## FAVOURABLE INCOME DIFERENTIAL PER SHARE, PREMIUM PAY BACK PERIOD ETC.

## QUESTION NO.29A(RTP)

| Face Value | `1000 & M arket Price of Convertible Debenture &` 900 |  |  |
| :--- | :--- | :--- | :--- |
| Conversion Ratio | 30 | Straight Value of Debenture |  |
| $8.5 \%$ Fully Convertible (into Equity shares) | Debentures |  |  |
| M arket Price of Equity share |  | 25 | Expected Dividend Per Share |

You are required to calculate: (a)Fair Conversion Value of Debenture As On Today OR Conversion Value of Debenture (b)Conversion Parity Price Of Equity Shares OR M arket Conversion Price (c)Conversion Parity Price Premium per Equity share OR Conversion Premium Per Share (d)Ratio of Conversion Parity Price Premium OR Ratio of Conversion Premium (e)Downside Risk or Premium over Straight Value of Debenture (f)Favourable income differential per share (g)Premium pay back period
Solution:
(a) $\underline{\text { Conversion Value of Debenture }}=25 \times 30=` 750$; (b) Parity Price $=\left[\frac{\mathrm{MV} \text { of CB }}{\text { Convarision Ratio }}\right]=\left[\frac{900}{30}\right]=` 30$
(c) Parity Price Premium $=30-25={ }^{`} 5$; (d) Parity Price Premium (\%) $=\left[\frac{30-25}{25}\right]=20 \%$
(e)Down Side Risk : in `: \(900-700=` 200\); in \%: $\left[\frac{900-700}{700}\right]=28.57$ or $\left[\frac{900-700}{900}\right]=22.22$
(f)Favourable income differential per share

If not converted: Income p.a $=1000 \times 8.5 \%=` 85$; if converted: 30 share x $` 1=` 30$
$\therefore$ (Favourable) Income difference $=` 85-` 30=` 55 ; ~ \therefore$ Per share: $\frac{85-30}{30 \text { No.0f ES }}=1.833$ per share
(g)Premium pay back period: Premium PBP $=\frac{\text { Extra Initial Investment }}{\text { Extra Annual CF }}=\frac{150}{55}=2.73$ Years

## CALCULATION OF FACE VALUE WHEN DIFFERENCE BETWEEN TWO BO IS GIVEN

QUESTION NO.54(4 Marks) A bond is held for a period of 45 days. The current discount yield is 6 percent per annum. It is expected that current yield will increase by 200 basis points and current market price will come down by ` 2.50. Calculate: (i)Face value of the Bond and (ii)Bond Equivalent Yield. Assume 360 days in a year.

## Solution:

## (i) Face Value of the Bond:

When Kd is $6 \%$ with 45days maturity period : At ' 1 face value, Present Value will be $\frac{1}{1+\frac{.06}{360} \times 45}=0.9925$
When Kd is $8 \%$ with 45days maturity period : At ` 1 face value, Present Value will be $\frac{1}{1+\frac{.08}{360} \times 45}=0.9900$

Difference in Price at `1 Face Value \(=0.0025\); So when difference is .0025 , face value is` 1 ; When difference is 1 , face value will be $\frac{1}{.0025}$
When difference is 2.5 , face value will be $\frac{1}{.0025} \times 2.5=` 1,000$

## Also Current Market Price in each case will be:

## When Discount Rate is 6\%

When ` 1 is face value,CM P is 0.9925 ,therefore when \({ }^{`} 1000\) is face value, CM P will be $1000 \times 0.9925=99.25$ When Discount Rate is $8 \%$
When `1 is face value, CMP is 0.9900 , therefore when` 1000 is face value, CM P will be $1000 \times 0.9900=90.90$ (ii) Bond Equivalent Yield (or Simply Return or Holding Period Return)

At the rate of $6 \%=\frac{1000-992.50}{992.50} \times \frac{360}{45} \times 100=6.05 \%$; At the rate of $8 \%=\frac{1000-990}{990} \times \frac{360}{45} \times 100=8.08 \%$

## QUESTION NO.58D The following data are available for a bond:

Face Value ` 10,000 to be redeemed at par on maturity ; Coupon rate $8.5 \%$ per annum ; Years to $M$ aturity 5 years Yield to M aturity (YTM ) 10 per cent You are required to calculate:
(i)Current market price of the Bond, (ii)M acaulay's Duration, (iii)Volatility of the Bond, (iv)Convexity of the Bond, (v)Expected market price, if there is a decrease in the YTM by 200 basis points
(a)By M acaulay's Duration based estimate (b)By Intrinsic Value M ethod.

| Years | $\underline{\mathbf{1}}$ | $\underline{\mathbf{2}}$ | $\underline{\mathbf{3}}$ | $\underline{\mathbf{4}}$ | $\underline{\mathbf{5}}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| PVIF $(10 \%$, n) | 0.909 | 0.826 | 0.751 | 0.683 | 0.621 |
| PVIF $(8 \%$, n) | 0.926 | 0.857 | 0.794 | 0.735 | 0.681 |

Solution:
(i)Current Market Price of Bond
$=` 850($ PVAF $10 \%, 5)+` 10,000($ PVF $10 \%, 5)=` 850(3.79)+` 10,000(0.621)=` 3,221.50+` 6,210=` 9,431.5$
(ii)Macaulay's Duration

| Year | Cash flow | P.V. @ 10\% |  | Proportion of bond value | Proportion of bond value $x$ time (years) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 850 | 0.909 | 772.65 | 0.082 | 0.082 |
| 2 | 850 | 0.826 | 702.10 | 0.074 | 0.148 |
| 3 | 850 | 0.751 | 638.35 | 0.068 | 0.204 |
| 4 | 850 | 0.683 | 580.55 | 0.062 | 0.248 |
| 5 | 10,850 | 0.621 | 6,737.85 | 0.714 | 3.57 |
|  |  |  | $\underline{9431.50}$ | 1.000 | $\underline{4.252}$ |

Duration of the Bond is 4.252 years
(iii) Volatility of Bond: Volatility of Bonds $=\frac{\text { Duration }}{(1+\text { YTM })}=\frac{4.252}{1.10}=3.865$
(iv)Convexity of Bond

| Year | Cash flow | P.V. @ 8\% |  | P.V @ 12\% |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 850 | 0.926 | 787.10 | 0.892 | 758.20 |
| 2 | 850 | 0.857 | 728.45 | 0.797 | 677.45 |
| 3 | 850 | 0.794 | 674.90 | 0.712 | 605.20 |
| 4 | 850 | 0.735 | 624.75 | 0.636 | 540.60 |

> Think big.Think positive.Think to do Different.Think to achieve.
> Drop of water in lake has no identity, but if it falls on lotus, it shines like pearl.

| 5 | 10,850 | 0.681 | $\underline{7388.85}$ | 0.567 | $\underline{6,151.95}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  |  | $\underline{10204.05}$ |  | $\underline{8,733.40}$ |  |

Approximate Modified Convexity $=\frac{B_{+}+B_{-}-2 B_{0}}{2 \times B_{0}(\Delta y)^{2}}=\frac{10204.05+8733.40-2(9431.5)}{2 \times 9431.5(0.02)^{2}}=9.867$
Convexity of Bond $=9.867 \times(0.02)^{2} \times 100=0.395 \%$ [Additional Analysis: This part is added extra by Institute. This part is not $100 \%$ correct. However students can add this point in exam, whenever convexity points comes in exam, in all above questions also like $\mathrm{Q} .58 \mathrm{~A} ; \mathrm{B} ; \mathrm{C}]$
(v)The expected market price if decrease in YTM by 200 basis points.
(A)By Macaulay's duration-based estimate: \% Change(Increase) in Bond Value $=3.865 \times .02=.0773$

Hence expected market price is ` \(9431.50+` 9431.50 \times .0773=` 10,160.55\)
Hence, the market price will increase. In other words, if YTM decreases, Bond Value will increase.
(B)By Intrinsic Value method

| Year | Cash flow | P.V. @ |  |
| :---: | :---: | :---: | :---: |
| 1 | 850 | 0.926 | 787.10 |
| 2 | 850 | 0.857 | 728.45 |
| 3 | 850 | 0.794 | 674.90 |
| 4 | 850 | 0.735 | 624.75 |
| 5 | 10,850 | 0.681 | 7388.85 |
|  |  |  | $\underline{10204.05}$ |

## WHEN BOND IMMUNIZATION CONCEPT FAILS

QUESTION NO. 59 ( 12 M arks) The following data are available for three bonds $A, B$ and $C$. These bonds are used by a bond portfolio manager to fund an outflow scheduled in 6 years. Current yield is $9 \%$. All bonds have face value of ` 100 each and will be redeemed at par. Interest is payable annually.

| Bond |  | Maturity (Years) |  |
| :--- | :--- | :--- | :--- |
| A |  | Coupon rate |  |
| B | 8 | $10 \%$ |  |
| C | 5 |  | $11 \%$ |
|  | 5 | $9 \%$ |  |

(i)Calculate the duration of each bond.
(ii)The bond portfolio manager has been asked to keep $45 \%$ of the portfolio money in Bond A . Calculate the percentage amount to be invested in bonds $B$ and $C$ that need to be purchased to immunise the portfolio.
(iii) After the portfolio has been formulated, an interest rate change occurs, increasing the yield to $11 \%$. The new duration of these bonds are: Bond $A=7.15$ years, Bond $B=6.03$ years and Bond $C=4.27$ years the portfolio still immunized? Why or why not?
(iv)Determine the new percentage of $B$ and $C$ bonds that are needed to immunize the portfolio. Bond $A$ remaining at $45 \%$ of the portfolio.
Present values be used as follows:

| Present Values | t1 | t2 | t3 | t4 | t5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| PVIF0.09,t | 0.917 | 0.842 | 0.772 | 0.708 | 0.650 |
| Present Values | t6 | t7 | t8 | T9 | +10 |
| PVIF0.09, t | 0.596 | 0.547 | 0.502 | 0.460 | 0.4224 |
| Solution: |  |  |  |  |  |

(i)Calculation of Bond Duration

Bond A

| Year | Cash flow | PVF@ 9\% | PV | Weights | Weights x time (years) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 10 | 0.917 | 9.17 | 0.086 | 0.086 |
| 2 | 10 | 0.842 | 8.42 | 0.079 | 0.158 |
| 3 | 10 | 0.772 | 7.72 | 0.073 | 0.219 |
| 4 | 10 | 0.708 | 7.08 | 0.067 | 0.268 |
| 5 | 10 | 0.650 | 6.50 | 0.061 | 0.305 |
| 6 | 10 | 0.596 | 5.96 | 0.056 | 0.336 |
| 7 | 10 | 0.547 | 5.47 | 0.051 | 0.357 |
| 8 | 10 | 0.502 | 5.02 | 0.047 | 0.376 |
| 9 | 10 | 0.460 | 4.60 | 0.043 | 0.387 |
| 10 | 110 | 0.4224 | 46.46 | 0.437 | 4.370 |
|  |  |  | 106.40 | 1.000 | $\underline{6.862}$ |

Duration of the bond is 6.862 years or 6.86 years.
Bond B

| Year | Cash flow | PVF@ 9\% | PV | Weights | Weights x time (years) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 11 | 0.917 | 10.087 | 0.091 | 0.091 |
| 2 | 11 | 0.842 | 9.262 | 0.083 | 0.166 |
| 3 | 11 | 0.772 | 8.492 | 0.076 | 0.228 |
| 4 | 11 | 0.708 | 7.788 | 0.070 | 0.280 |
| 5 | 11 | 0.650 | 7.150 | 0.064 | 0.320 |
| 6 | 11 | 0.596 | 6.556 | 0.059 | 0.354 |
| 7 | 11 | 0.547 | 6.017 | 0.054 | 0.378 |
| 8 | 111 | 0.502 | 55.722 | 0.502 | 4.016 |
|  |  |  | $\underline{111.224} 1$ |  | 5.833 |
| Duration of the bond B is 5.833 years or 5.84 years Bond C |  |  |  |  |  |
| Year | Cash flow | PVF@ 9\% | PV | Weights | Weights x time (years) |
| 1 | 9 | 0.917 | 8.253 | 0.082 | 0.082 |
| 2 | 9 | 0.842 | 7.578 | 0.076 | 0.152 |
| 3 | 9 | 0.772 | 6.948 | 0.069 | 0.207 |
| 4 | 9 | 0.708 | 6.372 | 0.064 | 0.256 |
| 5 | 109 | 0.650 | 70.850 | 0.709 | 3.545 |
|  |  |  | 100.00 | 1.000 | $\underline{4.242}$ |

Duration of the bond $C$ is 4.242 years or 4.24 years
(ii) Amount of Investment required in Bond B and C

Alt 1: $.45 \times 6.862+W b \times 5.833+(1-.45-W b) \times 4.242=6$ or $W b=.363125$ or $36.31 \%$; Therefore $\mathrm{Wc}=18.69 \%$ Alt 2:
Period required to be immunized
Less: Period covered from Bond A
To be immunized from $B$ and $C$
6.000 Years
3.087 Years
2.913 Years

Let proportion of investment in Bond $B$ and $C$ is $b$ and $c$ respectively then $b+c=0.55 ; 5.883 b+4.242 c=2.913$ On solving these equations, the value of $b$ and $c$ comes 0.3534 or 0.3621 and 0.1966 or 0.1879 respectively and accordingly, the \% of investment of $B$ and $C$ is $35.34 \%$ or $36.21 \%$ and $19.66 \%$ or $18.79 \%$ respectively.
Note: Any Alternative can be used in exam

Do not mix the words with your mood because you will have many options to change the mood but you will never get any option to replace the spoken words.
(iii) With revised yield the Revised Duration of Bond stands
$0.45 \times 7.15+0.36 \times 6.03+0.19 \times 4.27=6.20$ years
Comment: No portfolio is not immunized as the duration of the portfolio has been increased from 6 years to 6.20 years.
(iv) New percentage of B and C bonds that are needed to immunize the portfolio.

Alt 1: $.45 \times 7.15+$ Wb $\times 6.03+(1-.45-W b) \times 4.27=6$
or $3.2175+6.03 \mathrm{~Wb}+2.3485-4.27 \mathrm{~Wb}=6$ or $1.76 \mathrm{~Wb}=.434$ or $\mathrm{Wb}=24.66 \%$; Therefore $\mathrm{Wc}=30.34 \%$
Alt 2:
Period required to be immunized 6.0000 Years
Less: Period covered from Bond A
To be immunized from $B$ and $C$
3.2175 Years
2.7825 Years

Let proportion of investment in Bond $B$ and $C$ is $b$ and $c$ respectively, then $b+c=0.55 ; 6.03 b+4.27 c=2.7825$
On solving these equations, the value of $b$ and $c$ comes 0.2466 and 0.3034 respectively and accordingly, the $\%$ of investment of $B$ and $C$ is $24.66 \%$ or $25 \%$ and $30.34 \%$ or $30.00 \%$ respectively.

## YIELD CURVE

QUESTION NO.60 ABC Ltd. wants to issue 9\% Bonds redeemable in 5 years at its face value of ` 1,000 each. The annual spot yield curve for similar risk class of Bond is as follows:

| Year | $\underline{1}$ | $\underline{2}$ | $\underline{3}$ | $\underline{4}$ | $\underline{\mathbf{5}}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Interest Rate | $\underline{1} 2 \%$ | $11.62 \%$ | $11.33 \%$ | $\underline{11.06 \%}$ | $\underline{10.80 \%}$ |

(i)Evaluate the expected market price of the Bond if it has a Beta value of 1.10 due to its popularity because of lesser risk.
(ii)Interpret the nature of the above yield curve and reasons for the same.

Note: Use PV Factors upto 4 decimal points and value in ` upto 2 decimal points.

## Solution:

(i)For finding expected market price first we shall calculate Intrinsic Value of Bond as follows:

PV of Interest + PV of M aturity Value of Bond
Forward rate of interests
1st Year 12\%
2nd Year 11.62\%
3rd Year 11.33\%
4th Year 11.06\%
5th Year 10.80\%
PV of interest $=\frac{90}{(1+0.12)}+\frac{90}{(1+0.1162)^{2}}+\frac{90}{(1+0.1133)^{3}}+\frac{90}{(1+0.1106)^{4}}+\frac{90}{(1+0.1080)^{5}}$
$=` 90 \times 0.8929+` 90 \times 0.8026+` 90 \times 0.7247+` 90 \times 0.6573+` 90 \times 0.5988$
$=` 80.36+` 72.23+` 65.22+` 59.16+` 53.89=` 330.86$
PV of M aturity Value of Bond $=\frac{1000}{(1+0.1080)^{5}}=` 1,000 \times 0.5988=` 598.80$
Intrinsic value of Bond =` \(330.86+` 598.80=` 929.66\) Expected Price \(=\) Intrinsic Value \(\times\) Beta Value \(=` 929.66 \times 1.10=` 1,022.63\)
(ii)The given yield curve is inverted yield curve.

The main reason for this shape of curve is expectation for forthcoming recession when investors aremore interested in Short-term rates over the long term.

> If you want to build a positive attitude, learn the phrase, "do it now" and stop the habit of procrastination.


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| Roll Number | A26168 |
| :--- | :--- |
| Name | ADITYA MTTAL |
| Group I |  |
| Financial Reporting | 052 |
| Strategic Financial Management | 100 |
| Advanced Audting and Professional Ehics | 059 |
| Corporate and Alled Laws | 057 |
| Total | 278 |
| Result | PASS |
| Group II |  |
| Advanced Management Accounting | 083 |
| Information Systems Control and Audit | 059 |
| Direct Tax Laws | 073 |
| Indirect Tax Laws | 072 |
| Total | 287 |
| Result | PASS |
| Grand Total | 565 |



## 100 OUT OF 100 IN SFM

"Every successfull person has a painfull story" .."Every painfull story has a successfull ending" ... Accept the pain \& get ready to success.

