$
\begin{array}{lll}
\text { Capital employed } & = & ₹ 2,00,000 \\
\text { EBIT } & = & ₹ 30,000
\end{array}
$$

| Sources | Levered Company ( $)$ ) | Unlevered Company ( $)$ |
| :--- | :---: | :---: |
| Debt (@ 10\%) | $1,00,000$ | - |
| Equity | $1,00,000$ | $2,00,000$ |
| $\mathrm{~K}_{\mathrm{e}}$ | $20 \%$ | $12.5 \%$ |

Investor is holding 15\% shares in Unlevered company.
Calculate increase in annual earnings of investor if he switches his holding from unlevered to levered company.

## Answer

1. Calculation of Value of firms:

| Particulars | Levered (₹) | Unlevered (₹) |
| :--- | :---: | :---: |
| EBIT | 30,000 | 30,000 |
| Less: Interest @ 10\% | 10,000 | - |
| Earning available to Equity Shareholders | 20,000 | 30,000 |
| Equity Capitalization rate | $20 \%$ | $12.5 \%$ |
| Market Value of Equity (Earning for Equity $\div \mathrm{K}_{\mathrm{e}}$ ) | $1,00,000$ | $2,40,000$ |
| Value of Debt | $1,00,000$ | - |
| Value of the Firm | $\mathbf{2 , 0 0 , 0 0 0}$ | $\mathbf{2 , 4 0 , 0 0 0}$ |

Value of Unlevered company is more than that of Levered company therefore investor will sell his shares in unlevered company and buy shares in levered company. Market value of Debt and Equity of Levered company are in the ratio of ₹ $1,00,000$ : ₹ $1,00,000$, i.e., $1: 1$. To maintain the level of risk he will lend proportionate amount (50\%) and invest balance amount (50\%) in shares of Levered company.

## 2. Investment:

Sell shares in Unlevered company ( $2,40,000 \times 15 \%$ )
36,000
Lend money ( $36,000 \times 50 \%$ ) 18,000
Buy shares in Levered company 18,000
Total investment 36,000

## 3. Change in Return:

Income from shares in Levered company (18,000 $\times 20 \%$ ) 3,600
Add: Interest on money lent $(18,000 \times 10 \%) \quad 1,800$
Total income after switch over $\quad 5,400$
Income from Unlevered firm (36,000 $\times 12.5 \%) \quad \underline{4,500}$
Incremental Income due to arbitrage 900

## PAST YEAR QUESTIONS

## PYQ 1

'A' Ltd. and 'B' Ltd. are identical in every respect except capital structure. 'A' Ltd. does not use any debt in its capital structure whereas ' B ' Ltd. employs $12 \%$ debentures amounting to $₹ 10,00,000$. Assumung that:
(i) All assumptions of MM model are met;
(ii) Income tax rate is $30 \%$;
(iii) EBIT is ₹ $2,50,000$ and
(iv) The equity capitalization rate of ' A ' Ltd. is $20 \%$.

Calculate the value of both the companies and also find out Weighted Average Cost of Capital for both the companies.
[(5 Marks) Nov 2014]

## Answer <br> Calculation of value of ' $A$ ' Ltd and ' $B$ ' Ltd:

Value of 'A' Ltd. (Unlevered) $=\frac{\text { EBIT }(1-t)}{\mathrm{K}_{\mathrm{e}}}=\frac{2,50,000(1-.30)}{.20}=\boldsymbol{8 , 7 5 , 0 0 0}$

Value of 'B' Ltd. (Levered) = Market value of 'A' Ltd + Debt $\times$ Tax

$$
=\quad 8,75,000+10,00,000 \times 30 \% \quad=11,75,000
$$

## Calculation of WACC of ' $A$ ' Ltd and ' $B$ ' Ltd:

| $\mathrm{K}_{0}$ of ' $\mathrm{A}^{\prime}$ Ltd. | = | $\mathrm{K}_{\mathrm{e}}$ of 'A' Ltd = | $\begin{aligned} & 20 \% \\ & \text { [In case of All equity company } K_{o}=K_{e} \text { ] } \end{aligned}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{K}_{0}$ of 'B' Ltd. | = | $\frac{\operatorname{EBIT}(1-t)}{V} \times 100$ | = | 2,50,000 (1-.30) | $\times 100$ |
|  |  | 14.89\% |  | 11,75,000 |  |

## PYQ 2

RST Ltd. is expecting an EBIT of $₹ 4,00,000$ for F.Y. 2015-16. Presently the company is financed by equity share capital ₹ $20,00,000$ with equity capitalization rate of $16 \%$. The company is contemplating to redeem part of the capital by introducing debt financing. The company has two options to raise debt to the extent of $30 \%$ or $50 \%$ of the total fund. It is expected that for debt financing upto $30 \%$, the rate of interest will be $10 \%$ and equity capitalization rate will increase to $17 \%$. If the company opts for $50 \%$ debt, then the interest rate will be $12 \%$ and equity capitalization rate will be $20 \%$.

You are required to compute value of the company; its overall cost of capital under different options and also state which is the best option.
[(8 Marks) Nov 2015]

## Answer

> Statement of Value of Firm and Cost of Capital

## Particulars

All equity
30\% Debt
50\% Debt

| Earnings before interest and tax | $4,00,000$ | $4,00,000$ | $4,00,000$ |
| :--- | :---: | :---: | :---: |
| Less: Interest @ 10\% of ₹6,00,000 or | - | 60,000 | - |
| @ 12\% of ₹10,00,000 | - | - | $1,20,000$ |
| Earning available for Equity | $4,00,000$ | $3,40,000$ | $2,80,000$ |
| $\div \mathrm{K}_{\mathrm{e}}$ | $16 \%$ | $17 \%$ | $20 \%$ |
| Value of Equity (E) [PBT $\left.\div \mathrm{K}_{\mathrm{e}}\right]$ | $25,00,000$ | $20,00,000$ | $14,00,000$ |
| Value of Debt (D) | - | $6,00,000$ | $10,00,000$ |
| Value of Firm (V) | $\mathbf{2 5 , 0 0 , 0 0 0}$ | $\mathbf{2 6 , 0 0 , 0 0 0}$ | $\mathbf{2 4 , 0 0 , 0 0 0}$ |
| $\boldsymbol{K}_{\boldsymbol{o}}($ EBIT $\div \boldsymbol{V})$ | $\mathbf{1 6 \%}$ | $\mathbf{1 5 . 3 8 \%}$ | $\mathbf{1 6 . 6 7 \%}$ |

Decision: Company should opt for $30 \%$ debt finance having higher Value of firm and lower $\mathrm{K}_{0}$.

## PYQ 3

PNR Limited and PXR Limited are identical in every respect except capital structure. PNR limited does not employ debts in its capital structure whereas PXR Limited employs 12\% Debentures amounting to ₹ $20,00,000$.

## The following additional information are given to you:

(i) Income tax rate is $30 \%$
(ii) EBIT is ₹5,00,000
(iii) The equity capitalization rate of PNR Limited is $20 \%$ and
(iv) All assumptions of Modigliani - Miller Approach are met.

## Calculate:

(i) Value of both the companies,
(ii) Weighted average cost of capital for both the companies.
[(8 Marks) May 2017]

## Answer <br> Calculation of value of 'PNR' Ltd and 'PXR' Ltd:

| Value of 'PNR' Ltd. (Unlevered) | $=\frac{\text { EBIT }(1-\mathrm{t})}{\mathrm{K}_{\mathrm{e}}}$ |
| ---: | :--- |
|  | $=17,50,000$ |
| Value of 'PXR' Ltd. (Levered) | $=\quad \frac{5,00,000(1-.30)}{.20}$ |
|  | $=17,50,000+20,00,000 \times 30 \%$ |
|  | $=123,50,000$ |

## Calculation of WACC of 'PNR' Ltd and 'PXR' Ltd:

| $\mathrm{K}_{0}$ of 'PNR' Ltd. | = | $K_{e}$ of 'PNR' Ltd [In ca |  | $20 \%$ <br> quity company |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{K}_{0}$ of 'PXR' Ltd. | = | $\underline{\operatorname{EBIT}(1-t)} \times 100$ | $=$ | 5,00,000 (1-.30) |
|  |  | V |  | 23,50,000 |
|  | = | 14.89\% |  |  |

## PYQ 4

Stopgo Ltd. an all equity financed company is considering the repurchase of ₹200 Lakhs euity and to replace it with $15 \%$ debentures of the same amount. Current market value of the company is ₹ 1140

Lakhs and it's cost of capital is 20\%. It's earning before interest and tax (EBIT) are expected to remain constant in future. It's entire earnings are distributed as dividend. Applicable tax rate is $30 \%$.

You are required to calculate the impact on the following on account of the change in the capital structure as per MM Hypothesis:
(1) The market value of the company.
(2) It's cost of capital, and
(3) It's cost of equity.
[(5 Marks) May 2018]

## Answer

(1) Market Value (MV) of Stopgo Ltd:

MV before repurchase ( $\mathrm{V}_{\mathrm{UL}}$ ) = 1,140 Lakhs
MV after repurchase $\left(\mathrm{V}_{\mathrm{L}}\right) \quad=\quad \mathrm{V}_{\mathrm{UL}}+$ Debt $\times$ Tax
$=\quad 1,140 \mathrm{~L}+200 \mathrm{~L} \times 30 \%=1,200$ Lakhs

Impact on MV of firm $=1,200 \mathrm{~L}-1,140 \mathrm{~L}=\quad$ Increase by 60 Lakhs
(2) Weighted average cost of capital:

WACC before repurchase = $20 \%$

WACC after repurchase
$=\frac{\text { EBIT }(1-\mathrm{t})}{\text { Value of firm }} \times 10=\frac{325.71 \mathrm{~L}(1-0.30)}{1,200 \mathrm{~L}} \times 100$
$=19 \%$
Impact on Cost of capital $=\quad 20 \%-19 \% \quad$ Decrease by 1\%
(3) Cost of Equity:
$\mathrm{K}_{\mathrm{e}}$ before repurchase $=\quad 20 \%$
$K_{e}$ after repurchase
$=\quad \frac{(\text { EBIT }-I)(1-t)}{\text { MV of Equity }} \times 100$
$=\quad \frac{(325.71 \mathrm{~L}-15 \% \text { of } 200 \mathrm{~L})(1-0.30)}{1,000 \mathrm{~L}} \times 100$
$=\quad 20.70 \%$

Impact on $K_{e} \quad=\quad 20.70 \%-20 \% \quad=\quad$ Increase by 0.70\%
Workings notes:
MV of Equity (before repurchase) $=\frac{\text { EAT }}{\mathrm{K}_{\mathrm{e}}}$
1,140 Lakhs
$=\frac{\text { EAT }}{0.20}$
EAT
$=1,140$ Lakhs $\times 20 \%=228 \mathrm{~L}$
EBIT
$=\quad$ EAT $\div(1-t)$

|  | $=$ |
| ---: | :--- |
|  | $228 \mathrm{~L} \div(1-0.3)=325.71 \mathrm{~L}$ |
| MV of Equity (after repurchase) | $=$ |
|  | $=$ |
|  | Value of firm - Value of Debt |
| $1,200 \mathrm{~L}-200 \mathrm{~L}$ | $=\quad 1,000 \mathrm{~L}$ |

## PYQ 5

The following data relate to two companies belonging to the same risk class:

|  | $\boldsymbol{A} \boldsymbol{L} \boldsymbol{t} \boldsymbol{d}$. | $\boldsymbol{B} \boldsymbol{L} \boldsymbol{t \boldsymbol { d }}$. |
| :--- | :---: | :---: |
| Expected Net operating Income | $₹ 18,00,000$ | $₹ 18,00,000$ |
| 12\% Debt | $₹ 54,00,000$ | - |
| Equity Capitalization Rate | - | 18 |

## Required:

(a) Determine the total market value, Equity capitalization rate and weighted average cost of capital for each company assuming no taxes as per M.M. Approach.
(b) Determine the total market value, Equity capitalization rate and weighted average cost of capital for each company assuming $40 \%$ taxes as per M.M. Approach.
[(10 Marks) Nov 2018]

## Answer

(a) Various calculation without tax:

## Market Value of firms:

| Market Value of B Ltd. (VUL) | $=$ | EBIT $\div \mathrm{K}_{\mathrm{e}}$ |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  | $=$ | $₹ 18,00,000 \div 18 \%$ | $=$ | ₹1,00,00,000 |
| Market Value of A Ltd. $\left(\mathrm{V}_{\mathrm{L}}\right)$ | $=$ | Value of unlevered | $=$ | ₹1,00,00,000 |

## Equity Capitalization Rate:

Equity Capitalization Rate (B Ltd.) $=18 \%$ (given in the question)
Equity Capitalization Rate (A Ltd.) $=$ (EBIT -I$) \div$ *E (Value of Equity)
$=\quad(₹ 18,00,000-12 \% \times ₹ 54,00,000) \div ₹ 46,00,000$
$=\quad 25.04 \%$
*Value of Equity (E) of A Ltd. = Value of Firm - Debt
$=$ ₹ $1,00,00,000-₹ 54,00,000=$ ₹ $46,00,000$

## Weighted Average Cost of Capital:

| Weighted Average Cost of Capital (B Ltd.)= | $\mathrm{K}_{\mathrm{e}}$ | = | K | = | 18\% |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Weighted Average Cost of Capital (A Ltd.)= |  |  | e of |  |  |
| = |  |  | ₹1,0 | = | 18\% |

## (b) Various calculation with tax:

Market Value of B Ltd. ( $\mathrm{V}_{\mathrm{UL}}$ )
Market Value of A Ltd. $\left(\mathrm{V}_{\mathrm{L}}\right)$

| $=$ |  | EBIT $(1-\mathrm{t}) \div \mathrm{K}_{\mathrm{e}}$ or $\mathrm{K}_{\mathrm{o}}$ |  |
| :--- | :--- | :--- | :--- |
| $=$ | ₹ $18,00,000(1-0.40) \div 18 \%=$ | ₹ $60,00,000$ |  |
| $=$ |  |  |  |
| $=$ | Value of unlevered + Debt $\times$ Tax |  |  |
|  | ₹ $60,00,000+₹ 54,00,000 \times .4=$ | ₹ $81,60,000$ |  |

## Equity Capitalization Rate:

| Equity Capitalization Rate (B Ltd.) | $=\mathbf{1 8 \%}$ (given in the question) |
| ---: | :--- |
| Equity Capitalization Rate (A Ltd.) | $=\quad$ (EBIT - I) $(1-\mathrm{t}) \div * \mathrm{E}($ Value of Equity) |
|  | $=(₹ 18,00,000-12 \% \times ₹ 54,00,000)(1-.4) \div ₹ 27,60,000$ |
|  | $=25.04 \%$ |
| $*$ Value of Equity (E) of A Ltd. | $=$ Value of Firm - Debt |
|  | $=\quad ₹ 81,60,000-₹ 54,00,000 \quad=\quad ₹ 27,60,000$ |

Weighted Average Cost of Capital:

| Weighted Average Cost of Capital (B Ltd.) | $=$ | $\mathrm{K}_{\mathrm{e}} \quad=\quad \mathrm{K}_{0}$ |
| ---: | :--- | :--- | :--- |
| Weighted Average Cost of Capital (A Ltd.) $=$  EBIT $(1-\mathrm{t}) \div \mathrm{V}($ Value of Firm $)$ <br>  $=$ $₹ 18,00,000(1-0.4) \div ₹ 81,60,000$  <br>  $=$ $\mathbf{1 3 . 2 4 \%} \%$  |  |  |

## PYQ 6

A Limited and B Limited are identical except for capital structures. A Ltd. has 60 per cent debt and 40 per cent equity, whereas B Ltd. has 20 per cent debt and 80 per cent equity. (All percentages are in market value terms). The borrowing rate for both companies is 8 per cent in a no-tax world, and capital markets are assumed to be perfect.
(a) (i) If X , own 3 per cent of the equity shares of A Ltd., determine his return if the Company has net operating income of $₹ 4,50,000$ and the overall capitalisation rate of the company, $K_{o}$ is 18 per cent.
(ii) Calculate the implied required rate of return on equity of A Ltd.
(b) B Ltd. has the same net operating income as A Ltd.
(i) Calculate the implied required equity return of B Ltd.
(ii) Analyse why does it differ from that of A Ltd.
[(10 Marks) Jan 2021]
Answer
(a) Value of the A Ltd.

Value of Shares of A Ltd.

$$
\begin{array}{llll}
=\frac{\text { NOI }}{\mathrm{K}_{\mathrm{o}}} \quad=\frac{4,50,000}{18 \%} & =₹ 25,00,000 \\
=40 \% \text { of ₹ } 25,00,000 & = & =10,00,000
\end{array}
$$

## (i) Return of X on Shares on A Ltd

| Particulars | $₹$ |
| :---: | :---: |
| Net Operating income | $4,50,000$ |


| Less: Interest on Debt@ 8\% on ₹15,00,000 (60\% of ₹25,00,000) <br> Earnings for Equity Investors | $1,20,000$ |
| :--- | :---: |
| Return on 3\% Shares (3\% of ₹3,30,000) | $3,30,000$ |
| (ii) Implied required rate of return on Equity $=\frac{3,900}{10,00,000} \times 100$ |  |

(b) (i) Return on Shares on B Ltd

| Particulars | $₹$ |
| :--- | :---: |
| Net Operating income | $4,50,000$ |
| Less: Interest on Debt@ 8\% on ₹5,00,000 $(20 \%$ of ₹ $25,00,000)$ | 40,000 |
| Earnings for Equity Investors | $4,10,000$ |


| Value of Shares of Beta Ltd. | $=$ | $80 \%$ of $₹ 25,00,000$ | $=$ | ₹20,00,000 |
| :--- | :--- | :--- | :--- | :--- |
| Implied required rate of return on Equity | $=$ | $\frac{4,10,000}{20,00,000} \times 100$ | $=20.50 \%$ |  |

(ii) It is lower than the A Ltd. because B Ltd. uses less debt in its capital structure. As the equity capitalisation is a linear function of the debt-to-equity ratio when we use the net operating income approach, the decline in required equity return offsets exactly the disadvantage of not employing so much in the way of "cheaper" debt funds.

## PYQ 7

The details about two companies R Ltd. and S Ltd. having same operating risk are given below:

| Particulars | $\boldsymbol{R}$ Ltd. | $\boldsymbol{S}$ Ltd. |
| :--- | :---: | :---: |
| Profit before interest and tax | ₹10 Lakhs | ₹10 Lakhs |
| Equity share capital ₹10 each | ₹17 Lakhs | ₹50 Lakhs |
| Long term borrowings @ 10\% | ₹33 Lakhs | - |
| Cost of Equity $\left(\mathrm{K}_{\mathrm{e}}\right)$ | $18 \%$ | $15 \%$ |

(1) Calculate the value of equity of both the companies on the basis of M.M. Approach without tax.
(2) Calculate the total value of both the companies on the basis of M.M. Approach without tax.
[(5 Marks) July 2021]

## Answer

(1) Value of Equity $=\frac{\text { EBIT }-\mathrm{I}}{\mathrm{Ke}}$

| $\boldsymbol{R}$ Ltd. | $=\frac{\text { EBIT }-1}{\mathrm{Ke}}=\frac{10,00,000-10 \% \text { of } 33,00,000}{18 \%}=37,22,222$ |
| :--- | :--- |
| $S$ Ltd. | $=\frac{\text { EBIT }-\mathrm{I}}{\mathrm{Ke}}=\frac{10,00,000-0}{15 \%}=66,66,667$ |

## (2) Value of Companies:

| Value of S Ltd. $\left(\mathrm{V}_{\mathrm{UL}}\right)=$ | EBIT $\div \mathrm{K}_{\mathrm{o}} \quad=\quad 10,00,000 \div 15 \%=\mathbf{6 6 , 6 6 , 6 6 7}$ |  |
| :--- | :--- | :--- | :--- |
| Value of R Ltd. $\left(\mathrm{V}_{\mathrm{L}}\right)$ | $=\quad$ Value of S Ltd. $\left(\mathrm{V}_{\mathrm{UL}}\right)$ | $=\mathbf{6 6 , 6 6 , 6 6 7}$ |

Note: Alternatively Value of R Ltd. can be calculated as: V $=\mathrm{S}+\mathrm{D}(\mathrm{V}=37,22,222+33,00,000=$ 70,22,222).

## PYQ 8

The following are the costs and values for the firms A and B according to the traditional approach.

| Particulars | Firm $\boldsymbol{A}$ | Firm $\boldsymbol{B}$ |
| :--- | :---: | :---: |
| Total value of firm, V (in ₹) | 50,000 | 60,000 |
| Market value of debt, D (in ₹) | 0 | 30,000 |
| Market value equity, E (in ₹) | 50,000 | 30,000 |
| Expected net operating income (in ₹) | 5,000 | 5,000 |
| Cost of debt (in ₹) | 0 | 1,800 |
| Net Income (in ₹) | 5,000 | 3,200 |
| Cost of equity, Ke = NI/E | $10.00 \%$ | $10.70 \%$ |

(i) Compute the Equilibrium value for Firm A and B in accordance with the MM approach. Assume that (a) taxes do not exist and (b) the equilibrium value of Ke is $9.09 \%$.
(ii) Compute Value of Equity and Cost of Equity for both the firms.
[(4 Marks) Nov 22]

## Answer

(i) Equilibrium value of Firm A (Unlevered)

$$
\begin{array}{lll}
= & \text { Net operating income } \div \mathrm{K}_{\mathrm{e}} \\
= & ₹ 5,000 \div 9.09 \% \quad= & \text { ₹55,006 } \\
= & \text { Value of Firm A (Unlevered) } \\
= & \text { ₹55,006 } \\
= & \text { ₹55,006 } \\
= & \mathbf{9 . 0 9 \%} \\
= & \text { Value of Firm B - Value of debt } \\
= & \text { ₹55,006 - ₹30,000 = ₹25,006 } \\
= & \text { NI/E } \\
= & ₹ 3,200 \div ₹ 25,006= & \mathbf{1 2 . 8 0 \%}
\end{array}
$$

$$
\text { Equilibrium value of Firm B (Levered) } \quad=\quad \text { Value of Firm A (Unlevered) }
$$

(ii) Value of Equity Firm A

Cost of Equity Firm A
Value of Equity Firm B $\quad=\quad$ Value of Firm B - Value of debt

Cost of Equity Firm B

## SUGGESTED REVISION FOR EXAM:

BQ: $\quad 5,6,8,10,11,12,14$
PYQ: 3, 4

## MODIGLIANI AND MILLER (MM) HYPOTHESIS

## BQ 1

AB Engineering ltd. belongs to a risk class for which the capitalization rate is $10 \%$. It currently has outstanding 10,000 shares selling at $₹ 100$ each. The firm is contemplating the declaration of a dividend of ₹5 per share at the end of the current financial year. It expects to have a net income of ₹ $1,00,000$ and has a proposal for making new investments of ₹ $2,00,000$.

## Required:

1. Calculate value of firm when dividends are not paid.
2. Calculate value of firm when dividends are paid.

## Answer

## 1. Value of the firm when dividends are not paid:

Step 1: Calculate price at the end of the period:

| Ke | $=$ | 10\%, | $\mathrm{P}_{0}$ | $=$ | ₹ 100 , | $\mathrm{D}_{1}$ | $=$ | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}_{\text {o }}$ | $=$ | $\frac{\mathrm{P}_{1}+\mathrm{D}_{1}}{1+\mathrm{K}_{\mathrm{e}}}$ |  |  |  |  |  |  |
| ₹100 | = | $\frac{\mathrm{P}_{1}+0}{1+0.10}$ | or |  |  | $\mathrm{P}_{1}$ | = | ₹110 |

Step 2: No. of shares required to be issued:

$$
\text { No. of shares } \Delta \mathrm{n}=\quad \frac{\text { Funds requied-(E-D) }}{\text { Price at } \operatorname{end}\left(\mathrm{P}_{1}\right)} \quad=\quad \frac{2,00,000-(1,00,000-0)}{110}=\mathbf{9 0 9 . 0 9} \text { shares }
$$

Step 3: Calculation of value of firm:

$$
\begin{array}{ll}
\mathrm{nP}_{\mathrm{o}} & =\frac{(\mathrm{n}+\Delta \mathrm{n}) \mathrm{P}_{1}-\mathrm{I}+\mathrm{E}}{1+\mathrm{K}_{\mathrm{e}}} \\
\mathrm{nP}_{\mathrm{o}} & =\frac{(10,000+909.09) 110-2,00,000+1,00,000}{(1+.10)}
\end{array}
$$

## 2. Value of the firm when dividends are paid:

Step 1: Calculate price at the end of the period:

| Ke | $=$ | 10\%, | $\mathrm{P}_{0}$ | $=$ | ₹ 100 , | $\mathrm{D}_{1}$ | $=$ | ₹5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}_{\text {o }}$ | = | $\frac{\mathrm{P}_{1}+\mathrm{D}_{1}}{1+\mathrm{K}_{\mathrm{e}}}$ |  |  |  |  |  |  |
| $₹ 100$ | = | $\frac{\mathrm{P}_{1}+5}{1+0.10}$ | or |  |  | $\mathrm{P}_{1}$ | $=$ | ₹105 |

Step 2: No. of shares required to be issued:
No. of shares $\Delta \mathrm{n}=\quad \frac{\text { Funds requied- }(\mathrm{E}-\mathrm{D})}{\text { Price at } \operatorname{end}\left(\mathrm{P}_{1}\right)} \quad=\quad \frac{2,00,000-(1,00,000-50,000)}{105}=\mathbf{1 , 4 2 8 . 5 7}$ shares
Step 3: Calculation of value of firm:

$$
\begin{aligned}
\mathrm{nP}_{\mathrm{o}} & =\frac{(\mathrm{n}+\Delta \mathrm{n}) \mathrm{P}_{1}-\mathrm{I}+\mathrm{E}}{1+\mathrm{K}_{\mathrm{e}}} \\
\mathrm{nP}_{\mathrm{o}} & =\frac{(10,000+1,428.57) 105-2,00,000+1,00,000}{(1+.10)} \quad=\quad \mathfrak{F} 10,00,000
\end{aligned}
$$

Thus, it can be seen that the value of the firm remains the same in either case.
BQ 2
RST Ltd. has a capital of ₹ $10,00,000$ in equity shares of ₹ 100 each. The shares are currently quoted at par. The company proposes to declare a dividend of ₹10 per share at the end of the current financial year. The capitalization rate for the risk class of which the company belongs is $12 \%$. Net profit is $₹ 2,50,000$ and amount of new investment during the period is $₹ 5,00,000$. What will be the market price of the share at the end of the year, if

1. Dividend is not declared?
2. Dividend is declared?
3. Assuming that the company pays the dividend and has net profits of $₹ 5,00,000$ and makes new investments of ₹ $10,00,000$ during the period, how many new shares must be issued? Use the MM model.

## Answer

Given,

| Cost of Equity $\left(\mathrm{K}_{\mathrm{e}}\right)$ | $12 \%$ |
| :--- | ---: |
| Number of shares in the beginning (n) | 10,000 |
| Current Market Price $\left(\mathrm{P}_{0}\right)$ | $₹ 100$ |
| Net Profit (E) | $₹ 2,50,000$ |
| Expected Dividend | $₹ 10$ per share |
| Investment (I) | $₹ 5,00,000$ |

1. $\mathrm{P}_{\mathrm{o}}=\frac{\mathrm{P}_{1}+\mathrm{D}_{1}}{1+\mathrm{K}_{\mathrm{e}}}$
$₹ 100 \quad \frac{P_{1}+0}{1+0.12} \quad$ or $\quad P_{1}=₹ 112-0={ }^{2} 112$
2. $\mathrm{P}_{\mathrm{o}}=\frac{\mathrm{P}_{1}+\mathrm{D}_{1}}{1+\mathrm{K}_{\mathrm{e}}}$
$₹ 100 \quad \frac{P_{1}+10}{1+0.12} \quad$ or $\quad P_{1}=₹ 112-10={ }^{2} 102$
3. No. of shares $=\quad \frac{\text { Funds required-(E-D) }}{\text { Price at end }\left(\mathrm{P}_{1}\right)}$
$\Delta \mathrm{n} \quad=\quad \frac{10,00,000-(5,00,000-1,00,000)}{102} \quad=\quad 5882.35$ or 5883 shares

## BQ 3

M Ltd. belongs to a risk class for which the capitalization rate is $10 \%$. It has 25,000 outstanding shares and the current market price is ₹ 100 . It expects a net profit of $₹ 2,50,000$ for the year and the Board is considering dividend of ₹ 5 per share. M Ltd. requires to raise ₹ $5,00,000$ for an approved investment expenditure. Show, how the MM approach affects the value of $M$ Ltd. if dividends are paid or not paid?

## Answer

Given,

| Cost of Equity (Ke) | $10 \%$ |
| :--- | ---: |
| Number of shares in the beginning (n) | 25,000 |
| Current Market Price $\left(\mathrm{P}_{0}\right)$ | ₹ 100 |
| Net Profit (E) | ₹2,50,000 |
| Expected Dividend | ₹5 per share |
| Investment (I) | ₹5,00,000 |

## 1. Value of the firm when dividends are not paid:

Step 1: Calculate price at the end of the period:

| $\mathrm{K}_{\text {e }}$ | $=$ | 10\%, | $\mathrm{P}_{0}$ | = | $₹ 100$, | $\mathrm{D}_{1}$ | $=$ | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}_{\text {o }}$ | = | $\frac{\mathrm{P}_{1}+\mathrm{D}_{1}}{1+\mathrm{K}_{\mathrm{e}}}$ |  |  |  |  |  |  |
| ₹100 | $=$ | $\frac{\mathrm{P}_{1}+0}{1+0.10}$ |  | or |  | $\mathrm{P}_{1}$ | = | F110 |

Step 2: No. of shares required to be issued:

$$
\text { No. of shares } \Delta \mathrm{n}=\frac{\text { Funds requied-(E-D) }}{\text { Price at } \operatorname{end}\left(\mathrm{P}_{1}\right)}=\frac{5,00,000-(2,50,000-0)}{110}=2,272.73 \text { shares }
$$

Step 3: Calculation of value of firm:

$$
\begin{array}{ll}
\mathrm{nP}_{\mathrm{o}} & =\frac{(\mathrm{n}+\Delta \mathrm{n}) \mathrm{P}_{1}-\mathrm{I}+\mathrm{E}}{1+\mathrm{K}_{\mathrm{e}}} \\
\mathrm{nP}_{\mathrm{o}} & =\frac{(25,000+2,272.73) 110-5,00,000+2,50,000}{(1+.10)}=\mathbb{F} 25,00,000
\end{array}
$$

## 2. Value of the firm when dividends are paid:

Step 1: Calculate price at the end of the period:

| Ke | $=$ | 10\%, | $\mathrm{P}_{0}$ | $=$ | ₹ 100 , | $\mathrm{D}_{1}$ | $=$ | ₹5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}_{\text {o }}$ | = | $\frac{\mathrm{P}_{1}+\mathrm{D}_{1}}{1+\mathrm{K}_{\mathrm{e}}}$ |  |  |  |  |  |  |
| $₹ 100$ | = | $\frac{\mathrm{P}_{1}+5}{1+0.10}$ |  | or |  | $\mathrm{P}_{1}$ | = | ₹105 |

Step 2: No. of shares required to be issued:

$$
\text { No. of shares } \Delta \mathrm{n}=\frac{\text { Funds requied }-(\mathrm{E}-\mathrm{D})}{\text { Price at end }\left(\mathrm{P}_{1}\right)} \quad=\quad \frac{5,00,000-(2,50,000-1,25,000)}{105}=3,571.43 \text { shares }
$$

Step 3: Calculation of value of firm:

$$
\begin{array}{ll}
\mathrm{nP}_{\mathrm{o}} & =\frac{(\mathrm{n}+\Delta \mathrm{n}) \mathrm{P}_{1}-\mathrm{I}+\mathrm{E}}{1+\mathrm{K}_{\mathrm{e}}} \\
\mathrm{nP}_{\mathrm{o}} & =\frac{(25,000+3,571.43) 105-5,00,000+2,50,000}{(1+.10)}=\mathbb{F} 25,00,000
\end{array}
$$

Thus, it can be seen that the value of the firm remains the same in either case.

## BQ 4

Aakash Ltd. has 10 lakh equity shares outstanding at the start of the accounting year 2023. The existing market price per share is ₹ 150 . Expected dividend is ₹8 per share. The rate of capitalization appropriate to the risk class to which the company belongs is $10 \%$.

1. Calculate the market price per share when expected dividends are: (a) declared, and (b) not declared, based on the Miller - Modigliani approach.
2. Calculate number of shares to be issued by the company at the end of the accounting year on the assumption that the net income for the year is ₹ 3 crores, investment budget is $₹ 6$ crores, when (a) Dividends are declared, and (b) Dividends are not declared.
3. Proof that the market value of the shares at the end of the accounting year will remain unchanged irrespective of whether (a) Dividends are declared, or (ii) Dividends are not declared.

## Answer

1. Calculation of market price per share:
(a) When expected dividends are declared:

| Ke | $=$ | 10\%, | $\mathrm{P}_{0}$ | $=$ | ₹150, | $\mathrm{D}_{1}$ | = | ₹8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}_{\text {o }}$ | = | $\frac{\mathrm{P}_{1}+\mathrm{D}_{1}}{1+\mathrm{K}_{\mathrm{e}}}$ |  |  |  |  |  |  |
| $₹ 150$ | = | $\frac{\mathrm{P}_{1}+8}{1+0.10}$ |  | or |  | $\mathrm{P}_{1}$ | = | ₹157 |

(b) When expected dividends are not declared:

| Ke | $=$ | 10\%, | $\mathrm{P}_{0}$ | $=$ | ₹ 150, | $\mathrm{D}_{1}$ | = | ₹0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}_{\text {o }}$ | = | $\frac{\mathrm{P}_{1}+\mathrm{D}_{1}}{1+\mathrm{K}_{\mathrm{e}}}$ |  |  |  |  |  |  |
| ₹150 | = | $\frac{\mathrm{P}_{1}+0}{1+0.10}$ |  | or |  | $\mathrm{P}_{1}$ | = | F165 |

2. Calculation of no. of shares required to be issued:
(a) When expected dividends are declared:

$$
\begin{aligned}
\text { No. of shares } \Delta \mathrm{n} & =\frac{\text { Funds requied }-(\mathrm{E}-\mathrm{D})}{\text { Price at end }\left(\mathrm{P}_{1}\right)}=\frac{6,00,00,000-(3,00,00,000-80,00,000)}{157} \\
& =2,42,038.22 \text { shares }
\end{aligned}
$$

(b) When expected dividends are not declared:

$$
\begin{aligned}
\text { No. of shares } \Delta \mathrm{n} & =\frac{\text { Funds requied }-(\mathrm{E}-\mathrm{D})}{\text { Price at end }\left(\mathrm{P}_{1}\right)}=\frac{6,00,00,000-(3,00,00,000-0)}{165} \\
& =\mathbf{1 , 8 1 , 8 1 8 . 1 8} \text { shares }
\end{aligned}
$$

## 3. Calculation of market value of shares at the end:

(a) When expected dividends are declared:

Market value of shares $=$ Total shares at the end $\times$ Market value per share
$=(10,00,000+2,42,038.22) \times 157=$ ₹ $19,50,00,000$
(b) When expected dividends are not declared:

$$
\begin{aligned}
\text { Market value of shares } & =\text { Total shares at the end } \times \text { Market value per share } \\
& =(10,00,000+1,81,818.18) \times 165=\% \mathbf{₹ 1 9 , 5 0 , 0 0 , 0 0 0}
\end{aligned}
$$

Hence, it is proved that the total market value of shares remains unchanged irrespective of whether dividends are declared, or not declared.

## BQ 5

Ordinary shares of a listed company are currently trading at ₹ 10 per share with two lakh shares outstanding. The company anticipates that its earnings for next year will be ₹ $5,00,000$. Existing cost of capital for equity shares is $15 \%$. The company has certain investment proposals under discussion which will cause an additional 26,089 ordinary shares to be issued if no dividend is paid or an additional 47,619 ordinary shares to be issued if dividend is paid. Applying the MM hypothesis on dividend decisions.

Calculate the amount of investment and dividend that is under consideration by the company.

## Answer

## 1. Calculation of Investment:

When no dividend is paid:

$$
\begin{aligned}
\text { No. of shares } \Delta \mathrm{n} & =\frac{\text { Funds requied-(E-D) }}{\text { Price at } \operatorname{end}\left(\mathrm{P}_{1}\right)}=\frac{I-(5,00,000-0)}{11.50} \\
26,089 \times ₹ 11.50 & =\mathrm{I}-₹ 5,00,000 \\
\mathrm{I} & =₹ 8,00,024
\end{aligned}
$$

Working Note:

When expected dividends are not declared:

| Ke | $=$ | 15\%, | $\mathrm{P}_{0}$ | $=$ | ₹ 10, | $\mathrm{D}_{1}$ | = | ₹0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}_{\text {o }}$ | = | $\frac{\mathrm{P}_{1}+\mathrm{D}_{1}}{1+\mathrm{K}_{\mathrm{e}}}$ |  |  |  |  |  |  |
| ₹10 | = | $\frac{\mathrm{P}_{1}+0}{1+0.15}$ |  | or |  | $\mathrm{P}_{1}$ | = | ₹11.50 |

## 2. Calculation of Dividend:

When dividend is paid:

$$
\begin{array}{ll}
\mathrm{P}_{\mathrm{o}} & =\frac{\mathrm{P}_{1}+\mathrm{D}_{1}}{1+\mathrm{K}_{\mathrm{e}}} \\
₹ 10 & =\frac{\mathrm{P}_{1}+\mathrm{D}_{1}}{1+0.15}
\end{array} \quad \text { or } \quad \mathrm{P}_{1} \quad=\quad ₹ 11.50-D_{1} .
$$

Now,

| No. of shares $\Delta \mathrm{n}$ | $=\frac{\mathrm{I}(\mathrm{E}-\mathrm{D})}{\mathrm{P}_{1}} \quad=\quad \frac{8,00,024-\left(5,00,000-2,00,000 \mathrm{D}_{1}\right)}{P_{1}}$ |
| ---: | :--- |
| $47,619 \times \mathrm{P}_{1}$ | $=3,00,024+2,00,000 \mathrm{D}_{1}$ |
| $47,619 \times\left(11.50-\mathrm{D}_{1}\right)$ | $=5,47,619-47,619 \mathrm{D}_{1}=\quad 3,00,024+2,00,000 \mathrm{D}_{1}$ |
| $2,47,619 \mathrm{D}_{1}$ | $=2,47,595$ |
| $\mathrm{D}_{1}$ | $\left.=11.50-\boldsymbol{D}_{1}\right)$ |
|  |  |

## WALTER MODEL

## BQ 6

XYZ ltd. which earns ₹ 10 per share is capitalized at $10 \%$ and has a return on investment of $12 \%$. Determine the optimum dividend payout ratio and the price of the share at optimum payout.

## Answer

(1) The optimum dividend payout ratio is 'Zero', since $\mathrm{r}>\mathrm{K}$.
(2) Calculation of Price of share at optimum payout:

$$
\mathrm{P}=\frac{\mathrm{D}+(\mathrm{E}-\mathrm{D}) \times \frac{\mathrm{r}}{\mathrm{~K}_{\mathrm{e}}}}{\mathrm{~K}_{\mathrm{e}}} \quad=\frac{0+(10-0) \times \frac{0.12}{0.10}}{0.10}=\boldsymbol{₹} 120.00
$$

## BQ 7

The following figures are collected from the annual report of XYZ Ltd.:

| Net Profit | ₹30 lakhs |
| :--- | ---: |
| Outstanding 12\% preference shares | ₹100 lakhs |
| No. of Equity shares | 3 lakhs |
| Return on Investment | $20 \%$ |
| Cost of capital i.e. $\left(\mathrm{K}_{\mathrm{e}}\right)$ | $16 \%$ |

What should be the approximate dividend payout ratio so as to keep the share price at $\mathbf{F}^{2} 2$ by using Walter model?

## Answer



## Dividend Payout ratio:

$$
=\frac{\text { DPS }}{\text { EPS }} \times 100 \quad=\frac{3.12}{6} \times 100 \quad=52 \%
$$

## BQ 8

The following information pertains to $\mathrm{M} / \mathrm{s}$ XY Ltd.

| Earnings of the Company | ₹5,00,000 |
| :--- | ---: |
| Dividend Payout ratio | $60 \%$ |
| No. of shares outstanding | $1,00,000$ |
| Equity capitalization rate | $12 \%$ |
| Rate of return on investment | $15 \%$ |

1. What would be the market value per share as per Walter's model?
2. What is the optimum dividend payout ratio according to Walter's model and the market value of Company's share at that payout ratio?

## Answer

1. Calculation of market value per share as per Walter's model:

| P | $=\frac{\mathrm{D}+(\mathrm{E}-\mathrm{D}) \times \frac{\mathrm{r}}{\mathrm{K}_{\mathrm{e}}}}{\mathrm{K}_{\mathrm{e}}}$ | $=\frac{3+(5-3) \times \frac{0.15}{0.12}}{0.12}$ | $=₹ ₹ 45.83$ |
| :--- | :--- | :--- | :--- |
| EPS | $=\frac{\mathrm{PAT}}{\text { No of Equity Shares }}$ | $=\frac{5,00,000}{1,00,000}$ | $=₹ ₹ 5$ |
| DPS | $=\mathrm{EPS} \times$ Dividend payout ratio $=$ | $\mathrm{F} 5 \times 60 \%$ | $=₹ 3$ |

2. According to Walter's model when the return on investment is more than the cost of equity capital, the price per share increases as the dividend pay-out ratio decreases. Hence, the optimum dividend pay-out ratio in this case is nil.

$$
P(\text { at } 0 \text { Payout })=\frac{D+(E-D) \times \frac{\mathrm{r}}{K_{e}}}{K_{e}} \quad=\frac{0+(5-0) \times \frac{0.15}{0.12}}{0.12}=\text { ₹52.08 }
$$

## BQ 9

The earning per share of a company is $₹ 10$ and the rate of capitalization applicable to it is 10 per cent.

The company has three options of paying dividend i.e. (1) $50 \%$, (2) $75 \%$ and (3) $100 \%$.
Calculate the market price of share as per Walter's model if it can earn a return of (a) 15\%, (b) $\mathbf{1 0 \%}$ and (c) 5\% on its retained earnings.

## Answer

Market value of share (P) $\quad=\quad \frac{\mathrm{D}+(\mathrm{E}-\mathrm{D}) \times \frac{\mathrm{r}}{\mathrm{K}_{\mathrm{e}}}}{\mathrm{K}_{\mathrm{e}}}$
Calculation of Market Value per Share as per Walter's Model

|  | of Earning (r) | DP Ratio 50\% | DP Ratio 75\% | DP Ratio 100\% |
| :---: | :---: | :---: | :---: | :---: |
| (a) $15 \%$ |  | $5+(10-5) \times \frac{.15}{.10}$ | $\underline{7.5+(10-7.5) \times \frac{.15}{.10}}$ | $\underline{10+(10-10) \times \frac{.15}{.10}}$ |
|  |  | . 10 | . 10 | 10 |
|  |  | = ${ }^{1} 125$ | = ₹ 112.50 | = ${ }^{1} 100$ |
| (b) | 10\% | $5+(10-5) \times \frac{.10}{.10}$ | $\underline{7.5+(10-7.5) \times \frac{.10}{.10}}$ | $\underline{10+(10-10) \times \frac{.10}{.10}}$ |
|  |  | . 10 | . 10 | . 10 |
|  |  | = $₹ 100$ | = $₹ 100$ | = $\mathrm{F}^{100}$ |
| (c) | 5\% | $\frac{5+(10-5) \times \frac{.05}{.10}}{10}$ | $\frac{7.5+(10-7.5) \times \frac{.05}{.10}}{10}$ | $\underline{10+(10-10) \times \frac{.05}{.10}}$ |
|  |  |  |  |  |
|  |  | = 775 | = ${ }^{\text {8 }} 87.50$ | = $\mathbf{F}_{100}$ |

## BQ 10

The following information is supplied to you:

| Total Earnings | ₹2,00,000 |
| :--- | ---: |
| No. of equity shares (of ₹100 each) | 20,000 |
| Dividend paid | $₹ 1,50,000$ |
| Price/Earnings ratio | 12.5 |

## Applying Walter's Model:

1. Ascertain whether the company is following an optimal dividend policy.
2. Find out what should be the $\mathrm{P} / \mathrm{E}$ ratio at which the dividend policy will have no effect on the value of the share.
3. Will your decision change, if the $\mathrm{P} / \mathrm{E}$ ratio is 8 instead of 12.5 ?

## Answer

1. $\mathrm{K}_{\mathrm{e}}=\frac{1}{\mathrm{PE}}=\frac{1}{12.5}=8 \%$

$$
r=\frac{\text { Total Earnings }}{\text { Total Funds }} \times 100=\frac{2,00,000}{20,000 \text { Shares } \times 100 \text { per share }} \times 100=10 \%
$$

$r>K_{e}$, Therefore as per Walter model optimum dividend payout is Nil and company is paying dividend to shareholders means company is not following optimum dividend policy.
2. The $P / E$ ratio at which the dividend policy will have no effect on the value of the share is such at which the $\mathrm{k}_{\mathrm{e}}$ would be equal to the rate of return (r) of the firm.
$\mathrm{K}_{\mathrm{e}}=\mathrm{r}$
$=10 \%$
$\mathrm{PE}=\frac{1}{\mathrm{Ke}} \quad=\frac{1}{.10}$
$=10$ times
3. If the $\mathrm{P} / \mathrm{E}$ is 8 instead of 12.5 , then the $\mathrm{K}_{\mathrm{e}}$ which is the inverse of $\mathrm{P} / \mathrm{E}$ ratio, would be 12.5 :

$$
\mathrm{K}_{\mathrm{e}} \quad=\frac{1}{\mathrm{PE}} \quad=\frac{1}{8} \quad=12.5 \%
$$

In such a situation $K_{e}>r$ and optimum dividend payout will be 100\%.

## GORDON MODEL

BQ 11
X ltd. is a no growth company, pays a dividend of $₹ 5$ per share. If the cost of capital is $10 \%$, what should be the current market price of the share?

## Answer

$$
\begin{array}{ccccc}
P_{0} & = & \frac{D}{K_{e}} & = & \frac{5}{0.10}
\end{array}
$$

## BQ 12

XYZ is company having share capital of ₹10 lakhs of ₹10 each. It distributed current dividend of 20\% per annum. Annual growth rate in dividend expected is $2 \%$. The expected rate of return on its equity capital is $15 \%$, what should be the current market price of the share?

## Answer

$$
\mathrm{P}_{\mathrm{o}} \quad=\quad \frac{\mathrm{D}_{0}(1+\mathrm{g})}{\mathrm{K}_{\mathrm{e}}-\mathrm{g}}=\quad \frac{2(1+.02)}{0.15-0.02}=
$$

## BQ 13

A firm had paid dividend at ₹2 per share last year. The estimated growth of the dividends from the company is estimated to be $5 \%$ p.a. Determine the estimated market price of the equity share with $5 \%$ growth rate and if the estimated growth rate of dividends (i) rises to $8 \%$, and (ii) falls to $3 \%$. Also find out the present market price of the share, given that the required rate of return of the equity investors is $15 \%$.

## Answer

$$
\mathrm{P}_{\mathrm{o}} \quad=\quad \frac{\mathrm{D}_{0}(1+\mathrm{g})}{\mathrm{K}_{\mathrm{e}}-\mathrm{g}}=\quad \frac{2(1+.05)}{0.15-0.05} \quad=\quad ₹ 21
$$

1. MPS with $8 \%$ growth rate:

$$
\mathrm{P}_{\mathrm{o}} \quad=\quad \frac{\mathrm{D}_{0}(1+\mathrm{g})}{\mathrm{K}_{\mathrm{e}}-\mathrm{g}}=\quad \frac{2(1+.08)}{0.15-0.08} \quad=\quad \text { F30.86 }
$$

2. MPS with $3 \%$ growth rate:

$$
\mathrm{P}_{\mathrm{o}} \quad=\quad \frac{\mathrm{D}_{0}(1+\mathrm{g})}{\mathrm{K}_{\mathrm{e}}-\mathrm{g}}=\quad \frac{2(1+.03)}{0.15-0.03} \quad=\quad ₹ 17.17
$$

## BQ 14

By taking the following data of three different firms i.e. growth, normal and declining firm calculate the current price of share by using the Gordon model after that again calculate revised price of share with 0.4 retained earning and check the relationship between Gordon and Walter model.

| Factors | Growth Firm <br> $\boldsymbol{r}>\boldsymbol{K}_{\boldsymbol{e}}$ | Normal Firm <br> $\boldsymbol{r}=\boldsymbol{K}_{\boldsymbol{e}}$ | Declining <br> Firm <br> $\boldsymbol{r}<\boldsymbol{K}_{\boldsymbol{e}}$ |
| :--- | :---: | :---: | :---: |
| R (Rate of Return on Retained Earnings) | $15 \%$ | $10 \%$ | $8 \%$ |
| K (Cost of Capital) | $10 \%$ | $10 \%$ | $10 \%$ |
| E (Earning Per Share) | $₹ 10$ | $₹ 10$ | $₹ 10$ |
| B (Retained Earning) | 0.6 | 0.6 | 0.6 |
| 1- B | 0.4 | 0.4 | 0.4 |

## Answer

## Calculation of current price of share as per Gordon model:

| $\mathrm{P}_{\mathrm{o}}$ | $=$ | $\frac{D_{1}}{K_{e}-g}$ |  |
| :--- | :--- | :--- | :--- |
| Growth | $=$ | $\frac{10 \times 0.4}{0.10-0.09}$ | $=$ |
| Normal 400 |  |  |  |
| Declining | $=$ | $\frac{10 \times 0.4}{0.10-0.06}$ | $=$ |
|  | $=$ | $\frac{10 \times 0.4}{0.10-0.048}$ |  |
|  |  | $=$ | $₹ 76.92$ |

## Working note:

| G | $=$ | $\mathrm{b} \times \mathrm{r}$ |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Growth | $=$ | $15 \% \times .6$ | $=$ | $9 \%$ |
| Normal | $=$ | $10 \% \times .6$ | $=$ | $6 \%$ |
| Declining | $=$ | $8 \% \times .6$ | $=$ | $4.8 \%$ |

Calculation of revised price of share as per Gordon model when b is 0.4 and payout is 0.6:

| Growth | $=$ | $\frac{10 \times 0.6}{0.10-0.06}$ | $=₹$ |
| :--- | :--- | :--- | :--- |
| 1 150 |  |  |  |
| Normal | $=$ | $\frac{10 \times 0.6}{0.10-0.04}$ | $=₹ ₹ 100$ |
| Declining | $=$ | $\frac{10 \times 0.6}{0.10-0.032}$ | $=$ |

Working note:

| G | $=$ | $\mathrm{b} \times \mathrm{r}$ |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Growth | $=$ | $15 \% \times .4$ | $=$ | $6 \%$ |
| Normal | $=$ | $10 \% \times .4$ | $=$ | $4 \%$ |
| Declining | $=$ | $8 \% \times .4$ | $=$ | $3.2 \%$ |

From the above analysis it can be concluded that:

When $r>k$, the market value increases with retention ratio, when $r<k$, the market value of share stands to decrease and when $r=k$, the market value is not affected by dividend policy.

The conclusion of the Gordon's model is similar to that of Walter's model.

## BQ 15

The following figures are collected from the annual report of XYZ Ltd.:

| Net Profit | $₹ 30,00,000$ |
| :--- | ---: |
| Outstanding 12\% Preference Shares | $₹ 1,00,00,000$ |
| No. of Equity Shares | $3,00,000$ |
| Return on Investment | $20 \%$ |
| Cost of Capital | $16 \%$ |

Calculate price per share using Gordon's Model when dividend payout is (1) 25\%, (2) 50\% and (3) $100 \%$.

## Answer

Calculation of Price of Share as per Gordon model:

$$
\mathrm{P}_{\mathrm{o}} \quad=\frac{D_{1}}{K_{e}-g}
$$

(1) When $25 \%$ payout $=\frac{6 \times 0.25}{0.16-0.15}=$ ₹150
(2) When $50 \%$ payout $=\frac{6 \times 0.50}{0.16-0.10}=$ F50
(3) When $100 \%$ payout $=\frac{6 \times 1.00}{0.16-0.00}=$ F37.50

## Working note:

(a) Growth $=\mathrm{b} \times \mathrm{r}$

| When $25 \%$ payout $=$ | $20 \% \times .75$ | $=$ |
| :--- | :--- | :--- |
| When $50 \%$ payout | $=$ | $15 \%$ |
| When $100 \%$ payout | $=10 \% \times .50$ | $=$ |
| $20 \% \times .00$ | $=$ | $0 \%$ |

(b) Earning Per Share $=(\mathrm{PAT}-\mathrm{PD}) \div$ Number of shares

$$
=\quad(30,00,000-12 \% \text { of } 1,00,00,000) \div 3,00,000 \quad=\quad ₹ 6
$$

## BQ 16

The annual report of XYZ Ltd. provides the following information for the Financial Year 2020-21:

| Net Profit | ₹50,00,000 |
| :--- | ---: |
| Outstanding 15\% Preference Shares | ₹1,00,00,000 |
| No. of Equity Shares | $5,00,000$ |
| Return on Investment | $20 \%$ |
| Cost of Capital i.e. (Ke) | $16 \%$ |

Calculate price per share using Gordon's Model when dividend payout is (1) 25\%, (2) 50\% and (3) 100\%.

Answer
Calculation of Price of Share as per Gordon model:

$$
P_{o} \quad=\quad \frac{D_{1}}{K_{e}-g}
$$

(1) When $25 \%$ payout $=\frac{7 \times 0.25}{0.16-0.15} \quad=\quad ₹ 175$
(2) When $50 \%$ payout $=\frac{7 \times 0.50}{0.16-0.10} \quad$ ₹58.33
(3) When $100 \%$ payout $=\frac{7 \times 1.00}{0.16-0.00} \quad=\quad 43.75$

## Working note:

(a) Growth $=\mathrm{b} \times \mathrm{r}$

| When $25 \%$ payout | $=$ | $20 \% \times .75$ | $=$ |
| :--- | :--- | :--- | :--- |
|  | $15 \%$ |  |  |
| When $50 \%$ payout | $=$ | $10 \% \times .50$ | $=$ |
| When $100 \%$ payout | $=$ | $20 \% \times .00$ |  |

(b) Earning Per Share $=(\mathrm{PAT}-\mathrm{PD}) \div$ Number of shares

$$
=\quad(50,00,000-15 \% \text { of } 1,00,00,000) \div 5,00,000 \quad=\quad ₹ 7
$$

BQ 17
A N Ltd. gives you the following information:
The appropriate market rate of discount is $8 \%$ and that the company is expected to enjoy an above-average performance for eight years with dividends growing at say $10 \%$ per annum. After that time, because of competition and the company losing its present technological or marketing lead, the growth in dividends will revert to the average for all companies-say $4 \%$. The present dividend is ₹ 0.10 per share.

Compute the current value of equity share of the company.
Answer
Calculation of Present Value or Current Market Value of Share

| Year | Expected benefits | PVF @ 8\% | DCF |
| :---: | :---: | :---: | :---: |
| 1 | $0.10+10 \%$ = ₹ 0.11 | 0.926 | 0.101 |
| 2 | $0.11+10 \%=₹ 0.121$ | 0.857 | 0.103 |
| 3 | $0.121+10 \%=₹ 0.133$ | 0.794 | 0.106 |
| 4 | $0.133+10 \%=₹ 0.146$ | 0.735 | 0.107 |
| 5 | $0.146+10 \%$ = ₹ 0.161 | 0.681 | 0.110 |
| 6 | $0.161+10 \%$ = ₹ 0.177 | 0.630 | 0.112 |
| 7 | $0.177+10 \%=₹ 0.195$ | 0.583 | 0.114 |
| 8 | $0.195+10 \%$ = ₹ 0.214 | 0.540 | 0.116 |
| (9 to $\infty$ ) | $\mathrm{P}_{8}=₹ 5.55$ | 0.540 | 3.00 |
| Present value of all future benefits or Current market value of Share |  |  | ₹3.87 |

$\mathrm{P}_{8} \quad=\quad \frac{\mathrm{D}_{9}}{\mathrm{~K}_{\mathrm{e}}-\mathrm{g}} \quad=\frac{.214+4 \%}{8 \%-4 \%} \quad=\quad$ ₹5.55

BQ 18
A\&R Ltd. is a large-cap multinational company listed in BSE in India with a face value of ₹ 100 per share. The company is expected to grow @ $15 \%$ p.a. for next four years then $5 \%$ for an indefinite period. The shareholders expect $20 \%$ return on their share investments. Company paid ₹ 120 as dividend per share for the FY 2022-23. The shares of the company traded at an average price of ₹ 3,122 on last day.

Find out the intrinsic value of per share and state whether shares are overpriced or under-priced.

## Answer

Calculation of Present Value or Current Market Value or Intrinsic Value of Share

| Year | Expected benefits | PVF @ 20\% | DCF |
| :---: | :--- | :---: | :---: |
| 1 | $120.00+15 \%=₹ 138.00$ | 0.833 | 114.95 |
| 2 | $138.00+15 \%=₹ 158.70$ | 0.694 | 110.14 |
| 3 | $158.70+15 \%=₹ 182.50$ | 0.579 | 105.67 |
| 4 | $182.50+15 \%=₹ 209.88$ | 0.482 | 101.16 |
| $(5$ to $\infty)$ | $\mathrm{P}_{4}=₹ 1,469.16$ | 0.482 | 708.13 |
| Present value of all future benefits or Intrinsic value of Share |  | $\mathfrak{₹} 1,140.05$ |  |

$$
P_{4} \quad=\frac{D_{5}}{K_{e}-g}=\frac{209.88+5 \%}{20 \%-5 \%}=₹ 1,469.16
$$

Intrinsic value of share is $₹ 1,140.05$ as compared to latest market price of ₹ 3,122 . Market price of a share is overpriced by $₹ 1,981.95$.

## TRADITIONAL MODEL (GRAHAM AND DODD MODEL)

## BQ 19

The following information regarding the equity shares of M ltd. is given that Market price is ₹58.33, Dividend per share is $₹ 5$ and Multiplier is 7.

According to the Graham \& Dodd approach to the dividend policy, compute the EPS.

## Answer

$P \quad=\quad M(D+E / 3)$
$58.33=7(5+\mathrm{E} / 3)$
E = ₹9.99 or ₹10 approx.

## BQ 20

The earning per share of a company is ₹ 30 and dividend payout is $60 \%$. Multiplier is 2 .
Determine the price per share as per Graham \& Dodd model.

## Answer

| Price per share $(P)$ | $=$ | $M(D+E / 3)$ |
| :---: | :--- | :--- |
| $P$ | $=2(30 \times 0.60+30 / 3)$ | $=\quad ₹ 56$ |
| $P$ | $=$ | $2(18+10)$ |

## BQ 21

The dividend payout ratio of H Ltd. is $40 \%$. If the company follows traditional approach to dividend policy with a multiplier of 9 , what will be the $\mathrm{P} / \mathrm{E}$ ratio.

## Answer

Since the dividend payout ratio is $40 \%$

| D | = | 40\% of E i.e. 0.4E |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| P | = | $M(D+E / 3)$ |  | $9(\mathrm{D}+\mathrm{E} / 3)$ | = | $9(0.4 \mathrm{E}+\mathrm{E} / 3)$ |  |  |
| P | = | $9(0.4 \mathrm{E}+\mathrm{E} / 3)$ |  | $9\left(\frac{1.2 \mathrm{E}+\mathrm{E}}{3}\right)$ | = | 3 (2.2E) | = | 6.6E |
| P/E ratio | = | $\frac{\text { MPS }}{\text { EPS }}$ | = | $\frac{\mathrm{P}}{\mathrm{E}}$ | = | $\frac{6.6 \mathrm{E}}{\mathrm{E}}$ | = | 6.6times |

## LINTER'S MODEL

BQ 22
Given the last year's dividend is ₹9.80, speed of adjustment $=45 \%$, target payout ratio $60 \%$ and EPS for current year ₹20.

Calculate current year's dividend using Linter's model.

## Answer

$$
\begin{aligned}
\mathrm{D}_{1} & =\mathrm{D}_{0}+\left[(\text { EPS } \times \text { Target payout })-\mathrm{D}_{0}\right] \times \mathrm{Af} \\
& =9.80+[(20 \times 60 \%)-9.80] \times 0.45
\end{aligned}=\quad \mathbf{F} 10.79
$$

## MISCELLANEOUS

BQ 23
With the help of following figures calculate the market price of a share of a company by using:

1. Walter's formula
2. Dividend growth model (Gordon's formula)

| Earning per share (EPS) | ₹10 |
| :--- | ---: |
| Dividend per share (DPS) | ₹6 |
| Cost of capital (k) | $20 \%$ |
| Internal rate of return on investment | $25 \%$ |
| Retention Ratio | $40 \%$ |

## Answer

(a) Walter's formula:

$$
\mathrm{P} \quad=\frac{\mathrm{D}+(\mathrm{E}-\mathrm{D}) \times \frac{\mathrm{r}}{\mathrm{~K}_{\mathrm{e}}}}{\mathrm{~K}_{\mathrm{e}}}=\frac{6+(10-6) \times \frac{0.25}{0.20}}{0.20}=\mathbb{F} 55
$$

## (b) Gordon's formula (Dividend Growth model):

| $\mathrm{P}_{\mathrm{o}}$ | $=\frac{\mathrm{D}_{1}}{\mathrm{~K}_{\mathrm{e}}-\mathrm{g}}$ | $=$ | $\frac{6}{0.20-0.10}$ | $=$ |
| :--- | :--- | :--- | :--- | :--- |
| G 60 |  |  |  |  |
|  | $=$ | $\mathrm{b} \times \mathrm{r}$ | $=$ | $25 \% \times .4$ |

## BQ 24

The following information is given below in case of Aditya Ltd.:

| Earnings per share | $₹ 60$ |
| :--- | :--- |
| Capitalisation rate | $15 \%$ |
| Return on investment | $25 \%$ |
| Dividend payout ratio | $30 \%$ |

(a) Compute price per share using Walter's Model.
(b) What would be optimum dividend payout ratio per share under Gordon's Model.

## Answer

(a) Price per share using Walter's Model:

$$
\mathrm{P}=\frac{\mathrm{D}+(\mathrm{E}-\mathrm{D}) \times \frac{\mathrm{r}}{\mathrm{~K}_{\mathrm{e}}}}{\mathrm{~K}_{\mathrm{e}}}=\frac{18+(60-18) \times \frac{0.25}{0.15}}{0.15}=\text { ₹586.67 }
$$

(b) As per Gordon's model, when r > Ke, optimum dividend payout ratio is 'Zero'.

BQ 25
In the month of May of the current financial year, shares of RT Ltd. was sold for ₹ 1,460 per share. A long term earnings growth rate of $7.5 \%$ is anticipated. RT Ltd. is expected to pay dividend of $₹ 20$ per share.
(a) Calculate rate of return an investor can expect to earn assuming that dividends are expected to grow along with earnings at $7.5 \%$ per year in perpetuity?
(b) It is expected that RT Ltd. will earn about $10 \%$ on retained earnings and shall retain $60 \%$ of earnings. In this case, State whether, there would be any change in growth rate and cost of Equity?

## Answer

(a) $\mathrm{K}_{\mathrm{e}}=\frac{\mathrm{D}_{1}}{\mathrm{P}_{\mathrm{o}}}+\mathrm{g}=\frac{20}{1,460}+7.5 \%=8.87 \%$
(b) With rate of return on retained earnings (r) 10\% and retention ratio (b) 60\%, new growth rate will be as follows:
$g$ (revised growth rate $)=\mathrm{b} \times \mathrm{r}=0.10 \times 0.60=0.06$ or $6 \%$
Accordingly, dividend will also get changed and to calculate this, first we shall calculate previous retention ratio ( $\mathrm{b}_{1}$ ) and then EPS assuming that rate of return on retained earnings (r) is same. With previous growth rate of $7.5 \%$ and $\mathrm{r}=10 \%$, the retention ratio comes out to be:


## BQ 26

Mr H is currently holding $1,00,000$ shares of HM ltd, and currently the share of HM ltd is trading on Bombay Stock Exchange at ₹ 50 per share. Mr A have a policy to re-invest the amount of any dividend received into the shared back again of HM ltd. If HM ltd has declared a dividend of ₹10 per share.

Determine the no of shares that Mr A would hold after he re-invests dividend in shares of HM Itd.

## Answer

| Ex-dividend price of Share | $=$ | $₹ 40(50-10)$ |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Dividend received | $=$ | $₹ 10,00,000(1,00,000$ shares $\times ₹ 10)$ |  |  |
| Additional shares purchased | $=$ | $₹ 10,00,000 \div ₹ 40$ | $=$ | 25,000 |
| Total holding | $=$ | $1,00,000+25,000$ | $=$ | $\mathbf{1 , 2 5 , 0 0 0}$ Shares |

BQ 27
Following information is given pertaining to DG ltd:

| No of shares outstanding | $:$ | 1 lakh shares |
| :--- | :--- | :--- |
| Earnings Per share | $:$ | ₹25 per share |
| P/E Ratio | $:$ | 20 |
| Book Value per share | $:$ | ₹400 per share |

If company decides to repurchase 25,000 shares, at the prevailing market price, what is the resulting book value per share after repurchasing?

## Answer

| Current Market price | $=$ | $\mathrm{EPS} \times \mathrm{P} / \mathrm{E}=25 \times 20$ <br> $₹ 500$ per share |
| :--- | :--- | :--- |
| Amount paid for repurchase | $=$ | $₹ 1,25,00,000(25,000$ shares $\times ₹ 500$ per share $)$ |
| Book value before repurchase | $=$ | $₹ 4,00,00,000(₹ 400 \times 1$ lakh shares $)$ |
| Book Value after repurchase | $=$ | $₹ 2,75,00,000(4$ Cr. -1.25 Cr.$)$ |
| No of shares after repurchase | $=$ | 75,000 shares |
| Book value per share | $=$ | $2,75,00,000 \div 75,000$ |
|  | $=\quad ₹ 367$ per share |  |

## PAST YEAR QUESTIONS

## PYQ 1

Following information relating to Jee Ltd. are given:

| Profit after tax | $:$ | $₹ 10,00,000$ |
| :--- | :--- | :--- |
| Dividend payout ratio | $:$ | $50 \%$ |
| Number of Equity shares | $:$ | 50,000 |
| Cost of equity | $:$ | $10 \%$ |
| Rate of return on investment | $:$ | $12 \%$ |

(1) What would be the market value per share as per as per Walter's Model?
(2) What is the optimum dividend payout ratio according to Walter's Model and market value of equity share at that payout ratio?
[(5 Marks) Nov 2018]

## Answer

(1) Market value (P) per share as per Walter's Model:

$$
\begin{aligned}
P(\text { Market value of share }) & =\frac{\mathrm{D}+(\mathrm{E}-\mathrm{D}) \times \frac{\mathrm{r}}{\mathrm{~K}_{\mathrm{e}}}}{\mathrm{~K}_{\mathrm{e}}}=\frac{10+(20-10) \times \frac{0.12}{0.10}}{0.10} \\
& =₹ 220.00 \\
\mathrm{E}(\mathrm{EPS}) & =₹ 10,00,000 \text { (PAT) } \div 50,000 \text { shares } \\
& =₹ 20
\end{aligned}
$$

(2) According to Walter's Model when the return on investment is more than the cost of equity capital, the price per share increases as the dividend payout ratio decreases. Hence, the optimum dividend payout ratio in this case Nil. So, at a payout ratio zero, the market value of company's share will be:
$\begin{aligned} \mathrm{P}(\text { Market value of share }) & =\frac{D+(E-D) \times \frac{r}{K_{e}}}{K_{e}}=\frac{0+(20-0) \times \frac{0.12}{0.10}}{0.10} \\ & =₹ 240.00\end{aligned}$

## PYQ 2

The following information is supplied to you:

| Total Earning | $:$ | $₹ 40,00,000$ |
| :--- | :--- | :--- |
| Number of Equity Shares (of ₹100 each) | $:$ | $4,00,000$ |
| Dividend Per Share | $:$ | $₹ 4$ |
| Cost of Capital | $:$ | $16 \%$ |
| Internal Rate of Return | $:$ | $20 \%$ |
| Retention Ratio | $:$ | $60 \%$ |

## Calculate the market price of a share of company by using:

(1) Walter's Formula,
(2) Gordon' Formula.

## Answer

(1) Market Price of Share (P) as per Walter's Formula:

$$
\begin{aligned}
\mathrm{P}(\text { Market value of share }) & =\frac{\mathrm{D}+(\mathrm{E}-\mathrm{D}) \times \frac{\mathrm{r}}{\mathrm{~K}_{\mathrm{e}}}}{\mathrm{~K}_{\mathrm{e}}}=\frac{4+(10-4) \times \frac{0.20}{0.16}}{0.16} \\
& =₹ 1.875 \\
\mathrm{E} \text { (EPS) } & =₹ 40,00,000 \text { (Earning) } \div 4,00,000 \text { shares } \\
& =₹ 10
\end{aligned}
$$

(2) Market Price of Share (P) as per Gordon's Formula:

$$
\begin{array}{llll}
\mathrm{P}_{0}(\text { Market value of share }) & =\frac{\mathrm{D}_{1}}{\mathrm{~K}_{\mathrm{e}}-\mathrm{g}} & =\frac{4.00}{0.16-0.12}=\mathrm{F} 100.00 \\
\mathrm{G} \text { (Growth Rate) } & =\mathrm{b} \times \mathrm{r} & =20 \% \times .6=12 \%
\end{array}
$$

PYQ 3
Following figures and information were extracted from the company A Ltd.
Earnings of the company
₹ $10,00,000$
Dividend paid
₹ $6,00,000$
No. of shares outstanding 2,00,000
Price earnings ratio 10
Rate of return on investment
20\%

You are required to calculate:
(1) Current market price of the share.
(2) Capitalization rate of its risk class.
(3) What should be the optimum payout ratio?
(4) What should be the market price per share at optimal payout ratio? (use Walter's model)
[(5 Marks) Nov 2019]
Answer
(1) Current market price of share:

| Current Market Price of Share | $=$ | EPS $\times$ PE Ratio |
| ---: | :--- | :--- |
|  | $=\frac{10,00,000}{2,00,000} \times 10$ |  |$\quad$|  |
| :--- |

(2) Capitalization rate of its risk class:

Capitalization rate $\left(\mathrm{K}_{\mathrm{e}}\right) \quad=\quad 1 / \mathrm{PE}$ $=1 / 10 \quad=\quad 0.10$ or $\mathbf{1 0} \%$
(3) Optimum payout:
$r>K_{e}$, Therefore dividend payout should be Nil.
(4) Market Price of Share (P) as per Walter's Formula as per optimal payout ratio:
$\begin{aligned} P \text { (Market price of share) } & =\frac{\mathrm{D}+(\mathrm{E}-\mathrm{D}) \times \frac{\mathrm{r}}{\mathrm{K}_{\mathrm{e}}}}{\mathrm{K}_{\mathrm{e}}} \\ & =\mathrm{F}^{2} 100^{2}\end{aligned}$
$=\quad \frac{0+(5-0) \times \frac{0.20}{0.10}}{0.10}$

## PYQ 4

The following figures are extracted from the annual report of RJ Ltd.:

| Net Profit | ₹50 lakhs |
| :--- | ---: |
| Outstanding 13\% preference shares | ₹200 lakhs |
| No. of Equity shares | 6 lakhs |
| Return on Investment | $25 \%$ |
| Cost of capital i.e. $\left(\mathrm{K}_{\mathrm{e}}\right)$ | $15 \%$ |

You are required to compute the approximate dividend payout ratio by keeping the share price at $\mathrm{F}^{2} 0$ by using Walter model?
[(5 Marks) Nov 2020]

## Answer

$$
\begin{aligned}
& \text { EPS }=\frac{\text { PAT-Preference Dividend }}{\text { No of Equity Shares }}=\frac{50,00,000-13 \% \text { of } 2,00,00,000}{6,00,000}=\mathcal{F} 4 \\
& P=\frac{D+(E-D) \times \frac{r}{K_{e}}}{K_{e}}=\frac{D+(4-D) \times \frac{0.25}{0.15}}{0.15}=40 \\
& 6=\frac{0.15 \mathrm{D}+1-0.25 \mathrm{D}}{0.15} \\
& 0.9=1-0.10 \mathrm{D} \text { or } \quad \mathrm{D}=1 \\
& \text { Dividend Payout ratio }=\frac{\text { DPS }}{\text { EPS }} \times 100=\frac{1}{4} \times 100=25 \%
\end{aligned}
$$

## PYQ 5

The following information is taken from ABC Ltd.

| Net Profit for the year | $₹ 30,00,000$ |
| :--- | :--- |
| $12 \%$ Preference shares capital | $₹ 1,00,00,000$ |
| Equity share capital (Share of ₹10 each) | $₹ 60,00,000$ |
| Internal rate of return on investment | $22 \%$ |
| Cost of Equity capital | $18 \%$ |
| Retention ratio | $75 \%$ |

## Calculate the market price of the share using:

1. Gordon's Model
2. Walter's Model
[(5 Marks) Jan 2021]

## Answer

1. Calculation of Price of share as per Gordon model:

$$
\begin{array}{llll}
\mathrm{P}_{\mathrm{o}} & =\frac{\mathrm{D}_{1}}{\mathrm{~K}_{\mathrm{e}}-\mathrm{g}} & =\frac{3 \times 0.25}{0.18-0.165} & =\quad \mathrm{F} 50
\end{array}
$$

## 2. Calculation of Price of share as per Walter model:

$$
\mathrm{P}=\frac{\mathrm{D}+(\mathrm{E}-\mathrm{D}) \times \frac{\mathrm{r}}{\mathrm{~K}_{\mathrm{e}}}}{\mathrm{~K}_{\mathrm{e}}}=\frac{0.75+(3-0.75) \times \frac{0.22}{0.18}}{0.18}=\text { ₹ } 19.44
$$

## Working note:

(a) Growth $=\mathrm{b} \times \mathrm{r}=22 \% \times .75=16.50 \%$
(b) EPS $=(\mathrm{PAT}-\mathrm{PD}) \div$ Number of shares
$=(30,00,000-12 \%$ of $1,00,00,000) \div 6,00,000=₹ 3$
(c) DPS = EPS $\times$ Payout ratio $=$ ₹ $3 \times 25 \%=$ ₹ 0.75

## PYQ 6

The following information relates to LMN Ltd.

| Earnings of the Company | ₹30,00,000 |
| :--- | ---: |
| Dividend Payout ratio | $60 \%$ |
| No. of shares outstanding | $5,00,000$ |
| Rate of return on investment | $15 \%$ |
| Equity capitalized rate | $13 \%$ |

## Required:

1. Determine what would be the market value per share as per Walter's model?
2. Compute optimum dividend payout ratio according to Walter's model and the market value of company's share at that payout ratio?
[(5 Marks) July 2021]

## Answer

1. Calculation of market value per share as per Walter's model:

| P | = | $\underline{\mathrm{D}+(\mathrm{E}-\mathrm{D}) \times \frac{\mathrm{r}}{\mathrm{~K}_{\mathrm{e}}}}$ | = | $\frac{3.60+(6-3.60) \times \frac{0.15}{0.13}}{0.13}$ | = | ₹48.99 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathrm{K}_{\mathrm{e}}$ |  |  |  |  |
| EPS | $=$ | PAT | $=$ | 30,00,000 | = | ₹6 |
|  |  | No of Equity Shares | = | 5,00,000 | $=$ | ₹ |
| DPS | = | EPS $\times$ Dividend |  | ₹ $6 \times 60 \%$ | = | ₹3.60 |

2. According to Walter's model when the return on investment is more than the cost of equity capital, the price per share increases as the dividend pay-out ratio decreases. Hence, the optimum dividend payout ratio in this case is nil.

$$
P(\text { at } 0 \text { Payout })=\frac{D+(E-D) \times \frac{r}{K_{e}}}{K_{e}} \quad=\frac{0+(6-0) \times \frac{0.15}{0.13}}{0.13} \quad=\quad \text { F53.25 }
$$

## PYQ 7

X Ltd. is a manufacturing company. Current market price per share is ₹ 2,185 . During the F.Y. 2020-21, the company paid ₹ 140 as dividend per share. The company is expected to grow @12\% p.a. for next four years, then $5 \%$ p.a. for an indefinite period. Expected rate of return of shareholders is $18 \%$ p.a.
(i) Find out intrinsic value per share.
(ii) State whether shares are overpriced or underpriced.

| Year | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Discounting Factor@18\% | 0.847 | 0.718 | 0.608 | 0.515 | 0.436 |

[(5 Marks) Dec 2021]

## Answer

## (i) Calculation of Intrinsic Value of Share

| Year | Expected benefits | PVF @ 18\% | DCF |
| :---: | :---: | :---: | :---: |
| 1 | $140.00+12 \%=₹ 156.80$ | 0.847 | 132.81 |
| 2 | $156.80+12 \%=₹ 175.62$ | 0.718 | 126.10 |
| 3 | $175.62+12 \%=₹ 196.69$ | 0.608 | 119.59 |
| 4 | $196.69+12 \%=₹ 220.29$ | 0.515 | 113.45 |
| $(5$ to $\infty)$ | $\mathrm{P}_{4}=₹ 1,779.27$ | 0.515 | 916.32 |
| Present value of all future benefits or Intrinsic value of Share |  | $₹ 1,408.27$ |  |

$$
\mathrm{P}_{4} \quad=\quad \frac{D_{5}}{K_{e}-g}=\frac{220.29+5 \%}{18 \%-5 \%} \quad=\quad ₹ 1,779.27
$$

(ii) Intrinsic value of share is ₹ $1,408.27$ as compared to latest market price of ₹ 2,185 . Market price of a share is overpriced by ₹ 776.73 .

## PYQ 8

Following information are given for a company:

| Earnings per share | ₹ 10 |
| :--- | :---: |
| P/E ratio | 12.5 |
| Rate of return on investment | $12 \%$ |
| Market price per share as per Walter's model | ₹ 130 |

## You are required to calculate:

(a) Dividend payout ratio.
(b) Market price of share at optimum dividend payout ratio.
(c) $\mathrm{P} / \mathrm{E}$ ratio, at which the dividend policy will have no effect on the price of share.
(d) Market Price of share at this $\mathrm{P} / \mathrm{E}$ ratio.
(e) Market price of share using Dividend growth model.
[(5 Marks) May 23]

## Answer

(a)

| Market price of share (P) | $=\frac{\mathrm{D}+(\mathrm{E}-\mathrm{D}) \times \frac{\mathrm{r}}{\mathrm{K}_{\mathrm{e}}}}{\mathrm{K}_{e}}$ |
| ---: | :--- |
| 130 | $=\frac{\mathrm{D}+(10-\mathrm{D}) \times \frac{0.12}{0.08}}{0.08}$ |
| 10.40 | $=$ |
| 10.40 | $=$ |
| .5D | $=(10-\mathrm{D}) \times \frac{0.12}{0.08}$ |
| D | $=15-1.5 \mathrm{D}$ |
|  | $=$ |

$$
=\frac{9.20}{10.00} \times 100
$$

## Working Note:

$\mathrm{K}_{\mathrm{e}}=1 / \mathrm{PE} \quad=1 / 12.5=8 \%$
(b) $\mathrm{r}>\mathrm{K}_{\mathrm{e}}$, Therefore as per Walter model optimum dividend payout is Nil

Market price of share (P) $\quad=\frac{\mathrm{D}+(\mathrm{E}-\mathrm{D}) \times \frac{\mathrm{r}}{\mathrm{K}_{\mathrm{e}}}}{\mathrm{K}_{\mathrm{e}}}=\frac{0+(10-0) \times \frac{0.12}{0.08}}{0.08}=\boldsymbol{₹} 187.5$
(c) The P/E ratio at which the dividend policy will have no effect on the value of the share is such at which the $\mathrm{k}_{\mathrm{e}}$ would be equal to the rate of return ( r ) of the firm.
$\mathrm{K}_{\mathrm{e}} \quad=\quad \mathrm{r} \quad=\quad 12 \%$
PE $=1 / K_{e} \quad=1 / 12 \% \quad=\quad 8.33$ times
(d) Market price of share $(\mathrm{P}) \quad=\quad \mathrm{EPS} \times \mathrm{PE}=10 \times 8.33=\quad$ ₹ 83.33
(e) Market price of share using Dividend growth model:

$$
\mathrm{P}_{\mathrm{o}} \quad=\frac{\mathrm{D}_{1}}{\mathrm{~K}_{\mathrm{e}}-\mathrm{g}} \quad=\quad \frac{9.20}{0.08-0.0096} \quad=\quad ₹ 130.68
$$

## Working note:

$\mathrm{G}=\mathrm{b} \times \mathrm{r}=12 \% \times .08=0.96 \%$

## PYQ 9

(a) EPS of a company is ₹ 60 and Dividend payout ratio is $60 \%$. Multiplier is 5 . Determine price per share as per Graham \& Dodd model.
(b) Last Year's dividend is ₹6.34, adjustment factor is $45 \%$, target payout ratio is $60 \%$ and current year's EPS is ₹12. Compute current's year's dividend using Linter's model.
[(5 Marks) Nov 23]

## Answer

(a) P
$=\quad M(D+E / 3)$
$=5(36+60 / 3)$
$=\quad$ ₹280
(b) $\quad \mathrm{D}_{1} \quad=\quad \mathrm{D}_{0}+\left[(\right.$ EPS $\times$ Target payout $\left.)-\mathrm{D}_{0}\right] \times \mathrm{Af}$

$$
=6.34+[(12 \times 60 \%)-6.34] \times 0.45=\text { ₹ } 6.73
$$

PYQ 10
INFO Ltd is a listed company having share capital of ₹ 2,400 Crores of ₹ 5 each. During the year:

| Dividend distributed | $1000 \%$ |
| :--- | :--- |
| Expected Annual growth rate in dividend | $14 \%$ |
| Expected rate of return on its equity capital | $18 \%$ |

## Required:

(a) Calculate price of share applying Gordon's growth Model.
(b) What will be the price of share if the Annual growth rate in dividend is only $10 \%$ ?
(c) According to Gordon's growth Model, if Internal Rate of Return is 25\%, than what should be the optimum dividend payout ratio in case of growing stage of company? Comment.
[(5 Marks) Nov 23]
Answer
(a) $\mathrm{P}_{\mathrm{o}}=\frac{\mathrm{D}_{0}(1+\mathrm{g})}{\mathrm{K}_{\mathrm{e}}-\mathrm{g}}=\frac{50(1+.14)}{0.18-0.14}=\mathrm{F} 1,425$
(b) $\mathrm{P}_{\mathrm{o}}=\frac{\mathrm{D}_{0}(1+\mathrm{g})}{\mathrm{K}_{\mathrm{e}}-\mathrm{g}}=\frac{50(1+.10)}{0.18-0.10}=\mathrm{F} 687.50$
(c) When $\mathrm{r}(25 \%)$ is higher than $\mathrm{Ke}(18 \%)$ in case of growing stage company, Optimum payout is Nil.

## Working Notes:

$\mathrm{D}_{0} \quad=\quad 1,000 \%$ of $₹ 5=$ ₹ 50

## SUGGESTED REVISION FOR EXAM:

BQ: 1, 5, 7, 10, 14, 17, 18, 21, 22, 25, 27

PYQ: 6, 8

TABLE 1

Table I - Present Value Table (PVIF)
Present Value of $₹ 1$ at the end of $n$ years

| Years | $\mathbf{5 \%}$ | $\mathbf{6 \%}$ | $\mathbf{7 \%}$ | $\mathbf{8 \%}$ | $\mathbf{9 \%}$ | $\mathbf{1 0} \boldsymbol{\%}$ | $\mathbf{1 1 \%}$ | $\mathbf{1 2 \%}$ | $\mathbf{1 3 \%}$ | $\mathbf{1 4 \%}$ | $\mathbf{1 5 \%}$ | $\mathbf{2 0 \%}$ | $\mathbf{2 5 \%}$ | $\mathbf{3 0 \%}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | 0.9524 | 0.9434 | 0.9346 | 0.9259 | 0.9174 | 0.9091 | 0.9009 | 0.8929 | 0.8850 | 0.8772 | 0.8696 | 0.8333 | 0.8000 | 0.7692 |
| $\boldsymbol{2}$ | 0.9070 | 0.8900 | 0.8734 | 0.8573 | 0.8417 | 0.8264 | 0.8116 | 0.7972 | 0.7831 | 0.7695 | 0.7561 | 0.6944 | 0.6400 | 0.5917 |
| $\mathbf{3}$ | 0.8638 | 0.8396 | 0.8163 | 0.7938 | 0.7722 | 0.7513 | 0.7312 | 0.7118 | 0.6931 | 0.6750 | 0.6575 | 0.5787 | 0.5120 | 0.4552 |
| $\mathbf{4}$ | 0.8227 | 0.7921 | 0.7629 | 0.7350 | 0.7084 | 0.6830 | 0.6587 | 0.6355 | 0.6133 | 0.5921 | 0.5718 | 0.4823 | 0.4096 | 0.3501 |
| $\mathbf{5}$ | 0.7835 | 0.7473 | 0.7130 | 0.6806 | 0.6499 | 0.6209 | 0.5935 | 0.5674 | 0.5428 | 0.5194 | 0.4972 | 0.4019 | 0.3277 | 0.2693 |
| $\mathbf{6}$ | 0.7462 | 0.7050 | 0.6663 | 0.6302 | 0.5963 | 0.5645 | 0.5346 | 0.5066 | 0.4803 | 0.4556 | 0.4323 | 0.3349 | 0.2621 | 0.2072 |
| $\mathbf{7}$ | 0.7107 | 0.6651 | 0.6227 | 0.5835 | 0.5470 | 0.5132 | 0.4817 | 0.4523 | 0.4251 | 0.3996 | 0.3759 | 0.2791 | 0.2097 | 0.1594 |
| $\boldsymbol{8}$ | 0.6768 | 0.6274 | 0.5820 | 0.5403 | 0.5019 | 0.4665 | 0.4339 | 0.4039 | 0.3762 | 0.3506 | 0.3269 | 0.2326 | 0.1678 | 0.1226 |
| $\mathbf{9}$ | 0.6446 | 0.5919 | 0.5439 | 0.5002 | 0.4604 | 0.4241 | 0.3909 | 0.3606 | 0.3329 | 0.3075 | 0.2843 | 0.1938 | 0.1342 | 0.0943 |
| $\mathbf{1 0}$ | 0.6139 | 0.5584 | 0.5083 | 0.4632 | 0.4224 | 0.3855 | 0.3522 | 0.3220 | 0.2946 | 0.2697 | 0.2472 | 0.1615 | 0.1074 | 0.0725 |
| $\mathbf{1 1}$ | 0.5847 | 0.5268 | 0.4751 | 0.4289 | 0.3875 | 0.3505 | 0.3173 | 0.2875 | 0.2607 | 0.2366 | 0.2149 | 0.1346 | 0.0859 | 0.0558 |
| $\mathbf{1 2}$ | 0.5568 | 0.4970 | 0.4440 | 0.3971 | 0.3555 | 0.3186 | 0.2858 | 0.2567 | 0.2307 | 0.2076 | 0.1869 | 0.1122 | 0.0687 | 0.0429 |
| $\mathbf{1 3}$ | 0.5303 | 0.4688 | 0.4150 | 0.3677 | 0.3262 | 0.2897 | 0.2575 | 0.2292 | 0.2042 | 0.1821 | 0.1625 | 0.0935 | 0.0550 | 0.0330 |
| $\mathbf{1 4}$ | 0.5051 | 0.4423 | 0.3878 | 0.3405 | 0.2992 | 0.2633 | 0.2320 | 0.2046 | 0.1807 | 0.1597 | 0.1413 | 0.0779 | 0.0440 | 0.0254 |
| $\mathbf{1 5}$ | 0.4810 | 0.4173 | 0.3624 | 0.3152 | 0.2745 | 0.2394 | 0.2090 | 0.1827 | 0.1599 | 0.1401 | 0.1229 | 0.0649 | 0.0352 | 0.0195 |
| $\mathbf{1 6}$ | 0.4581 | 0.3936 | 0.3387 | 0.2919 | 0.2519 | 0.2176 | 0.1883 | 0.1631 | 0.1415 | 0.1229 | 0.1069 | 0.0541 | 0.0281 | 0.0150 |
| $\mathbf{1 7}$ | 0.4363 | 0.3714 | 0.3166 | 0.2703 | 0.2311 | 0.1978 | 0.1696 | 0.1456 | 0.1252 | 0.1078 | 0.0929 | 0.0451 | 0.0225 | 0.0116 |
| $\mathbf{1 8}$ | 0.4155 | 0.3505 | 0.2959 | 0.2502 | 0.2120 | 0.1799 | 0.1528 | 0.1300 | 0.1108 | 0.0946 | 0.0808 | 0.0376 | 0.0180 | 0.0089 |
| $\mathbf{1 9}$ | 0.3957 | 0.3305 | 0.2765 | 0.2317 | 0.1945 | 0.1635 | 0.1377 | 0.1161 | 0.0981 | 0.0829 | 0.0703 | 0.0313 | 0.0144 | 0.0068 |
| $\mathbf{2 0}$ | 0.3769 | 0.3118 | 0.2584 | 0.2145 | 0.1784 | 0.1486 | 0.1240 | 0.1037 | 0.0868 | 0.0728 | 0.0611 | 0.0261 | 0.0115 | 0.0053 |

TABLE 2

Table II - Annuity Factor Table (PVAF)
Present Value of Annuity of $₹ 1$ per year (Cumulative Discounting Factor)

| Years | 5\% | 6\% | 7\% | 8\% | 9\% | 10\% | 11\% | 12\% | 13\% | 14\% | 15\% | 20\% | 25\% | 30\% |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.9524 | 0.9434 | 0.9346 | 0.9259 | 0.9174 | 0.9091 | 0.9009 | 0.8929 | 0.8850 | 0.8772 | 0.8696 | 0.8333 | 0.8000 | 0.7692 |
| 2 | 1.8594 | 1.8334 | 1.8080 | 1.7833 | 1.7591 | 1.7355 | 1.7125 | 1.6901 | 1.6681 | 1.6467 | 1.6257 | 1.5278 | 1.4400 | 1.3609 |
| 3 | 2.7232 | 2.6730 | 2.6243 | 2.5771 | 2.5313 | 2.4869 | 2.4437 | 2.4018 | 2.3612 | 2.3216 | 2.2832 | 2.1065 | 1.9520 | 1.8161 |
| 4 | 3.5460 | 3.4651 | 3.3872 | 3.3121 | 3.2397 | 3.1699 | 3.1024 | 3.0373 | 2.9745 | 2.9137 | 2.8550 | 2.5887 | 2.3616 | 2.1662 |
| 5 | 4.3295 | 4.2124 | 4.1002 | 3.9927 | 3.8897 | 3.7908 | 3.6959 | 3.6048 | 3.5172 | 3.4331 | 3.3522 | 2.9906 | 2.6893 | 2.4356 |
| 6 | 5.0757 | 4.9173 | 4.7665 | 4.6229 | 4.4859 | 4.3553 | 4.2305 | 4.1114 | 3.9975 | 3.8887 | 3.7845 | 3.3255 | 2.9514 | 2.6427 |
| 7 | 5.7864 | 5.5824 | 5.3893 | 5.2064 | 5.0330 | 4.8684 | 4.7122 | 4.5638 | 4.4226 | 4.2883 | 4.1604 | 3.6046 | 3.1611 | 2.8021 |
| 8 | 6.4632 | 6.2098 | 5.9713 | 5.7466 | 5.5348 | 5.3349 | 5.1461 | 4.9676 | 4.7988 | 4.6389 | 4.4873 | 3.8372 | 3.3289 | 2.9247 |
| 9 | 7.1078 | 6.8017 | 6.5152 | 6.2469 | 5.9952 | 5.7590 | 5.5370 | 5.3282 | 5.1317 | 4.9464 | 4.7716 | 4.0310 | 3.4631 | 3.0190 |
| 10 | 7.7217 | 7.3601 | 7.0236 | 6.7101 | 6.4177 | 6.1446 | 5.8892 | 5.6502 | 5.4262 | 5.2161 | 5.0188 | 4.1925 | 3.5705 | 3.0915 |
| 11 | 8.3064 | 7.8869 | 7.4987 | 7.1390 | 6.8052 | 6.4951 | 6.2065 | 5.9377 | 5.6869 | 5.4527 | 5.2337 | 4.3271 | 3.6564 | 3.1473 |
| 12 | 8.8633 | 8.3838 | 9.9427 | 7.5361 | 7.1607 | 6.8137 | 6.4924 | 6.1944 | 5.9176 | 5.6603 | 5.4206 | 4.4392 | 3.7251 | 3.1903 |
| 13 | 9.3936 | 8.8527 | 8.3577 | 7.9038 | 7.4869 | 7.1034 | 6.7499 | 6.4235 | 6.1218 | 5.8424 | 5.5831 | 4.5327 | 3.7801 | 3.2233 |
| 14 | 9.8986 | 9.2950 | 8.7455 | 8.2442 | 7.7862 | 7.3667 | 6.9819 | 6.6282 | 6.3025 | 6.0021 | 5.7245 | 4.6106 | 3.8241 | 3.2487 |
| 15 | 10.3797 | 9.7122 | 9.1079 | 8.5595 | 8.0607 | 7.6061 | 7.1909 | 6.8109 | 6.4624 | 6.1422 | 5.8474 | 4.6755 | 3.8593 | 3.2682 |
| 16 | 10.8378 | 10.1059 | 9.4466 | 8.8514 | 8.3126 | 7.8237 | 7.3792 | 6.9740 | 6.6039 | 6.2651 | 5.9542 | 4.7296 | 3.8874 | 3.2832 |
| 17 | 11.2741 | 10.4773 | 9.7632 | 9.1216 | 8.5436 | 8.0216 | 7.5488 | 7.1196 | 6.7291 | 6.3729 | 6.0472 | 4.7746 | 3.9099 | 3.2948 |
| 18 | 11.6896 | 10.8276 | 10.0591 | 9.3719 | 8.7556 | 8.2014 | 7.7016 | 7.2497 | 6.8399 | 6.4674 | 6.1280 | 4.8122 | 3.9279 | 3.3037 |
| 19 | 12.0853 | 11.1581 | 10.3356 | 9.6036 | 8.9501 | 8.3649 | 7.8393 | 7.3658 | 6.9380 | 6.5504 | 6.1982 | 4.8435 | 3.9424 | 3.3105 |
| 20 | 12.4622 | 11.4699 | 10.5940 | 9.8181 | 9.1285 | 8.5136 | 7.9633 | 7.4694 | 7.0248 | 6.6231 | 6.2593 | 4.8696 | 3.9539 | 3.3158 |

## Table III - Compound Value Table (FVIF) Compound Value of ₹ 1 after n year (Growth Factor)

| Years | $\mathbf{5 \%}$ | $\mathbf{6 \%}$ | $\mathbf{7 \%}$ | $\mathbf{8 \%}$ | $\mathbf{9 \%}$ | $\mathbf{1 0 \%}$ | $\mathbf{1 2 \%}$ | $\mathbf{1 4 \%}$ | $\mathbf{1 5 \%}$ | $\mathbf{1 6 \%}$ | $\mathbf{1 8 \%}$ | $\mathbf{2 0} \%$ | $\mathbf{2 4 \%}$ | $\mathbf{2 8 \%}$ | $\mathbf{3 2 \%}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | 1.050 | 1.060 | 1.070 | 1.080 | 1.090 | 1.100 | 1.120 | 1.130 | 1.150 | 1.160 | 1.180 | 1.200 | 1.240 | 1.280 | 1.320 |
| $\mathbf{2}$ | 1.102 | 1.124 | 1.115 | 1.166 | 1.188 | 1.210 | 1.254 | 1.300 | 1.322 | 1.346 | 1.392 | 1.440 | 1.538 | 1.638 | 1.742 |
| $\mathbf{3}$ | 1.158 | 1.191 | 1.225 | 1.260 | 1.295 | 1.331 | 1.405 | 1.482 | 1.521 | 1.561 | 1.643 | 1.728 | 1.907 | 2.097 | 2.300 |
| $\mathbf{4}$ | 1.216 | 1.262 | 1.311 | 1.360 | 1.412 | 1.464 | 1.574 | 1.689 | 1.749 | 1.811 | 1.939 | 2.074 | 2.364 | 2.984 | 3.036 |
| $\mathbf{5}$ | 1.276 | 1.338 | 1.403 | 1.469 | 1.539 | 1.611 | 1.762 | 1.925 | 2.011 | 2.100 | 2.288 | 2.488 | 2.932 | 3.436 | 4.008 |
| $\mathbf{6}$ | 1.340 | 1.419 | 1.501 | 1.677 | 1.677 | 1.772 | 1.974 | 2.193 | 2.313 | 2.436 | 2.700 | 2.986 | 3.635 | 4.396 | 5.290 |
| $\mathbf{7}$ | 1.407 | 1.504 | 1.606 | 1.714 | 1.828 | 1.949 | 2.211 | 2.505 | 2.660 | 2.826 | 3.186 | 3.583 | 4.508 | 5.630 | 6.983 |
| $\boldsymbol{8}$ | 1.477 | 1.594 | 1.718 | 1.851 | 1.993 | 2.144 | 2.467 | 2.853 | 3.059 | 3.278 | 3.759 | 4.300 | 5.590 | 7.206 | 9.217 |
| $\mathbf{9}$ | 1.551 | 1.689 | 1.838 | 1.999 | 2.172 | 2.358 | 2.773 | 3.252 | 3.518 | 3.803 | 4.436 | 5.160 | 6.931 | 9.223 | 12.116 |
| $\mathbf{1 0}$ | 1.629 | 1.791 | 1.967 | 2.159 | 2.367 | 2.594 | 3.106 | 3.707 | 4.046 | 4.411 | 5.234 | 6.192 | 8.594 | 11.806 | 16.060 |
| $\mathbf{1 1}$ | 1.710 | 1.898 | 2.105 | 2.332 | 2.580 | 2.853 | 3.479 | 4.206 | 4.652 | 5.117 | 6.176 | 7.430 | 10.657 | 15.112 | 21.119 |
| $\mathbf{1 2}$ | 1.796 | 2.012 | 2.252 | 2.518 | 2.813 | 3.138 | 3.896 | 4.818 | 5.350 | 5.936 | 7.288 | 8.916 | 13.215 | 19.343 | 27.983 |
| $\mathbf{1 3}$ | 1.888 | 2.132 | 2.410 | 2.730 | 3.006 | 3.452 | 4.363 | 5.492 | 6.153 | 6.886 | 8.599 | 10.699 | 16.386 | 24.795 | 36.937 |
| $\mathbf{1 4}$ | 1.980 | 2.261 | 2.579 | 2.937 | 3.342 | 3.797 | 4.887 | 6.261 | 7.071 | 7.988 | 10.147 | 12.839 | 20.319 | 31.691 | 48.757 |
| $\mathbf{1 5}$ | 2.079 | 2.397 | 2.579 | 3.172 | 3.642 | 4.177 | 5.474 | 7.138 | 8.13 | 9.266 | 11.974 | 15.407 | 25.196 | 40.565 | 64.359 |
| $\mathbf{1 6}$ | 2.186 | 2.540 | 2.952 | 3.426 | 3.970 | 4.595 | 6.130 | 8.137 | 9.35 | 10.748 | 14.129 | 18.488 | 31.243 | 51.923 | 84.954 |
| $\mathbf{1 7}$ | 2.292 | 2.613 | 3.159 | 3.700 | 4.328 | 5.554 | 6.866 | 9.276 | 10.70 | 12.468 | 16.672 | 22.186 | 38.741 | 66.461 | 112.41 |
| $\mathbf{1 8}$ | 2.407 | 2.854 | 3.380 | 5.996 | 4.717 | 5.560 | 7.690 | 10.533 | 12.3 | 14.463 | 19.673 | 26.623 | 48.039 | 85.071 | 148.02 |
| $\mathbf{1 9}$ | 2.527 | 3.026 | 3.617 | 4.316 | 5.142 | 6.116 | 8.613 | 12.743 | 14.2 | 16.777 | 23.214 | 31.948 | 59.568 | 108.89 | 159.39 |
| $\mathbf{2 0}$ | 2.653 | 3.207 | 3.870 | 4.661 | 5.604 | 6.728 | 9.646 | 13.743 | 16.3 | 19.461 | 27.393 | 38.338 | 73.864 | 139.38 | 257.92 |

